

# Light neutrinos in cosmology

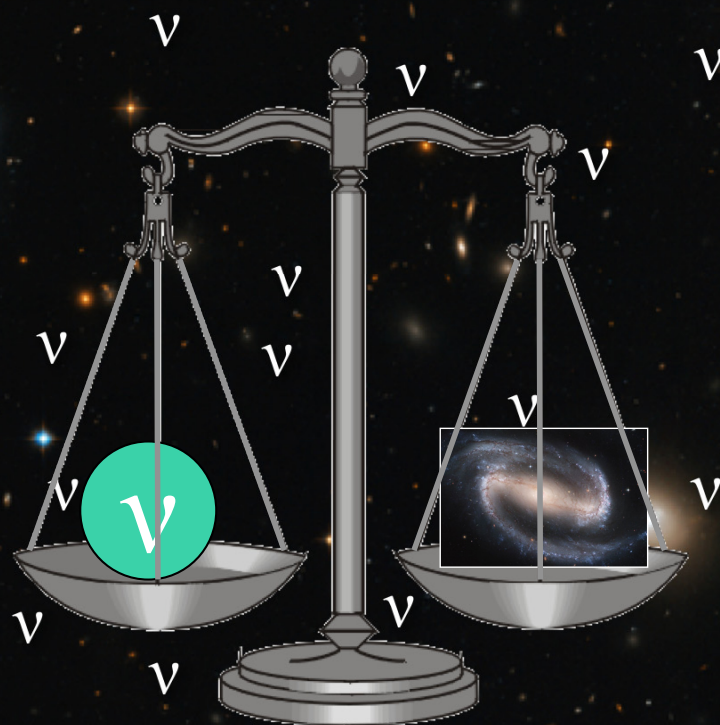
**Sergio Pastor**  
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**CIEMAT**  
Madrid, 3 Nov 2010



# Light neutrinos in cosmology



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# Outline

Introduction: the Cosmic Neutrino Background

The radiation content of the Universe

Neutrinos as Dark Matter

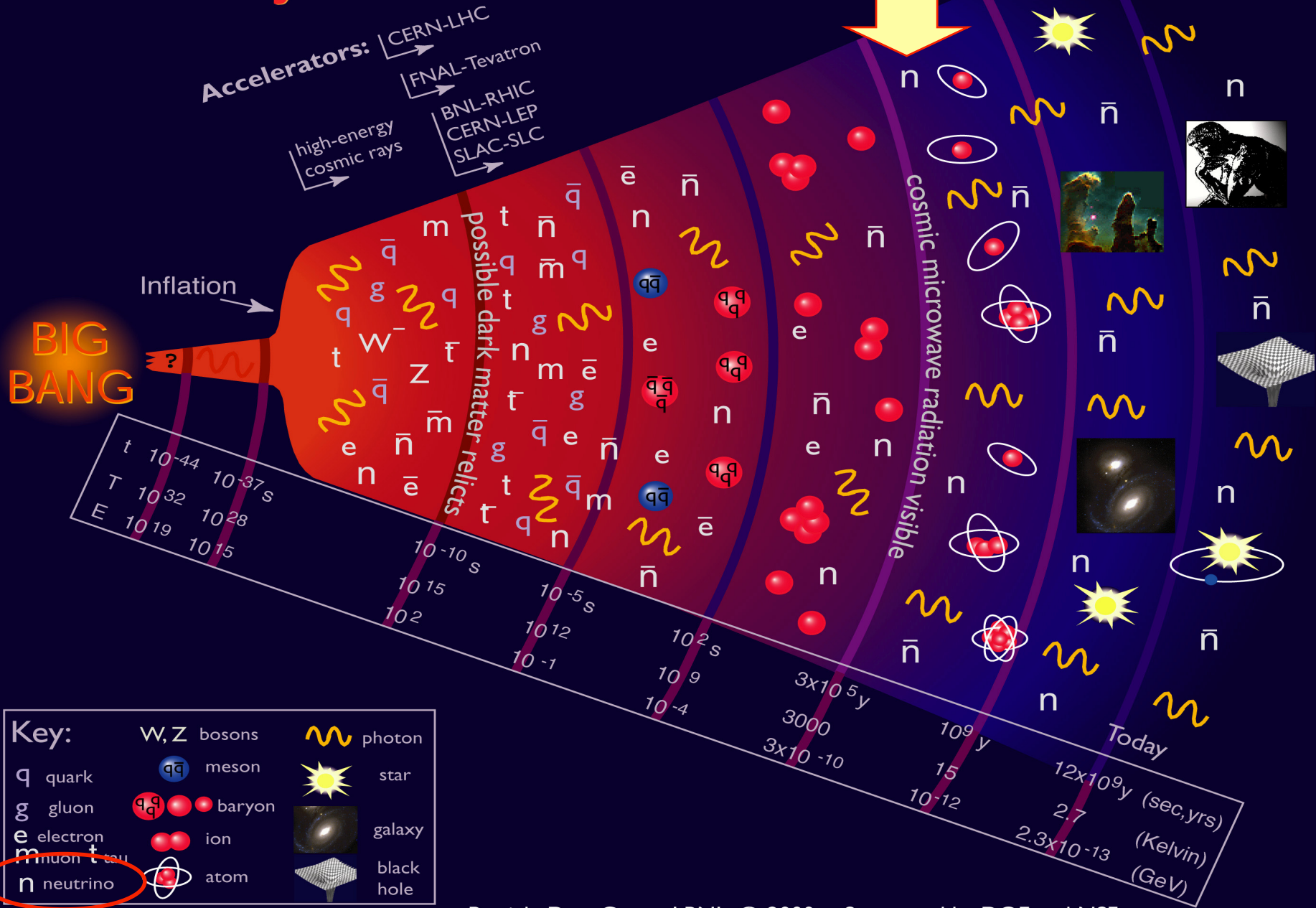
Cosmological bounds on  $\Sigma m_\nu$

# Introduction: the Cosmic Neutrino Background



# History of the Universe

This is a neutrino!



# History of the Universe

Neutrinos coupled  
by weak interactions

Decoupled neutrinos  
(Cosmic Neutrino  
Background, CNB/CvB)

BIG  
BANG

Inflation

high-energy  
cosmic rays

AL-RHC  
CERN-LEP  
SLAC-SLC

possible dark matter relicts

cosmic microwave radiation visible

$t$   $10^{-44}$   $10^{-37}$ s  
 $T$   $10^{32}$   $10^{28}$   
 $E$   $10^{19}$   $10^{15}$

$10^{-10}$ s  
 $10^{-15}$   
 $10^{-12}$   
 $10^{-1}$

$T \sim \text{MeV}$   
 $t \sim \text{sec}$

Primordial  
Nucleosynthesis

Key:

|             |            |
|-------------|------------|
| W, Z bosons | photon     |
| quark       | meson      |
| gluon       | baryon     |
| electron    | ion        |
| muon        | atom       |
| tau         | star       |
| neutrino    | galaxy     |
|             | black hole |

# Neutrinos in Equilibrium

$$1 \text{ MeV} \leq T \leq m_\mu$$

$$T_\nu = T_e = T_\gamma$$

$$\nu_\alpha \nu_\beta \leftrightarrow \bar{\nu}_\alpha \bar{\nu}_\beta$$

$$\nu_\alpha \bar{\nu}_\beta \leftrightarrow \bar{\nu}_\alpha \nu_\beta$$

$$\nu_\alpha e^- \leftrightarrow \bar{\nu}_\alpha e^-$$

$$\nu_\alpha \bar{\nu}_\alpha \leftrightarrow e^+ e^-$$

$$\mathcal{L}_{\text{SM}} = -2\sqrt{2}G_F \left\{ (\bar{\nu}_e \gamma^\mu L \nu_e) (\bar{e} \gamma_\mu L e) + \sum_{P, \alpha} g_P (\bar{\nu}_\alpha \gamma^\mu L \nu_\alpha) (\bar{e} \gamma_\mu P e) \right\}$$

$$P = L, R = (1 \mp \gamma_5)/2$$

$$g_L = -\frac{1}{2} + \sin^2 \theta_W \text{ and } g_R = \sin^2 \theta_W$$

# Neutrino decoupling

As the Universe expands, particle densities are diluted and temperatures fall. Weak interactions become **ineffective** to keep neutrinos in good thermal contact with the e.m. plasma

Rough, but quite accurate estimate of the decoupling temperature

Rate of weak processes  $\sim$  Hubble expansion rate

$$\Gamma_w \approx \sigma_w |v| n, \quad H^2 = \frac{8\pi\rho_R}{3M_p^2} \rightarrow G_F^2 T^5 \approx \sqrt{\frac{8\pi\rho_R}{3M_p^2}} \rightarrow T_{dec}^v \approx 1 \text{ MeV}$$



# History of the Universe

Neutrinos coupled  
by weak interactions  
(in equilibrium)

Free-streaming  
neutrinos (decoupled)  
Cosmic Neutrino  
Background

$$f_v(p, T) = \frac{1}{e^{p/T} + 1}$$

BIG  
BANG

Neutrinos keep the energy  
spectrum of a relativistic  
fermion with eq form

Key:

|             |            |
|-------------|------------|
| W, Z bosons | photon     |
| quark       | meson      |
| gluon       | baryon     |
| electron    | ion        |
| muon        | atom       |
| tau         | black hole |
| neutrino    |            |

$T \sim \text{MeV}$   
 $t \sim \text{sec}$

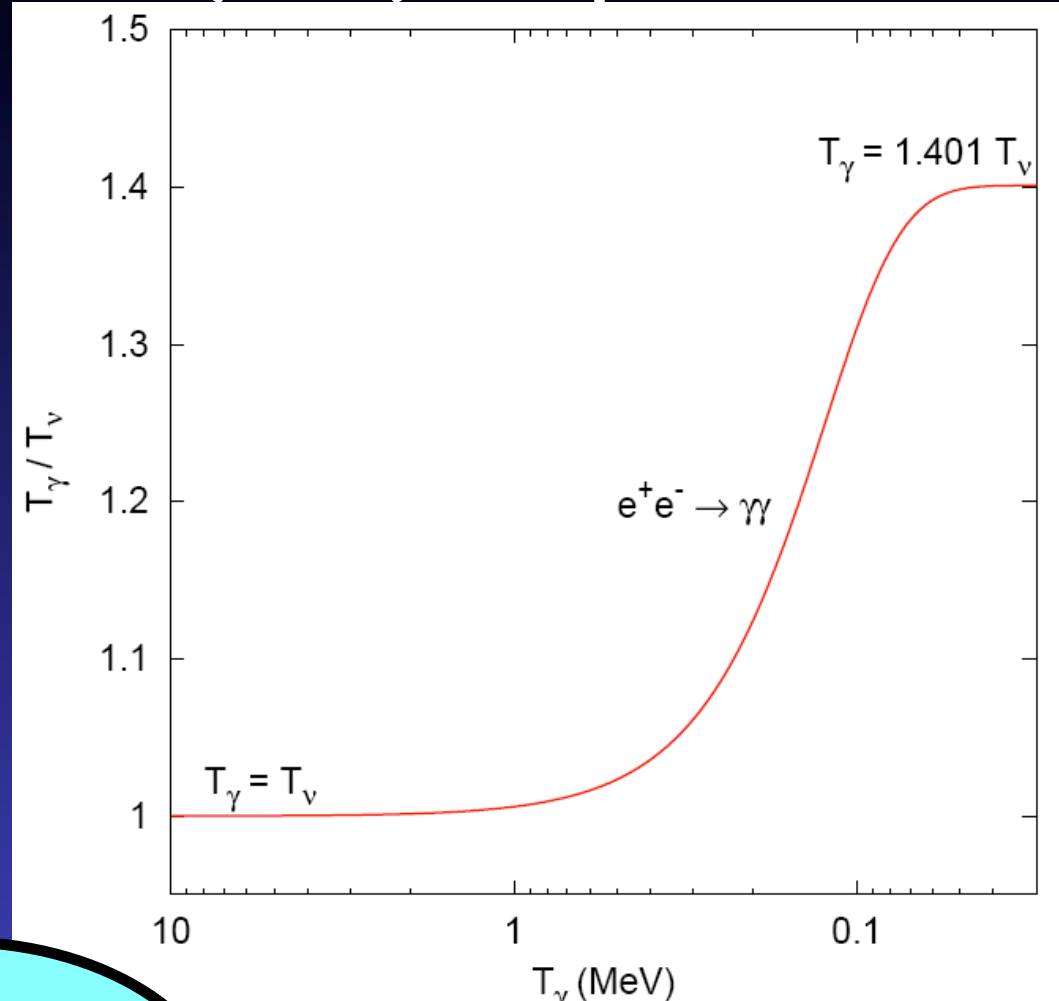
# Neutrino and Photon (CMB) temperatures

At  $T \sim m_e$ ,  
electron-  
positron pairs  
annihilate



heating photons  
but not the  
decoupled  
neutrinos

$$\frac{T_\gamma}{T_\nu} = \left(\frac{11}{4}\right)^{1/3}$$



$$f_\nu(p, T) = \frac{1}{e^{p/T_\nu} + 1}$$

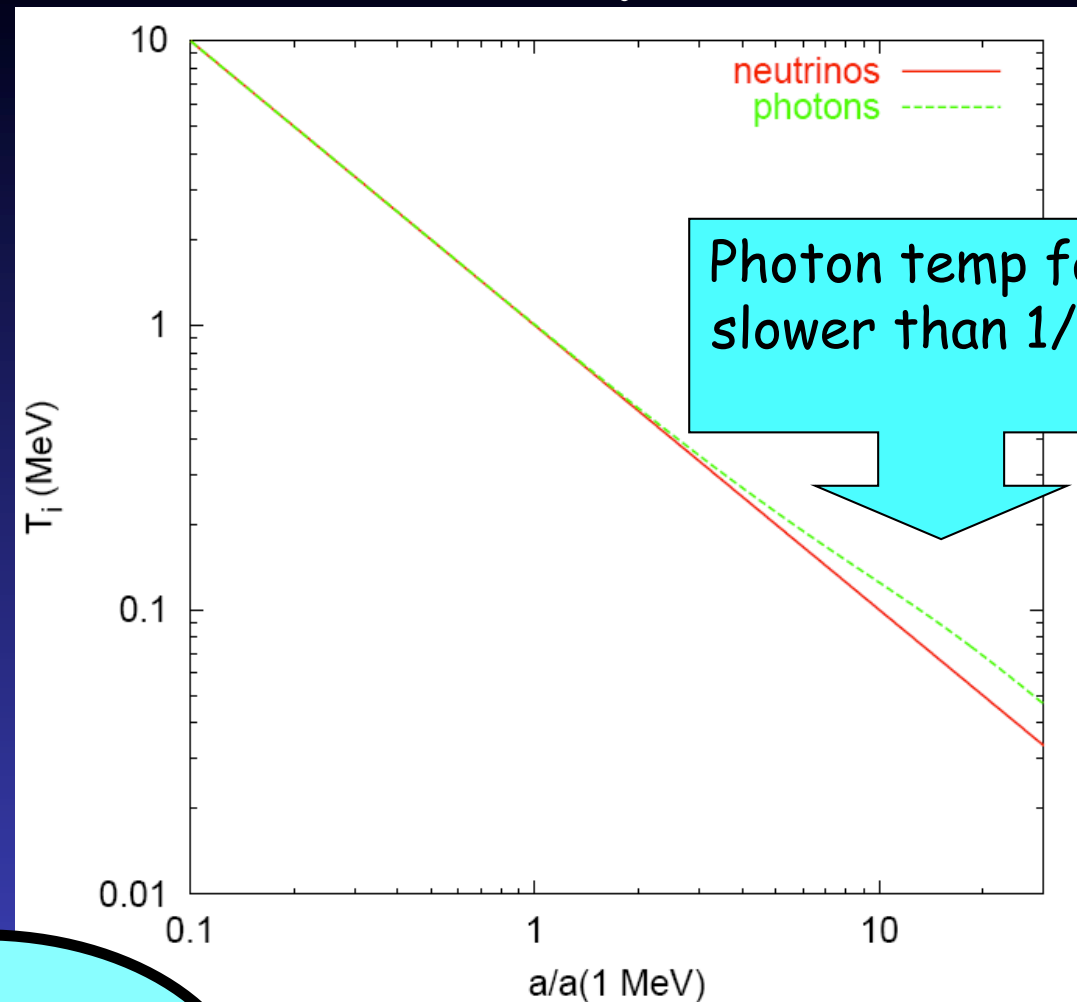
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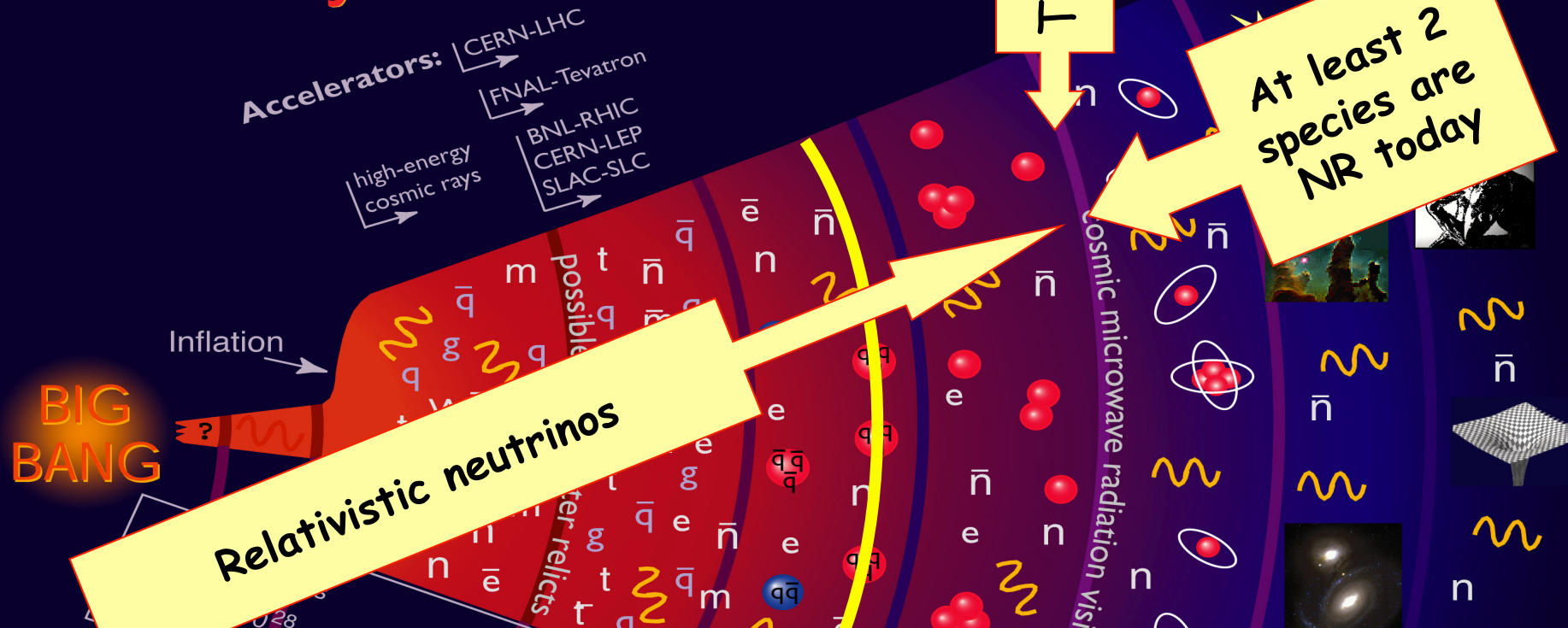
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$$f_\nu(p, T) = \frac{1}{e^{p/T_\nu} + 1}$$

# History of the Universe



Neutrino cosmology is interesting because **Relic neutrinos are very abundant:**

- The CNB contributes to radiation at early times and to matter at late times (info on the number of neutrinos and their masses)
- Cosmological observables can be used to test standard or non-standard neutrino properties



# The Cosmic Neutrino Background

Neutrinos decoupled at  $T \sim \text{MeV}$ , keeping a spectrum as that of a relativistic species

$$f_v(p, T) = \frac{1}{e^{p/T_v} + 1}$$

- Number density

$$n_v = \int \frac{d^3 p}{(2\pi)^3} f_v(p, T_v) = \frac{3}{11} n_\gamma = \frac{6\zeta(3)}{11\pi^2} T_{CMB}^3$$

- Energy density

$$\rho_{v_i} = \int \sqrt{p^2 + m_{v_i}^2} \frac{d^3 p}{(2\pi)^3} f_v(p, T_v) \rightarrow \begin{cases} \frac{7\pi^2}{120} \left(\frac{4}{11}\right)^{4/3} T_{CMB}^4 & \text{Massless} \\ m_{v_i} n_v & \text{Massive } m_v \gg T \end{cases}$$

# The Cosmic Neutrino Background

Neutrinos decoupled at  $T \sim \text{MeV}$ , keeping a spectrum as that of a relativistic species

$$f_\nu(p, T) = \frac{1}{e^{p/T_\nu} + 1}$$

- Number density

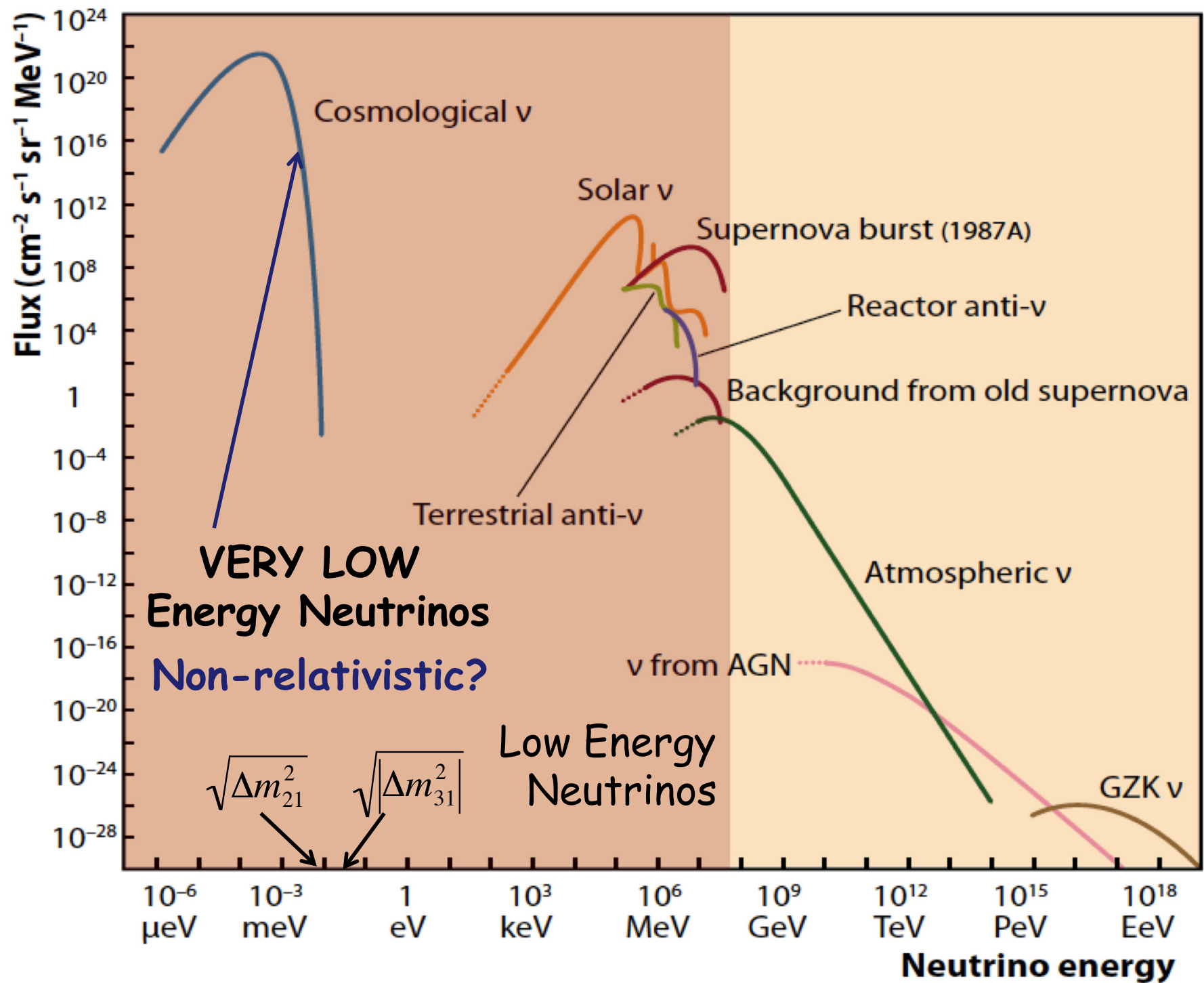
At present  $112 (\nu + \bar{\nu}) \text{ cm}^{-3}$  per flavour

- Energy density

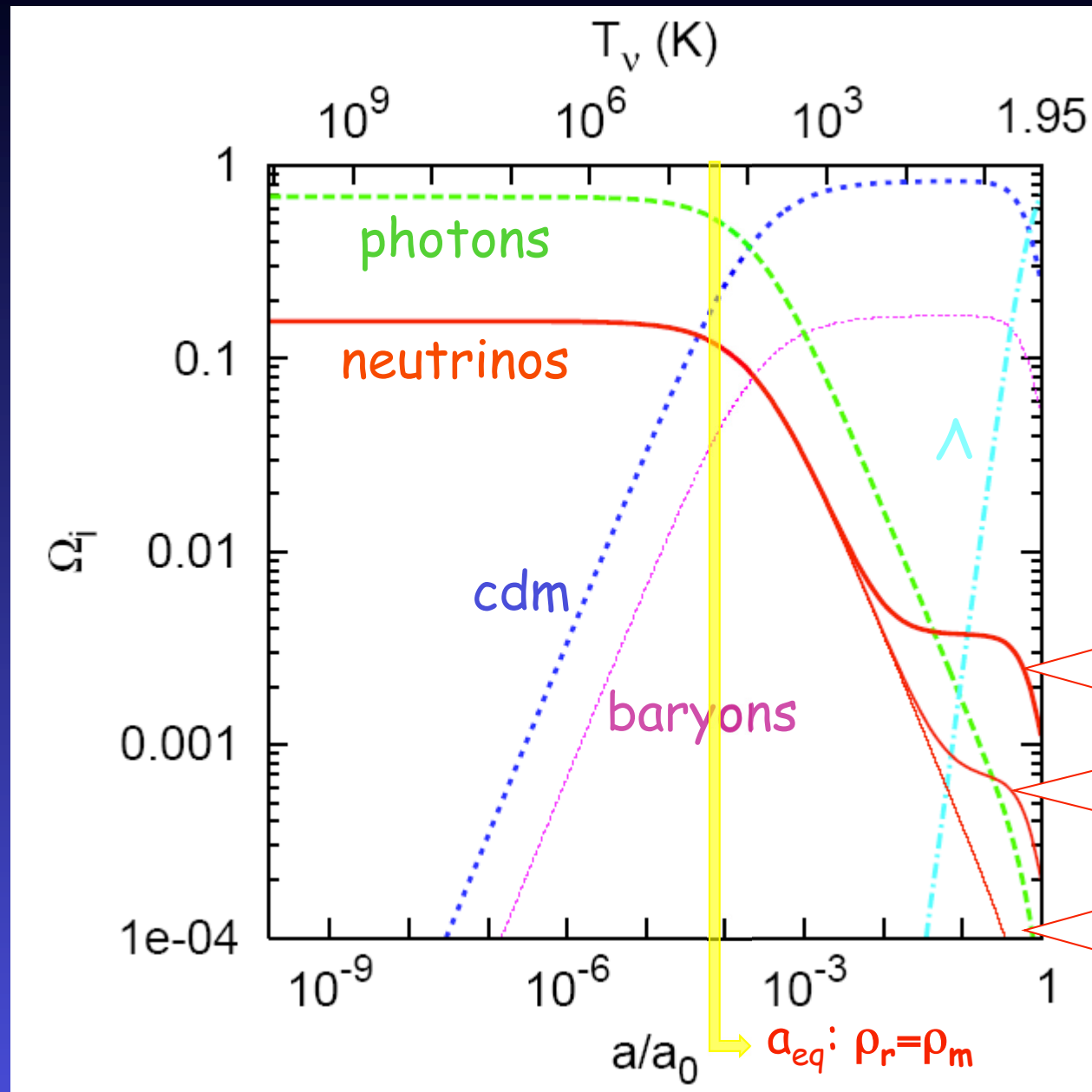
Contribution to the energy density of the Universe

$$\Omega_\nu h^2 \simeq 1.7 \times 10^{-5} \quad \text{Massless}$$

$$\Omega_\nu h^2 = \frac{\sum_i m_{\nu_i}}{94.1 \text{ eV}} \quad \begin{array}{l} \text{Massive} \\ m_\nu \gg T \end{array}$$



# Evolution of the background densities: 1 MeV $\rightarrow$ now



$$\Omega_i = \rho_i / \rho_{crit}$$

$$m_3 = 0.05 \text{ eV}$$

$$m_2 = 0.009 \text{ eV}$$

$$m_1 \approx 0 \text{ eV}$$

# The radiation content of the Universe ( $N_{\text{eff}}$ )



# Relativistic particles in the Universe

At  $T \gg m_e$ , the radiation content of the Universe is

$$\rho_r = \rho_\gamma + \rho_\nu = \frac{\pi^2}{15} T^4 + 3 \times \frac{7}{8} \times \frac{\pi^2}{15} T^4 = \left[ 1 + \frac{7}{8} \times 3 \right] \rho_\gamma$$

At  $T < m_e$ , the radiation content of the Universe is

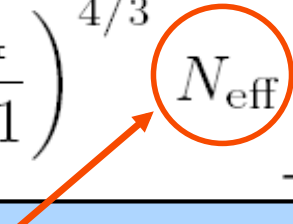
$$\rho_r = \rho_\gamma + \rho_\nu = \frac{\pi^2}{15} T_\gamma^4 + 3 \times \frac{7}{8} \times \frac{\pi^2}{15} T_\nu^4 = \left[ 1 + \frac{7}{8} \left( \frac{4}{11} \right)^{4/3} 3 \right] \rho_\gamma$$

$$\rho_r = \rho_\gamma + \rho_\nu = \left[ 1 + \frac{7}{8} \left( \frac{4}{11} \right)^{4/3} N_{\text{eff}} \right] \rho_\gamma$$

$\frac{T_\nu^4}{T_\gamma^4}$

# Relativistic particles in the Universe

At  $T \ll m_e$ , the radiation content of the Universe is

$$\rho_r = \rho_\gamma + \rho_\nu + \rho_x = \left[ 1 + \frac{7}{8} \left( \frac{4}{11} \right)^{4/3} N_{\text{eff}} \right] \rho_\gamma$$


**Effective number of relativistic neutrino species**

Traditional parametrization of the energy density stored in relativistic particles

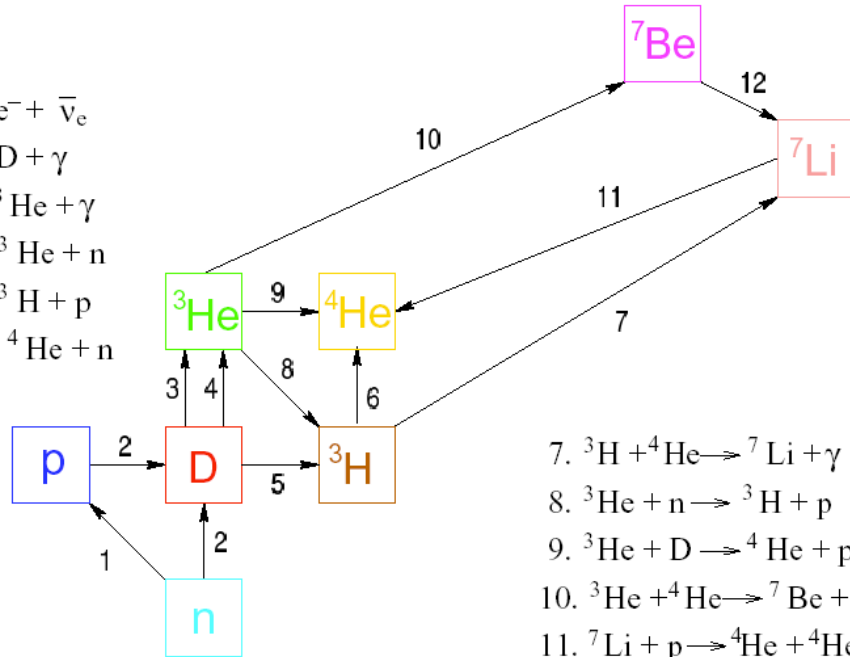
**# of flavour neutrinos:**  $N_\nu = 2.984 \pm 0.008$  (LEP data)

Constraints on  $N_{\text{eff}}$  from Primordial Nucleosynthesis and other cosmological observables (CMB+LSS)

# BBN: Creation of light elements

Produced elements: D,  $^3\text{He}$ ,  $^4\text{He}$ ,  $^7\text{Li}$  and small abundances of others

1.  $n \rightarrow p + e^- + \bar{\nu}_e$
2.  $p + n \rightarrow D + \gamma$
3.  $D + p \rightarrow ^3\text{He} + \gamma$
4.  $D + D \rightarrow ^3\text{He} + n$
5.  $D + D \rightarrow ^3\text{H} + p$
6.  $^3\text{H} + D \rightarrow ^4\text{He} + n$



7.  $^3\text{H} + ^4\text{He} \rightarrow ^7\text{Li} + \gamma$
8.  $^3\text{He} + n \rightarrow ^3\text{H} + p$
9.  $^3\text{He} + D \rightarrow ^4\text{He} + p$
10.  $^3\text{He} + ^4\text{He} \rightarrow ^7\text{Be} + \gamma$
11.  $^7\text{Li} + p \rightarrow ^4\text{He} + ^4\text{He}$
12.  $^7\text{Be} + n \rightarrow ^7\text{Li} + p$

Theoretical inputs:

- $\tau_n$ , the neutron lifetime;
- $G_N$ , the Newton gravitational constant;
- $\eta$ , the baryon to photon number density ratio;
- the nuclear rates.

The first two parameters are now known with a satisfactory accuracy

$$\tau_n = 885.7 \pm 0.8 \text{ s} ,$$

$$G_N = 6.7087 \pm 0.0010 \cdot 10^{-39} \text{ GeV}^{-2} .$$

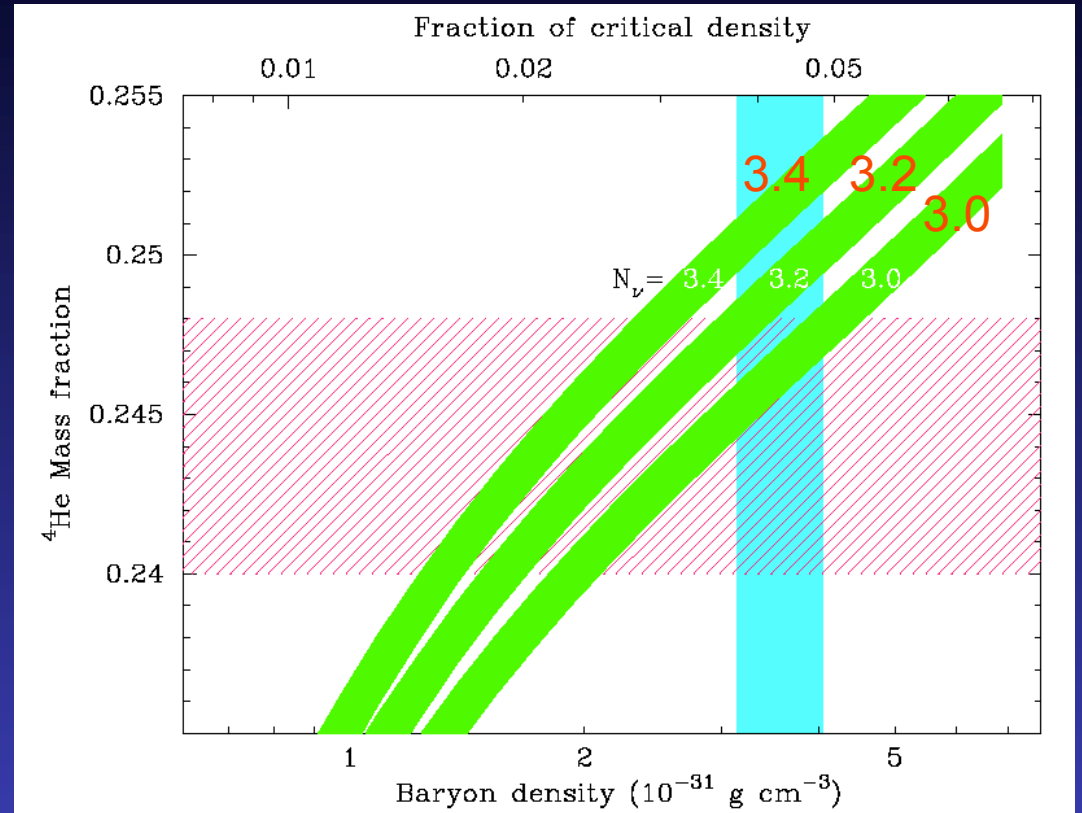
# Effect of neutrinos on BBN

## 1. $N_{\text{eff}}$ fixes the expansion rate during BBN

$$H = \sqrt{\frac{8\pi\rho}{3M_p^2}}$$

$$\rho(N_{\text{eff}}) > \rho_0 \rightarrow \uparrow {}^4\text{He}$$

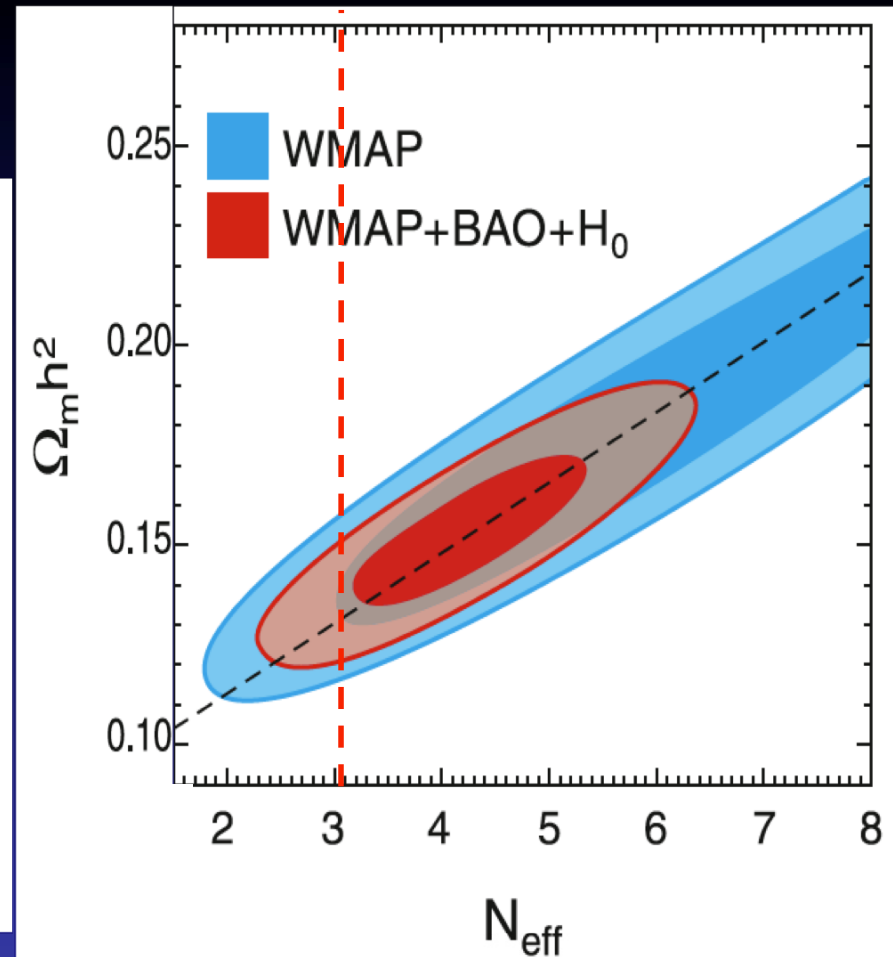
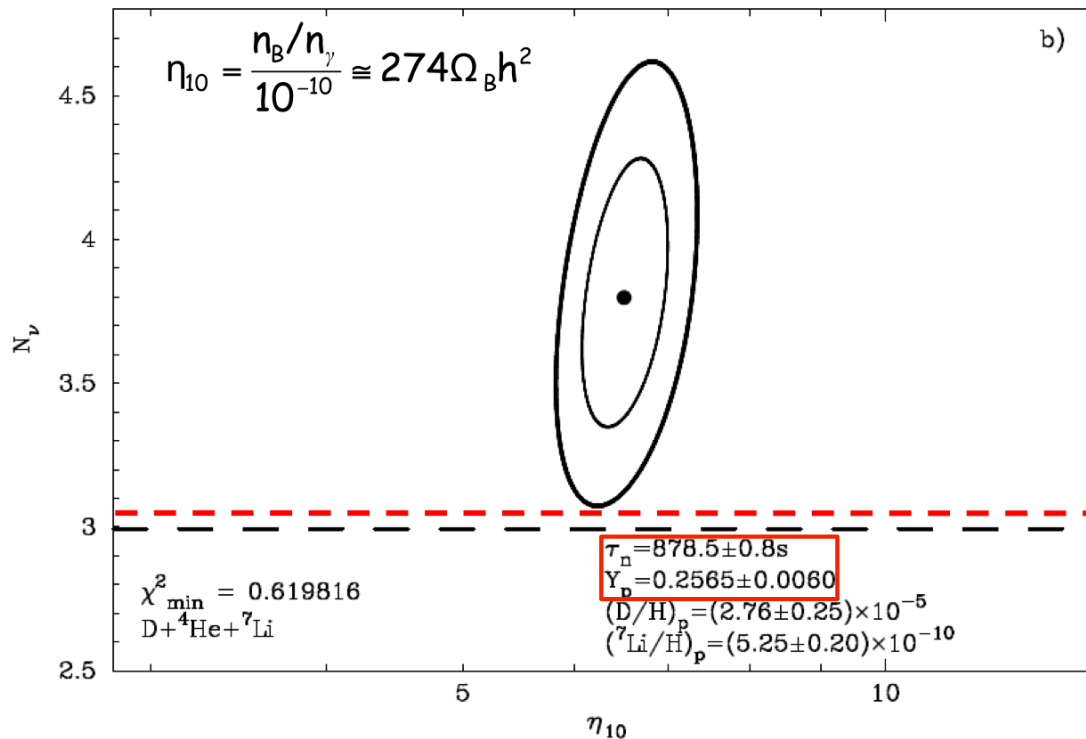
Burles, Nollett & Turner 1999



## 2. Direct effect of electron neutrinos and antineutrinos on the n-p reactions



# allowed ranges for $N_{\text{eff}}$



## Recent ${}^4\text{He}$ data

Izotov & Thuan, ApJ 710 (2010) L67

$$N_{\text{eff}} = 3.80^{+0.80}_{-0.70} \quad (95\% \text{ CL})$$

## from non-BBN data

WMAP [7-year], arXiv:1001.4538

$$2.7 < N_{\text{eff}} < 6.2 \quad (\text{WMAP+BAO+}H_0)$$

Larger errors: Aver et al, JCAP 05 (2010) 003

# Extra relativistic particles

- Extra radiation: **How to get  $N_{\text{eff}} > 3$ ?**

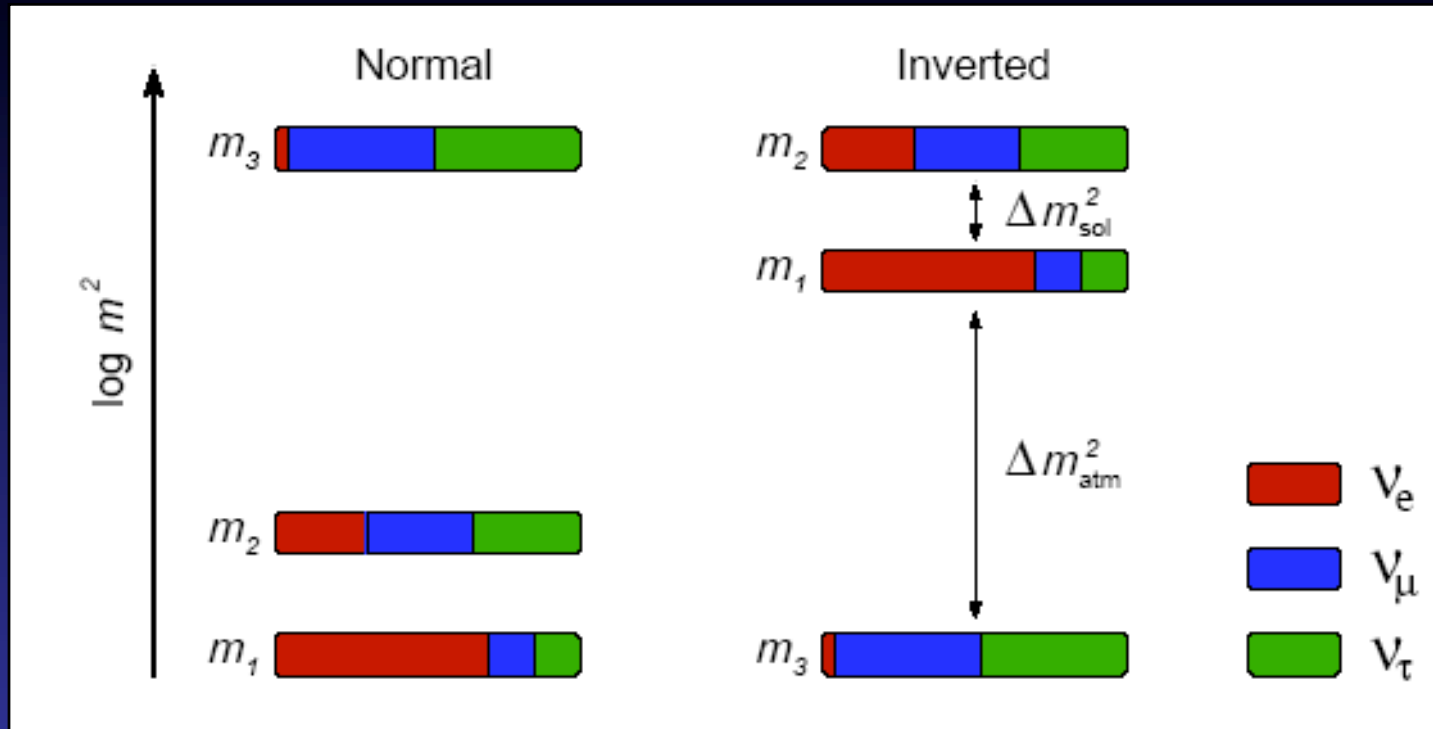
Neutrinos in non-standard scenarios: **NS Interactions, sterile neutrinos (totally or partially thermalized), relic neutrino asymmetries**

Other relativistic particles: **scalars, pseudoscalars, relativistic decay products of heavy particles...**



# Neutrinos as Dark Matter

# Neutrino masses



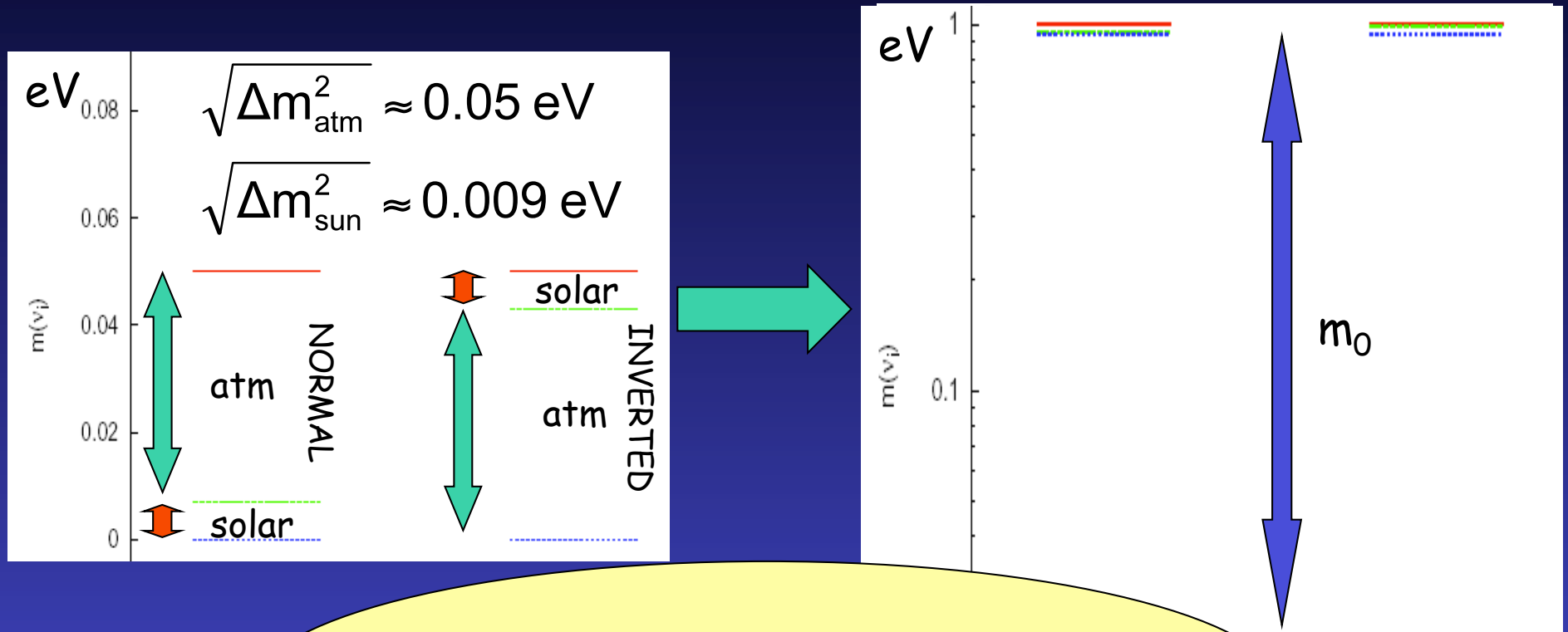
Possible neutrino mass hierarchy patterns

$$\nu_{\alpha L} = \sum_{i=1}^3 U_{\alpha i} \nu_{iL}, \quad (\alpha = e, \mu, \tau)$$

Present evidences  
for flavour neutrino  
oscillations: data on  
solar, atmospheric,  
reactor and accelerator  
neutrinos

# Neutrino masses

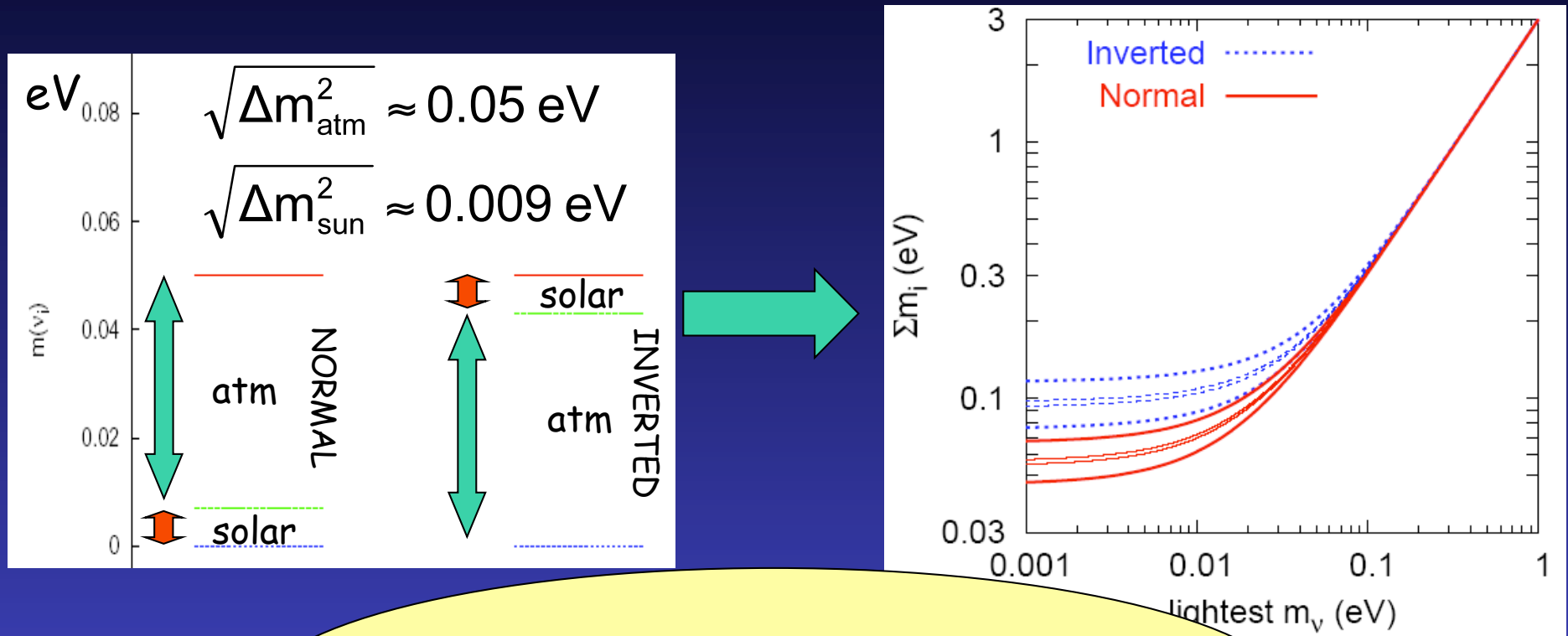
Data on flavour oscillations do not fix the absolute scale of neutrino masses



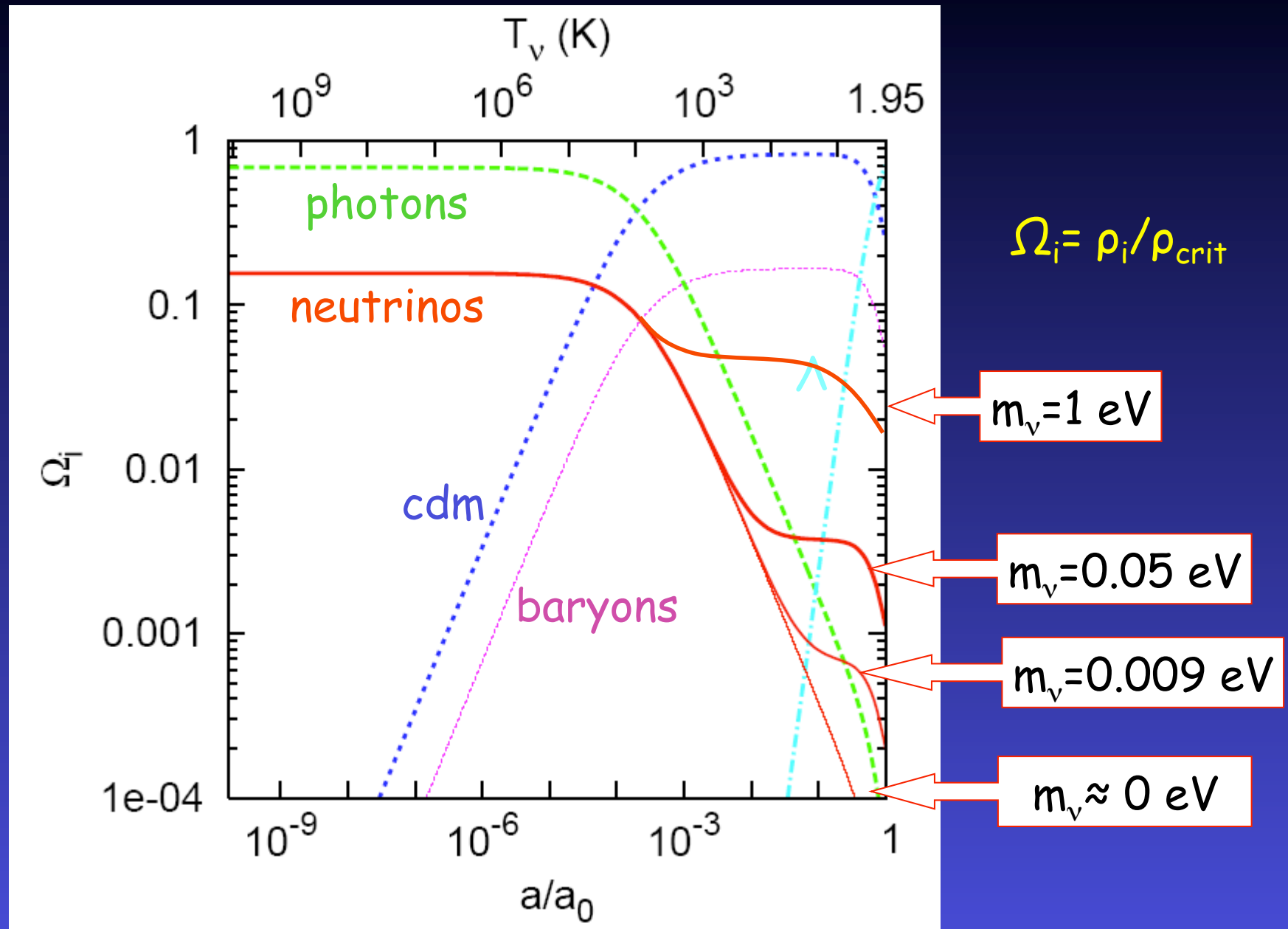
What is the value of  $m_0$  ?

# Neutrino masses

Data on flavour oscillations do not fix the absolute scale of neutrino masses



# Evolution of the background densities: 1 MeV $\rightarrow$ now



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Contribution to the energy density of the Universe

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$$\Omega_\nu h^2 = \frac{\sum_i m_{\nu_i}}{94.1 \text{ eV}} \quad \text{Massive } m_\nu \gg T$$

# Neutrinos as Dark Matter

- Neutrinos are natural **DM candidates**

$$\Omega_v h^2 = \frac{\sum_i m_i}{93.2 \text{ eV}} \quad \Omega_v < 1 \rightarrow \sum_i m_i < 46 \text{ eV}$$
$$\Omega_v < \Omega_m \approx 0.3 \rightarrow \sum_i m_i < 15 \text{ eV}$$

- They stream freely until non-relativistic (collisionless phase mixing)  **Neutrinos are HOT Dark Matter**
- First structures to be formed when Universe became matter-dominated are **very large**
- **Ruled out by structure formation**  **CDM**

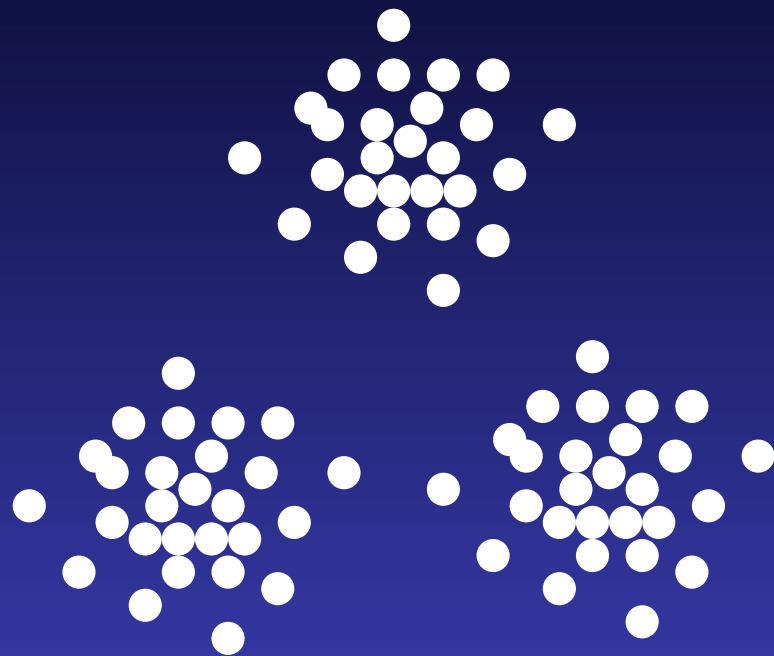


# Neutrinos as Hot Dark Matter

Massive Neutrinos can still be subdominant DM: limits on  $m_\nu$  from Structure Formation (combined with other cosmological data)

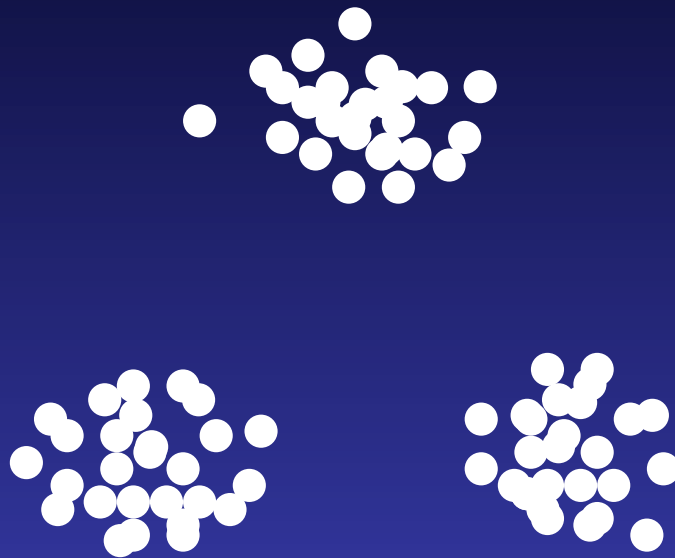
# Structure formation after equality

baryons and  
CDM (matter)  
experience  
gravitational  
clustering



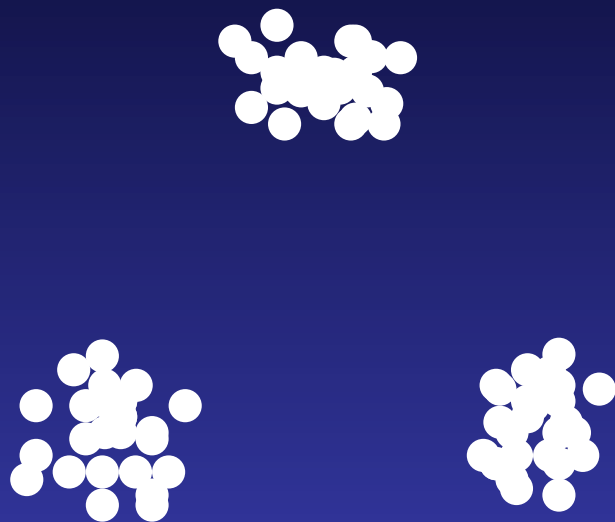
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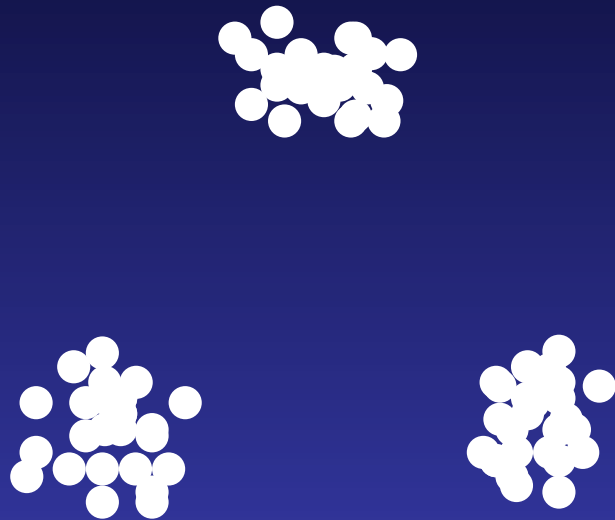
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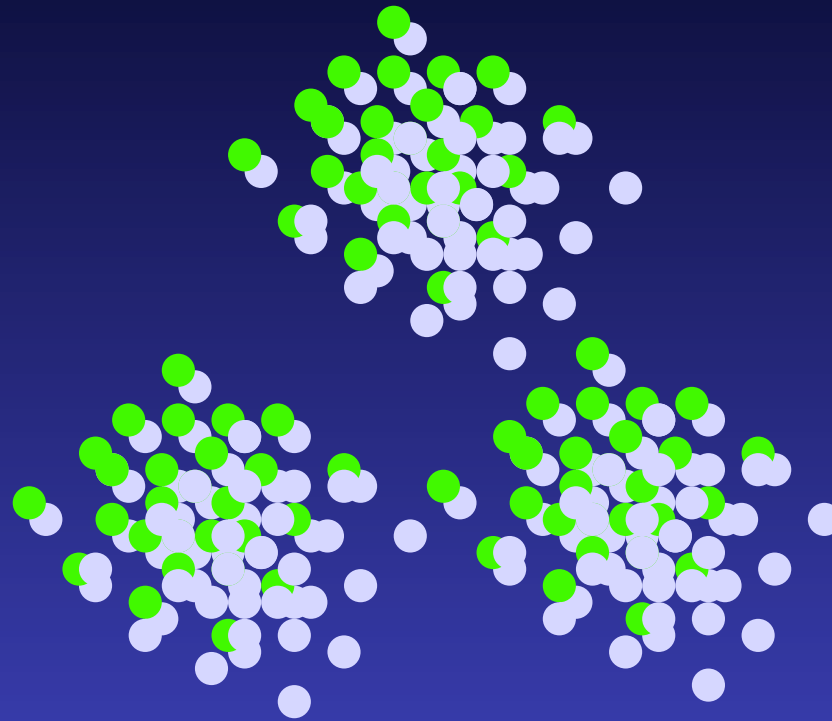


growth of  $\delta\rho/\rho(k,t)$  fixed by  
**gravity vs expansion** balance

$$\Rightarrow \delta\rho/\rho \propto a$$

# Structure formation after equality

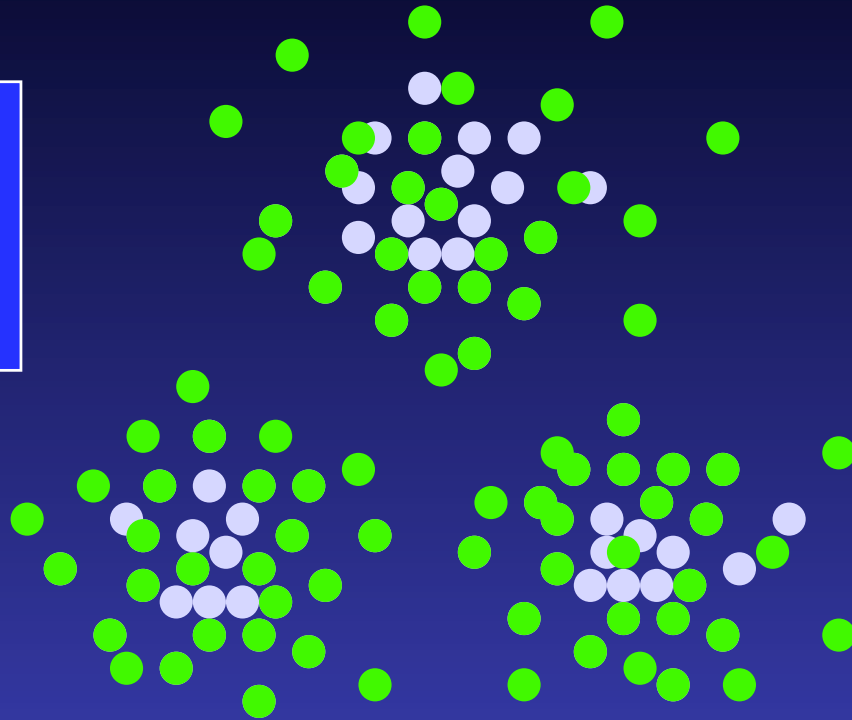
baryons and  
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neutrinos  
experience  
free-streaming  
with  
 $v = c$  or  $\langle p \rangle / m$

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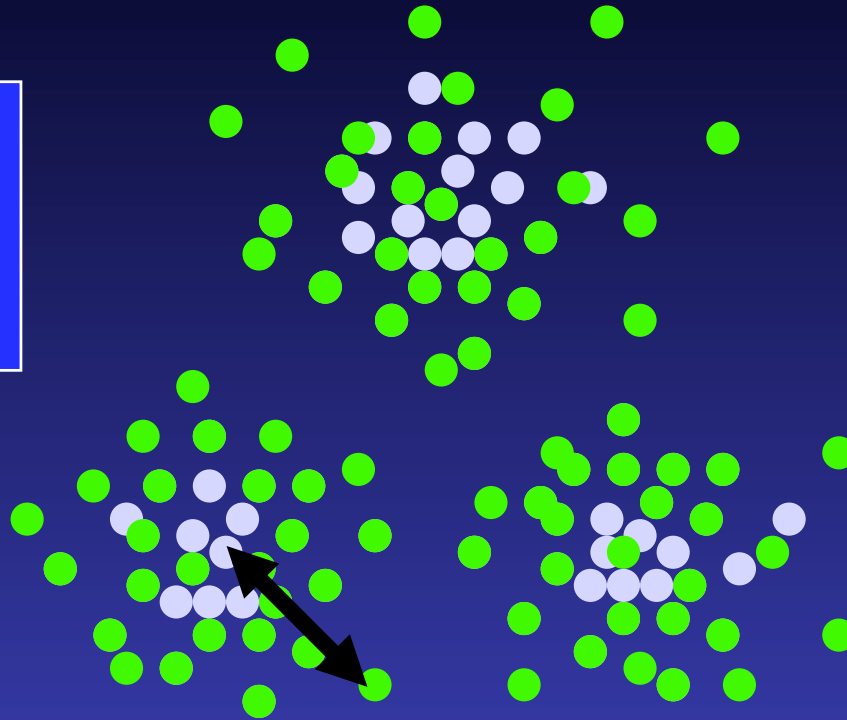


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# Structure formation after equality

baryons and  
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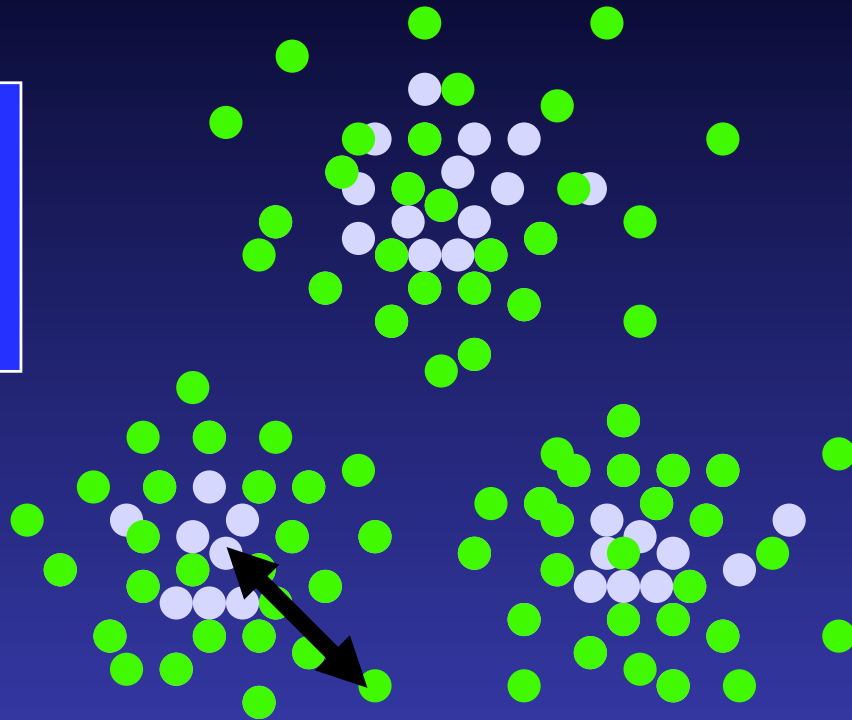
neutrinos cannot cluster below a diffusion length

$$\lambda = \int v dt < \int c dt$$



# Structure formation after equality

baryons and  
CDM (matter)  
experience  
gravitational  
clustering



neutrinos  
experience  
free-streaming  
with  
 $v = c$  or  $\langle p \rangle / m$

for  $(2\pi/k) < \lambda$  ,  
free-streaming suppresses growth of structures during MD

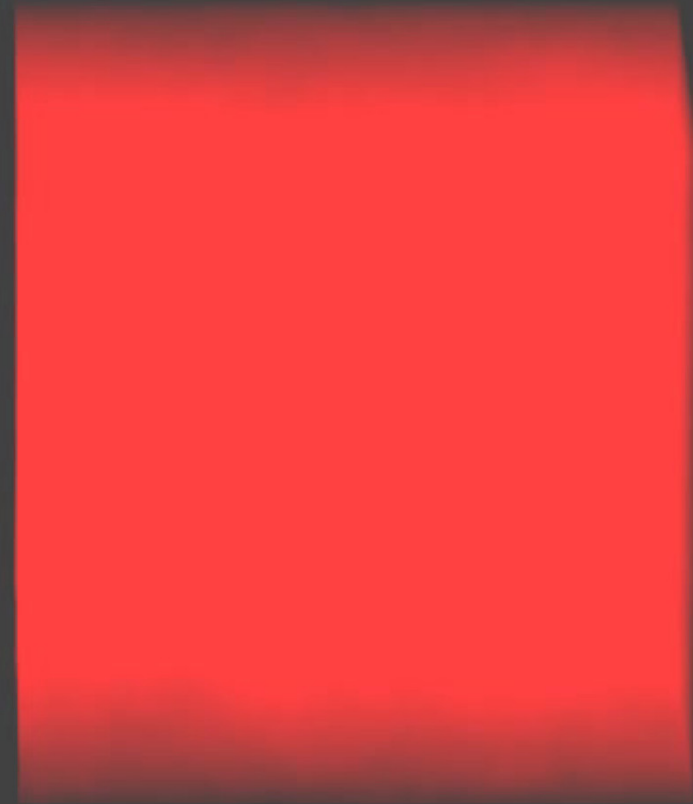
$$\Rightarrow \delta\rho/\rho \propto a^{1-3/5} f_v$$

$$\text{with } f_v = \rho_v/\rho_m \approx (\Sigma m_\nu)/(15 \text{ eV})$$

# Neutrinos as Hot Dark Matter

Massive Neutrinos can still be subdominant DM: limits on  $m_\nu$  from Structure Formation (combined with other cosmological data)

$Z=32.33$



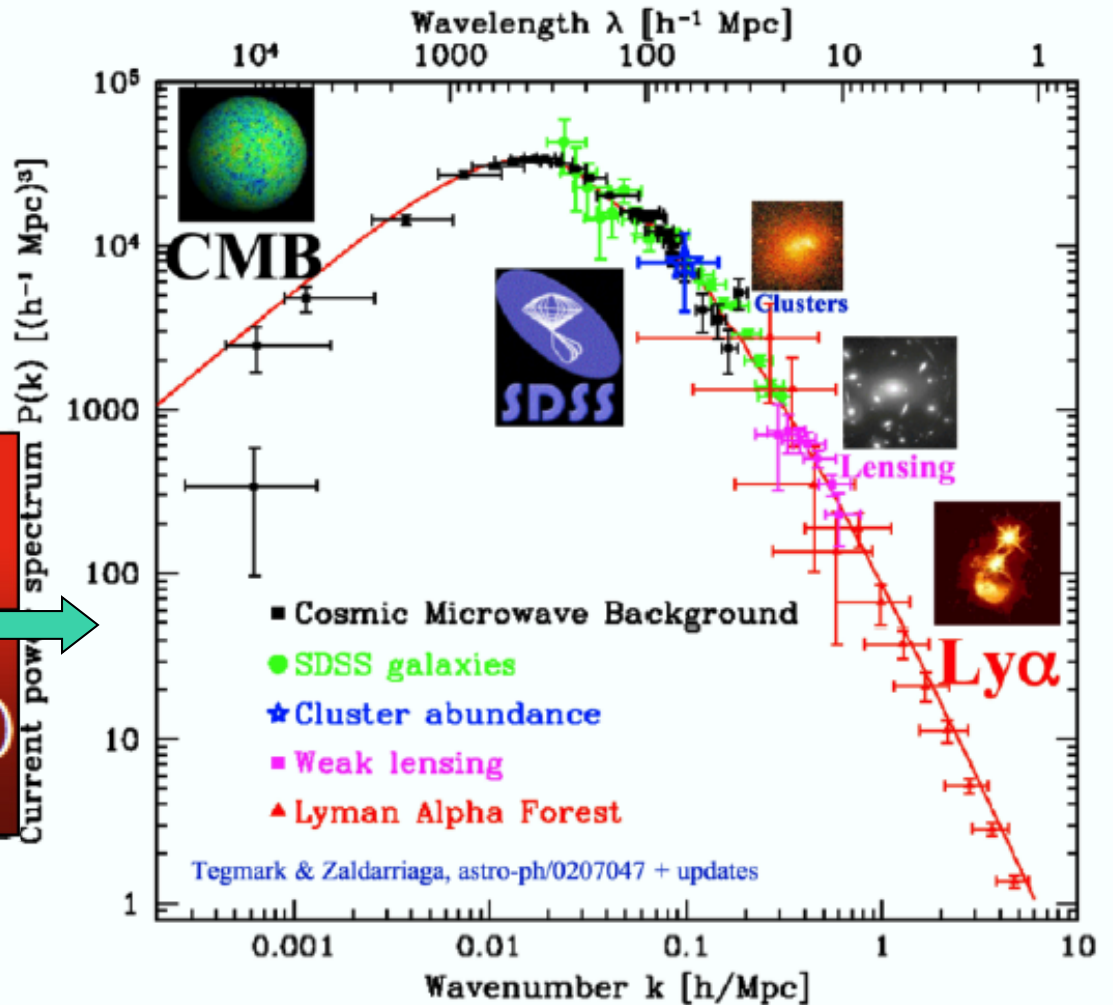
# Power Spectrum of density fluctuations

Field of density  
Fluctuations

$$\delta(x) = \frac{\delta\rho(x)}{\bar{\rho}}$$

Matter power spectrum is  
the Fourier transform of the  
two-point correlation function

$$\langle \delta(x_1)\delta(x_2) \rangle = \int \frac{d^3k}{(2\pi)^3} e^{ik(x_2-x_1)} P(k)$$



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TAUP 2003  
September 5, 2003

# Neutrinos as Hot Dark Matter: effect on $P(k)$

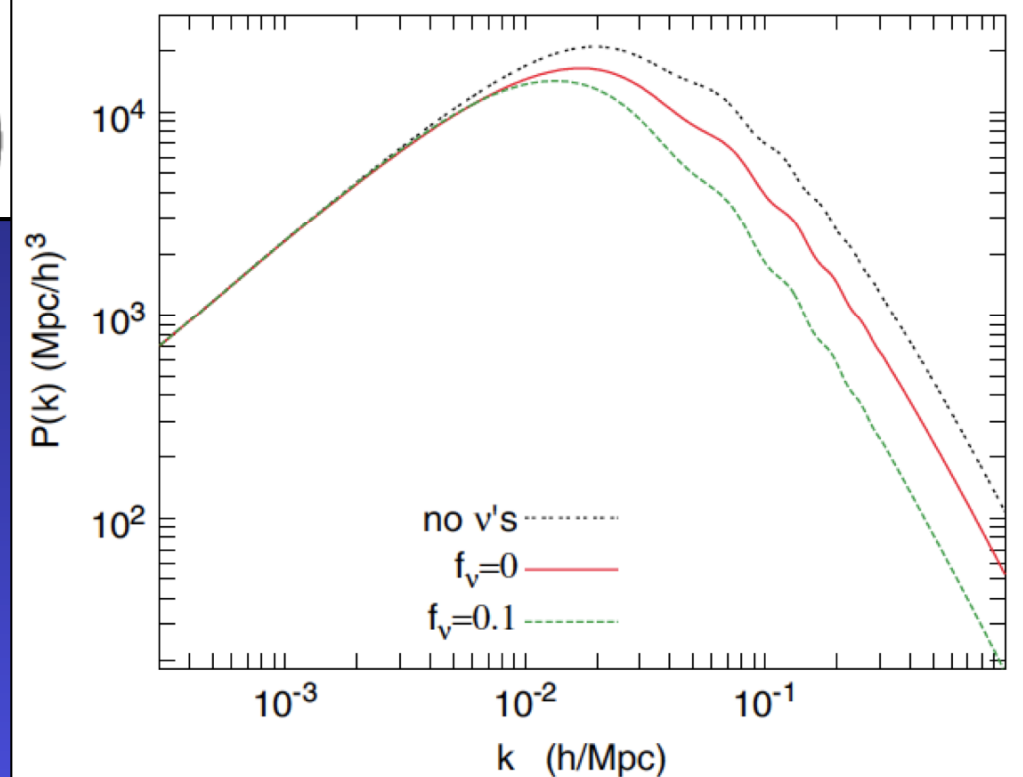
Massive Neutrinos can still be subdominant DM: **limits on  $m_\nu$  from Structure Formation (combined with other cosmological data)**

- Effect of Massive Neutrinos: **suppression of Power at small scales**

The small-scale suppression is given by

$$\left(\frac{\Delta P}{P}\right) \approx -8 \frac{\Omega_\nu}{\Omega_m} \approx -0.8 \left(\frac{m_\nu}{1 \text{ eV}}\right) \left(\frac{0.1 N}{\Omega_m h^2}\right)$$

$f_\nu$

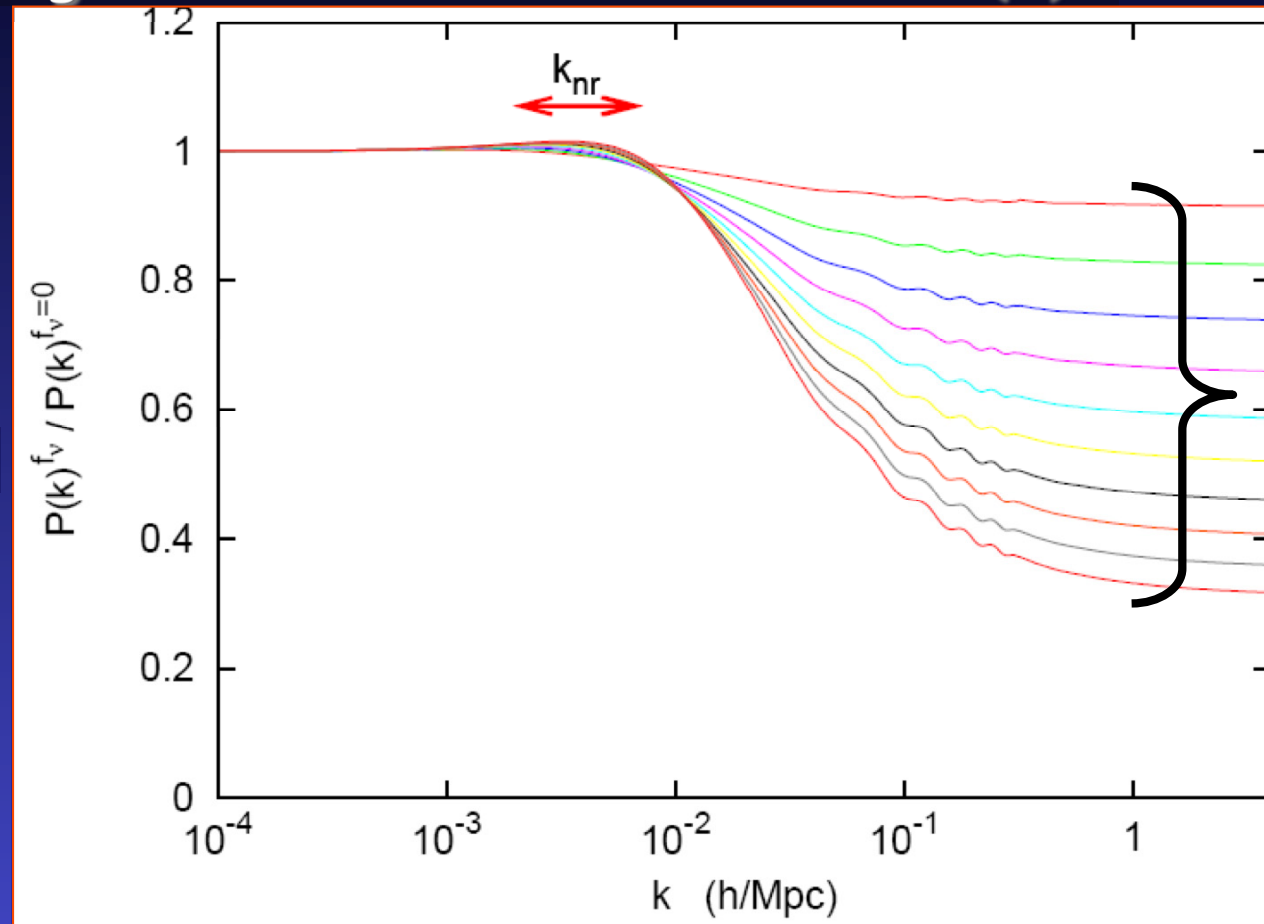


# Effect of massive neutrinos on $P(k)$

Observable signature of the total mass on  $P(k)$  :

$P(k)$  massive

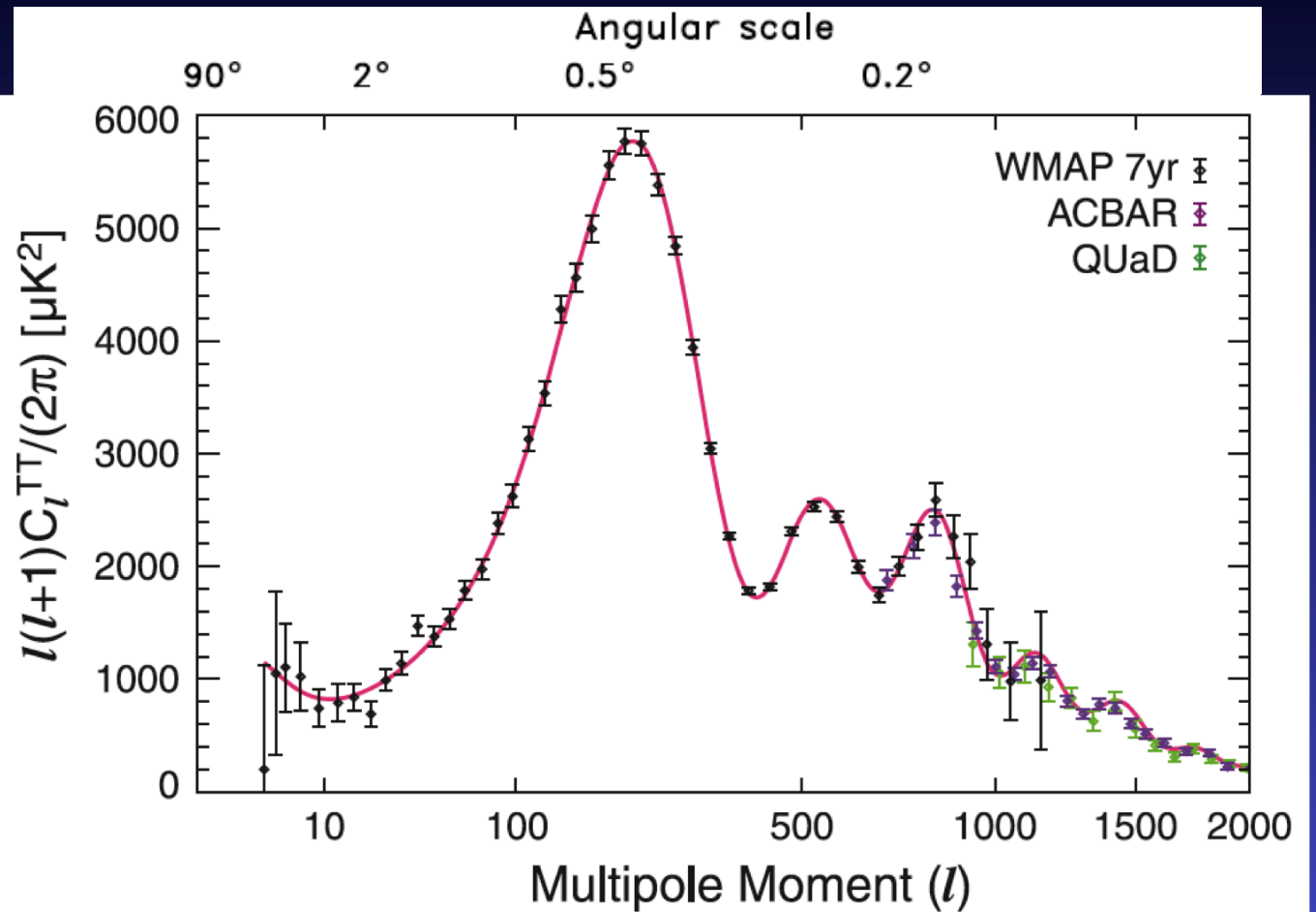
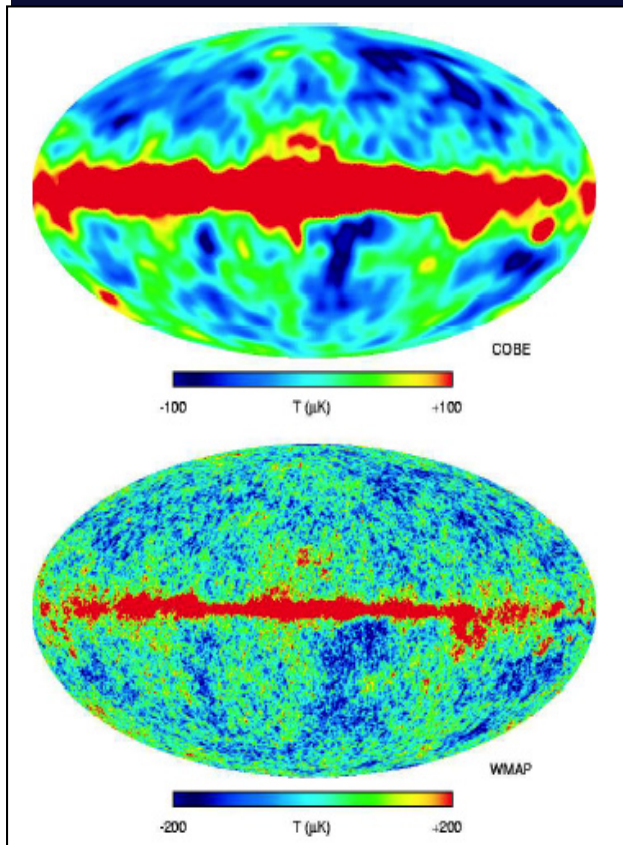
$P(k)$  massless



various  
 $f_v$

Lesgourgues & SP, Phys. Rep. 429 (2006) 307

# CMB TT DATA



# Effect of massive neutrinos on the CMB spectra

- 1) CMB spectrum essentially unchanged if neutrinos become NR **AFTER** photon decoupling ( $z_{\text{rec}} \sim 1089$ )

$$\begin{aligned} 1 + z_{\text{nr}} &= \frac{T_{\nu, \text{nr}}}{T_{\nu, 0}} \\ &= 1.99 \times 10^3 (m_\nu / \text{eV}) \\ &= 6.24 \times 10^4 \omega_\nu, \end{aligned}$$

Neutrinos become NR **BEFORE** recombination if:

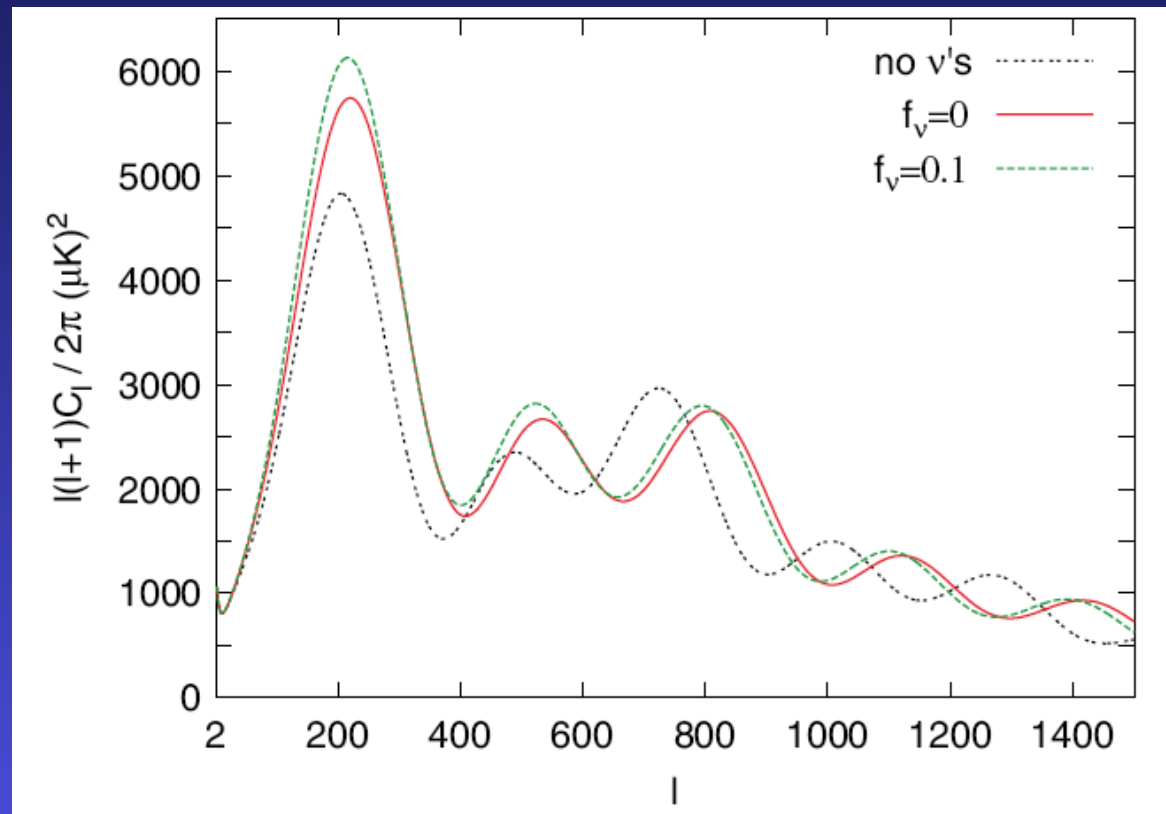
$$\omega_\nu \geq 0.017 \quad \Rightarrow \quad \sum_i m_i \geq 1.6 \text{ eV}$$

More details including effects of neutrino mass on “reduced CMB observables” in **Ichikawa et al, PRD 71 (2005) 043001**

# Effect of massive neutrinos on the CMB spectra

- 1) CMB spectrum essentially unchanged if neutrinos become NR **AFTER** photon decoupling.
- 2) Impact on CMB spectra is indirect: **non-zero**  $\Omega_\nu$  modifies the **background evolution** (change in **equality** time)

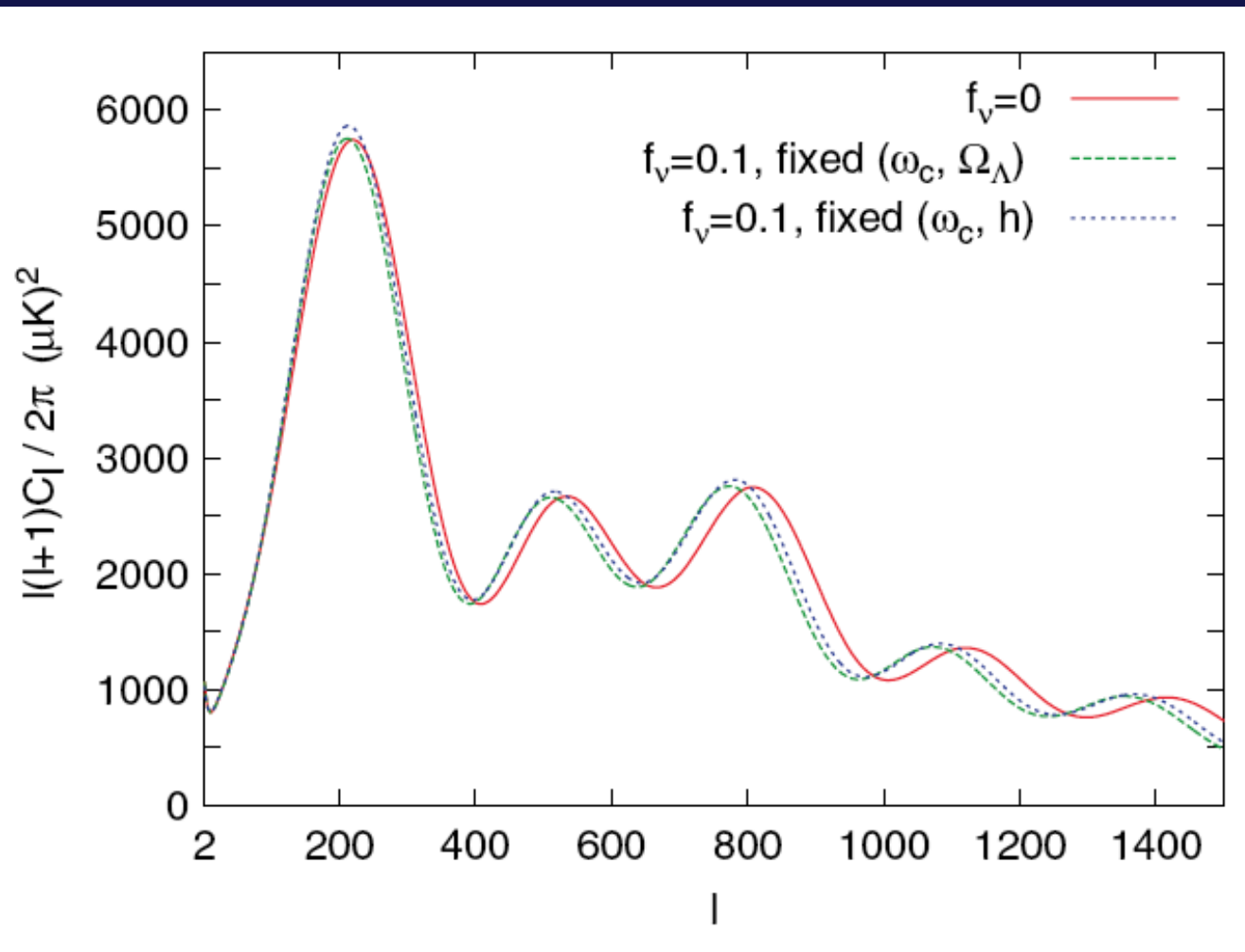
**Ex:** in a flat universe,  
keep  $\Omega_\Lambda + \Omega_{\text{cdm}} + \Omega_b + \Omega_\nu = 1$   
constant





# Effect of massive neutrinos on the CMB spectra

Problem with **parameter degeneracies**: change in other cosmological parameters can mimic the effect of  $\nu$  masses



Cosmological bounds on  $\Sigma m_\nu$

# Cosmological bounds on neutrino mass(es)

A unique cosmological bound on  $m_\nu$  DOES NOT exist !

Different analyses have found upper bounds on neutrino masses, since they depend on

- The combination of cosmological data used
- The assumed cosmological model: number of parameters (problem of parameter degeneracies)
- The properties of relic neutrinos

# Cosmological Data

- CMB **Temperature**: WMAP plus data from other experiments at large multipoles (CBI, ACBAR, VSA...)
- CMB **Polarization**: WMAP, ...
- Large Scale Structure:
  - \* **Galaxy Clustering** (2dF, SDSS)
  - \* **Bias (Galaxy, ...)**: Amplitude of the Matter  $P(k)$  (SDSS,  $\sigma_8$ )
  - \* **Lyman- $\alpha$  forest**: independent measurement of power on small scales
  - \* **Baryon acoustic oscillations** (SDSS)

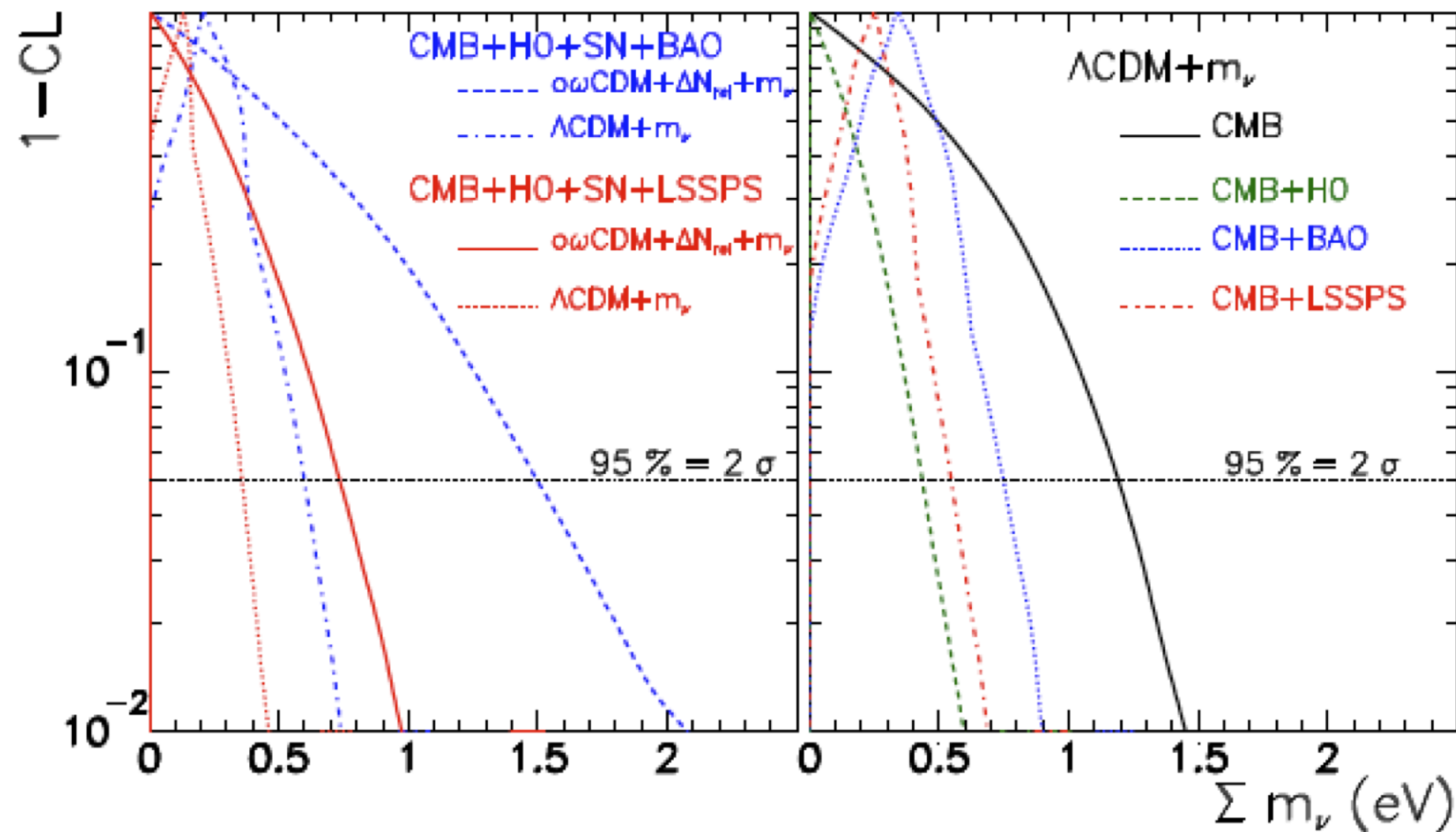
Bounds on parameters from other data: **SNIa** ( $\Omega_m$ ), **HST** ( $h$ ), ...

# Cosmological Parameters: example

| Parameter        | Meaning                       | Status         |
|------------------|-------------------------------|----------------|
| $\tau$           | Reionization optical depth    | Not optional   |
| $\omega_b$       | Baryon density                | Not optional   |
| $\omega_d$       | Dark matter density           | Not optional   |
| $f_\nu$          | Dark matter neutrino fraction | Well motivated |
| $\Omega_\Lambda$ | Dark energy density           | Not optional   |
| $w$              | Dark energy equation of state | Worth testing  |
| $\Omega_k$       | Spatial curvature             | Worth testing  |
| $A_s$            | Scalar fluctuation amplitude  | Not optional   |
| $n_s$            | Scalar spectral index         | Well motivated |
| $\alpha$         | Running of spectral index     | Worth testing  |
| $r$              | Tensor-to-scalar ratio        | Well motivated |
| $n_t$            | Tensor spectral index         | Well motivated |
| $b$              | Galaxy bias factor            | Not optional   |

SDSS Coll, PRD 69 (2004) 103501

# Current cosmological bounds on neutrino masses



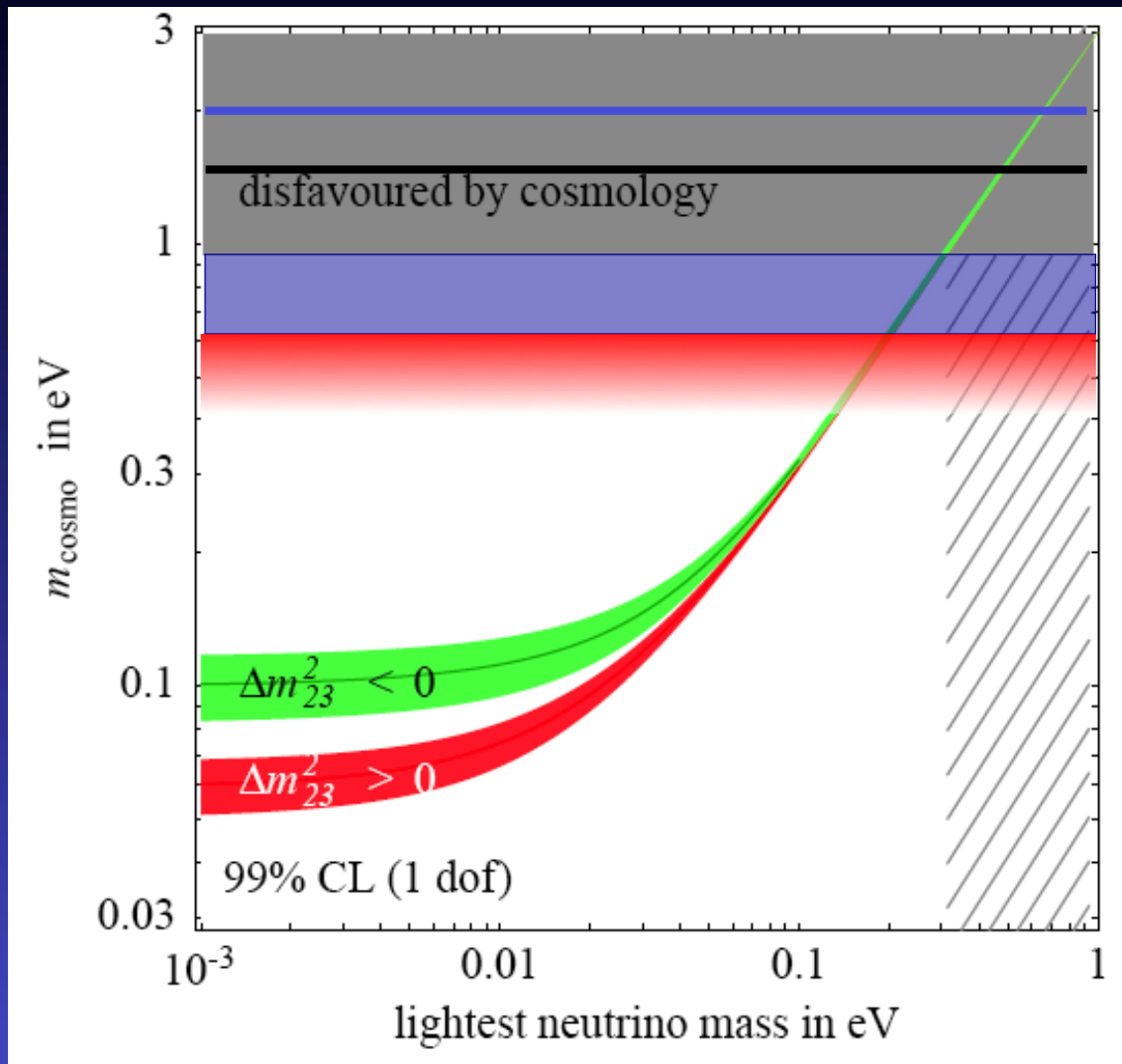
González-García et al., JCAP 08 (2010) 117

# Current cosmological bounds on neutrino masses

|                           | CMB+HO+SN+BAO |                      |                                            | CMB+HO+SN+LSS-PS |                      |                                            |
|---------------------------|---------------|----------------------|--------------------------------------------|------------------|----------------------|--------------------------------------------|
|                           | best          | $1\sigma$            | 95% CL                                     | best             | $1\sigma$            | 95% CL                                     |
| $H_0$ km/s/Mpc            | 76.2          | $+3.0$<br>$-2.8$     | $+5.7$<br>$-5.6$                           | 74.4             | $+2.8$<br>$-2.9$     | $+5.6$<br>$-5.6$                           |
| $\Omega_b h^2 \times 100$ | 2.205         | $+0.057$<br>$-0.050$ | $+0.103$<br>$-0.105$                       | 2.239            | $+0.059$<br>$-0.046$ | $+0.095$<br>$-0.108$                       |
| $\Omega_c h^2$            | 0.131         | $+0.018$<br>$-0.013$ | $+0.036$<br>$-0.023$                       | 0.128            | $+0.024$<br>$-0.009$ | $+0.042$<br>$-0.018$                       |
| $n_S$                     | 0.961         | $+0.021$<br>$-0.015$ | $+0.040$<br>$-0.030$                       | 0.971            | $+0.019$<br>$-0.017$ | $+0.037$<br>$-0.033$                       |
| $\tau$                    | 0.086         | $+0.011$<br>$-0.015$ | $+0.026$<br>$-0.028$                       | 0.083            | $+0.016$<br>$-0.011$ | $+0.030$<br>$-0.023$                       |
| $\sigma_8$                | 0.787         | $+0.091$<br>$-0.073$ | $+0.135$<br>$-0.179$                       | 0.824            | $+0.051$<br>$-0.048$ | $+0.097$<br>$-0.105$                       |
| $\Omega_k$                | -0.006        | $+0.010$<br>$-0.009$ | $-0.022 \leq \Omega_k \leq 0.016$          | -0.011           | $+0.008$<br>$-0.009$ | $-0.028 \leq \Omega_k \leq 0.007$          |
| $\omega$                  | -1.17         | $+0.19$<br>$-0.21$   | $-0.62 \leq \omega + 1 \leq 0.18$          | -1.12            | $+0.21$<br>$-0.20$   | $-0.57 \leq \omega + 1 \leq 0.26$          |
| $\Delta N_{\text{rel}}$   | 1.2           | $+1.1$<br>$-0.61$    | $0.08 \leq \Delta N_{\text{rel}} \leq 3.2$ | 1.3              | $+1.4$<br>$-0.54$    | $0.21 \leq \Delta N_{\text{rel}} \leq 3.6$ |
| $\sum m_\nu$ (eV)         |               | $\leq 0.77$          | $\leq 1.5$                                 |                  | $\leq 0.37$          | $\leq 0.76$                                |

González-García et al., JCAP 08 (2010) 117

# Neutrino masses in 3-neutrino schemes



CMB

CMB + galaxy clustering

+ HST, SNI-a...

+ **BAO** and/or bias



## Current cosmological bounds on neutrino masses

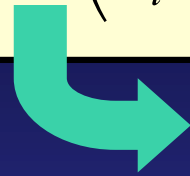
Dependence on the data set AND the cosmological model used.

| Model                                               | Observables     | $\Sigma m_\nu$ (eV) 95% Bound |
|-----------------------------------------------------|-----------------|-------------------------------|
| $o\omega\text{CDM} + \Delta N_{\text{rel}} + m_\nu$ | CMB+H0+SN+BAO   | $\leq 1.5$                    |
| $o\omega\text{CDM} + \Delta N_{\text{rel}} + m_\nu$ | CMB+H0+SN+LSSPS | $\leq 0.76$                   |
| $\Lambda\text{CDM} + m_\nu$                         | CMB+H0+SN+BAO   | $\leq 0.61$                   |
| $\Lambda\text{CDM} + m_\nu$                         | CMB+H0+SN+LSSPS | $\leq 0.36$                   |
| $\Lambda\text{CDM} + m_\nu$                         | CMB (+SN)       | $\leq 1.2$                    |
| $\Lambda\text{CDM} + m_\nu$                         | CMB+BAO         | $\leq 0.75$                   |
| $\Lambda\text{CDM} + m_\nu$                         | CMB+LSSPS       | $\leq 0.55$                   |
| $\Lambda\text{CDM} + m_\nu$                         | CMB+H0          | $\leq 0.45$                   |

González-García et al., JCAP 08 (2010) 117

# Absolute mass scale searches

|                          |                                                            |        |
|--------------------------|------------------------------------------------------------|--------|
| Tritium $\beta$<br>decay | $m_{\nu_e} = \left( \sum_i  U_{ei} ^2 m_i^2 \right)^{1/2}$ | 2.2 eV |
|--------------------------|------------------------------------------------------------|--------|



$$[c_{13}^2 c_{12}^2 m_1^2 + c_{13}^2 s_{12}^2 m_2^2 + s_{13}^2 m_3^2]^{1/2}$$

|                                      |                                               |              |
|--------------------------------------|-----------------------------------------------|--------------|
| Neutrinoless<br>double beta<br>decay | $m_{ee} = \left  \sum_i U_{ei}^2 m_i \right $ | < 0.2-0.8 eV |
|--------------------------------------|-----------------------------------------------|--------------|



$$|c_{13}^2 c_{12}^2 m_1 + c_{13}^2 s_{12}^2 m_2 e^{i\phi_2} + s_{13}^2 m_3 e^{i\phi_3}|$$

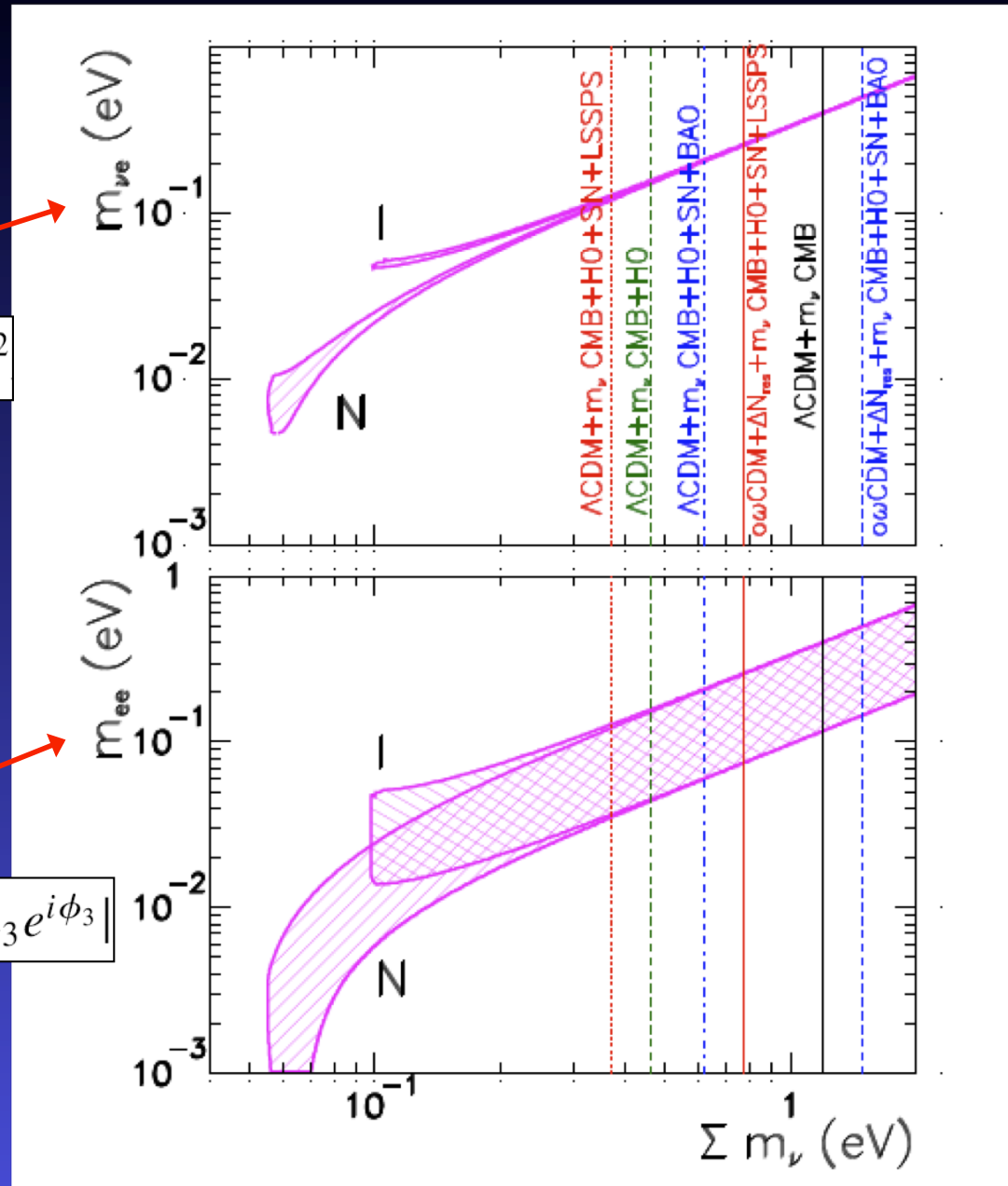
|           |                   |              |
|-----------|-------------------|--------------|
| Cosmology | $\sim \sum_i m_i$ | < 0.2-2.0 eV |
|-----------|-------------------|--------------|

# Tritium $\beta$ decay, $0\nu 2\beta$ and Cosmology

$$[c_{13}^2 c_{12}^2 m_1^2 + c_{13}^2 s_{12}^2 m_2^2 + s_{13}^2 m_3^2]^{1/2}$$

$$|c_{13}^2 c_{12}^2 m_1 + c_{13}^2 s_{12}^2 m_2 e^{i\phi_2} + s_{13}^2 m_3 e^{i\phi_3}|$$

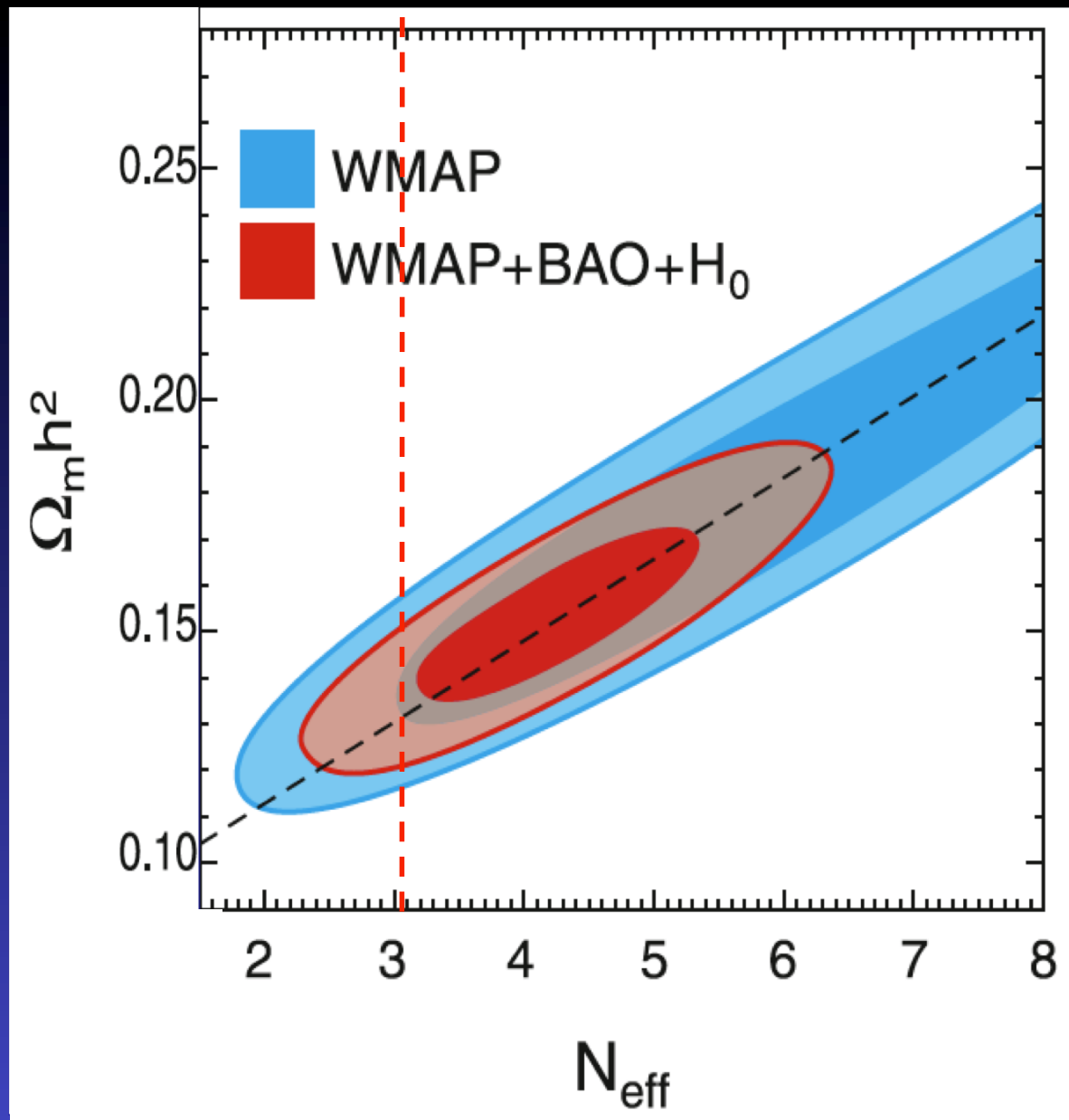
González-García et al.,  
JCAP 08 (2010) 117



Future sensitivities on  $m_\nu$  and  
 $N_{\text{eff}}$  from cosmology

allowed range  
for  $N_{\text{eff}}$

WMAP [7-year], arXiv:1001.4538



$$2.7 < N_{\text{eff}} < 6.2 \text{ (WMAP+BAO+} H_0 \text{)}$$

# Future bounds on $N_{\text{eff}}$

Forecast analysis:  
Bowen et al,  
MNRAS 334 (2002) 760



$$\sigma[N_{\text{eff}}] \sim 3 \text{ (WMAP)}$$

$$\sigma[N_{\text{eff}}] \sim 0.2 \text{ (Planck)}$$

ERROR FORECASTS

| Experiment   | $f_{\text{sky}}$ | $\theta_b$ | $w_T^{-1/2}$<br>[ $\mu$ K'] | $w_P^{-1/2}$<br>[ $\mu$ K'] | $\Delta N_\nu$<br>TT | $\Delta N_\nu$<br>TT+TE+EE | $\Delta N_\nu$ (free Y)<br>TT+TE+EE |
|--------------|------------------|------------|-----------------------------|-----------------------------|----------------------|----------------------------|-------------------------------------|
| Planck       | 0.8              | 7'         | 40                          | 56                          | 0.6                  | 0.20                       | 0.24                                |
| ACT          | 0.01             | 1.7'       | 3                           | 4                           | 1                    | 0.47                       | 0.9                                 |
| ACT + Planck |                  |            |                             |                             | 0.4                  | 0.18                       | 0.24                                |
| CMBPOL       | 0.8              | 4'         | 1                           | 1.4                         | 0.12                 | 0.05                       | 0.09                                |

Example of future  
CMB satellite

Bashinsky & Seljak, PRD 69 (2004) 083002

# Future bounds on $N_{\text{eff}}$

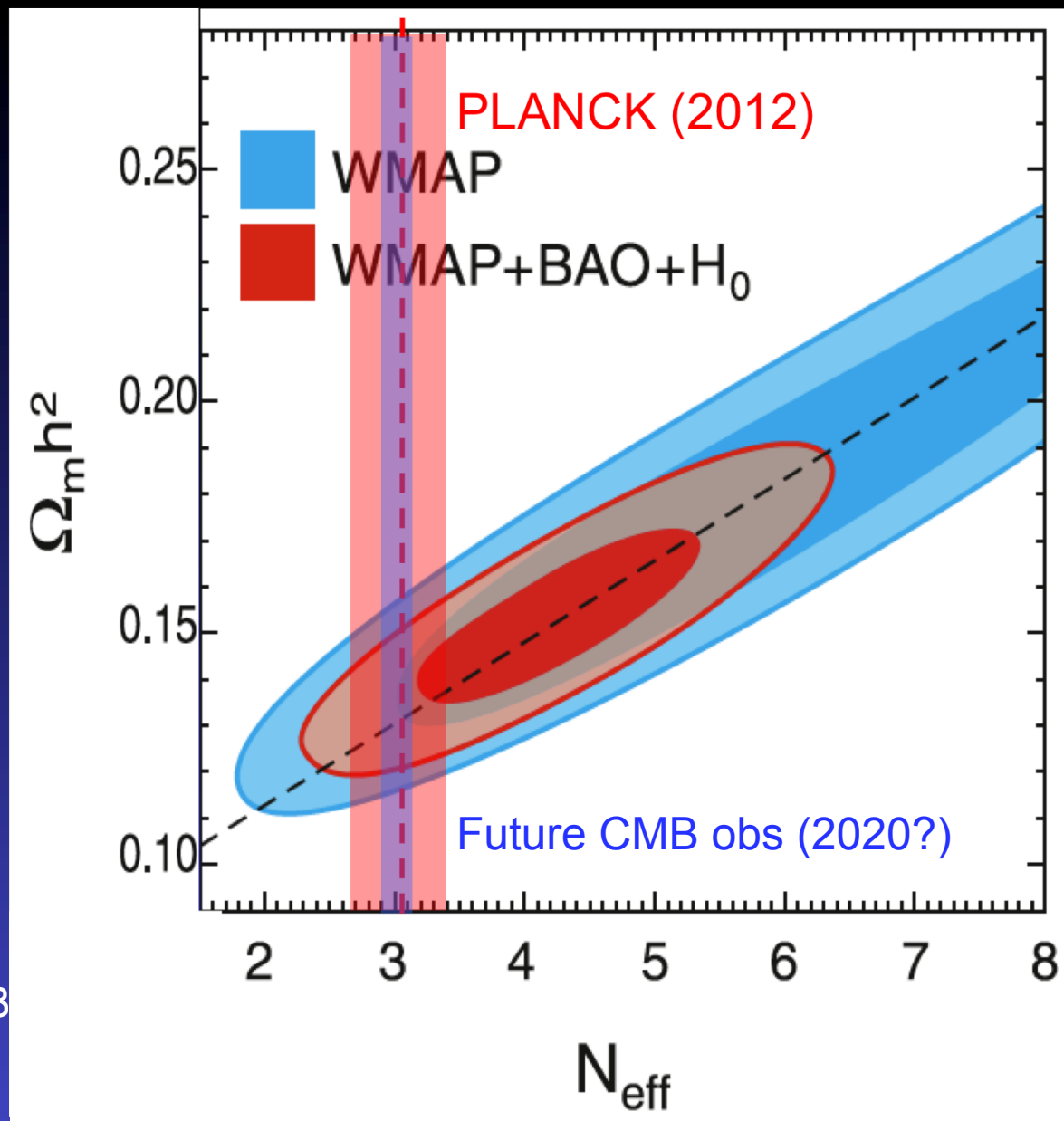
|                      | Planck | P+BAO | P+HPS | P+HST | P+HST+BAO | P+HST+HPS |
|----------------------|--------|-------|-------|-------|-----------|-----------|
| $\omega_{\text{dm}}$ | 0.22   | 0.24  | 0.20  | 0.21  | 0.21      | 0.19      |
| $N_{\text{eff}}$     | 0.21   | 0.21  | 0.22  | 0.21  | 0.21      | 0.22      |
| $\sum m_\nu$         | 0.68   | 0.81  | 0.44  | 0.67  | 0.73      | 0.44      |
| $w$                  | 2.14   | 1.16  | 0.72  | 0.74  | 0.76      | 0.55      |
| $n_s$                | 0.46   | 0.48  | 0.49  | 0.46  | 0.48      | 0.48      |

**Table 3:** Projected sensitivity of Planck data (P) combined with LSS data to selected parameters of the **vanilla+ $f_\nu$ + $N_{\text{eff}}$ + $w$  model**. Given are the standard deviations of the marginalised posteriors, normalised to the values obtained with current CMB+HST+HPS data. Note that just like for current CMB data, the addition of BAO data shifts the posterior towards larger neutrino masses, resulting in a two-tailed pdf with a correspondingly larger standard deviation – this does not mean that the constraining power of Planck+BAO is worse than that of Planck alone. The marginalised posteriors of all the other parameters are very close to two-tailed Gaussians, and do not suffer from this effect.

Hamann et al, JCAP 07 (2010) 022

allowed range  
for  $N_{\text{eff}}$

WMAP [7-year], arXiv:1001.4538

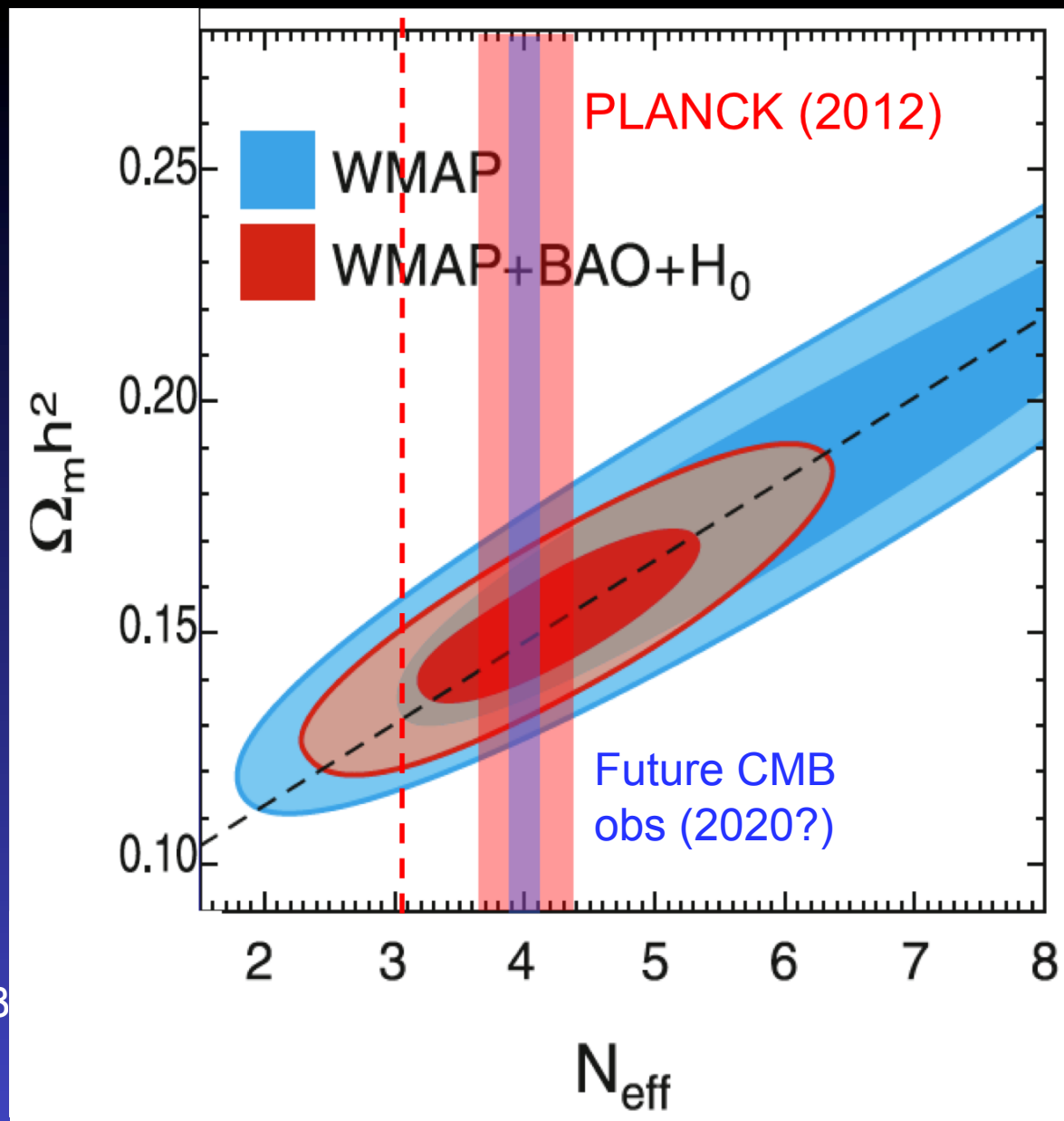


$$2.7 < N_{\text{eff}} < 6.2 \text{ (WMAP+BAO+} H_0 \text{)}$$



allowed range  
for  $N_{\text{eff}}$

WMAP [7-year], arXiv:1001.4538



$$2.7 < N_{\text{eff}} < 6.2 \text{ (WMAP+BAO+H}_0\text{)}$$

# Future sensitivities on $\Sigma m_\nu$

Future cosmological data will be available from

- o **CMB (Temperature & Polarization anis.)**
- o **High-z Galaxy redshift surveys**

Hannestad & Wong, JCAP 07 (2007) 004

Takada et al, PRD 73 (2006) 083520

- o **Galaxy cluster surveys**

Wang et al, PRL 95 (2005) 011302

- o **Weak lensing surveys (tomography)**

Hannestad et al, JCAP 06 (2006) 025

Song & Knox, PRD 70 (2004) 063510

- o **CMB lensing**

Perotto et al, JCAP 10 (2006) 013

Lesgourgues et al, PRD 73 (2006) 045021

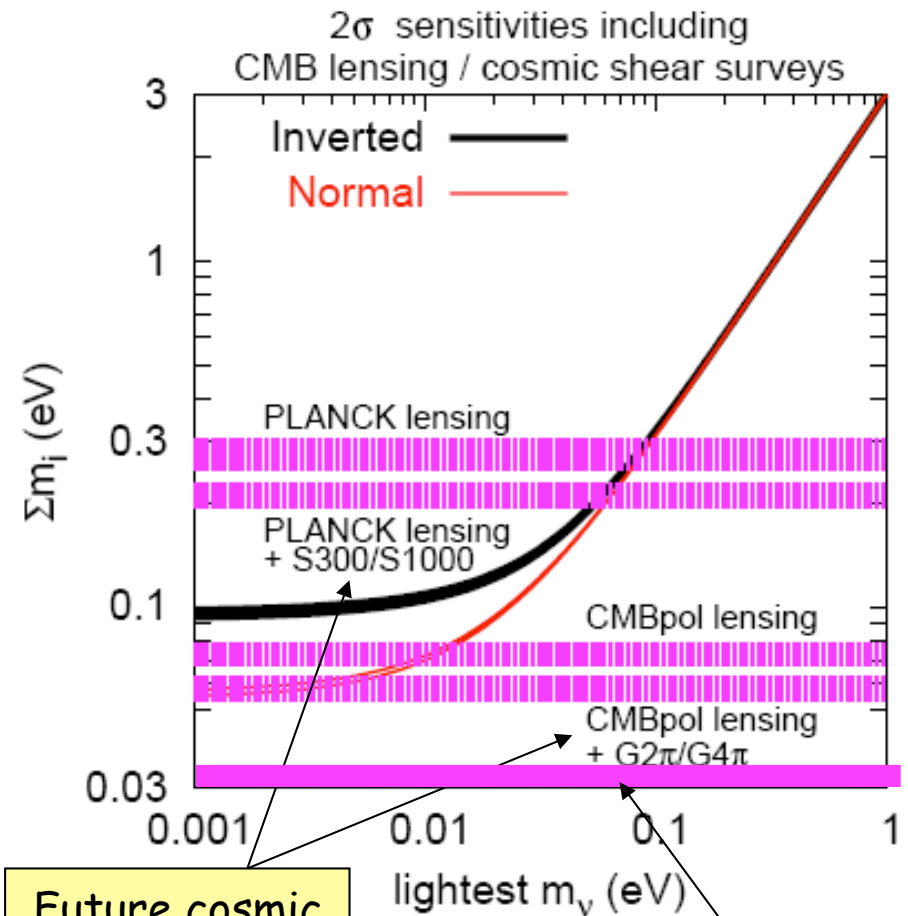
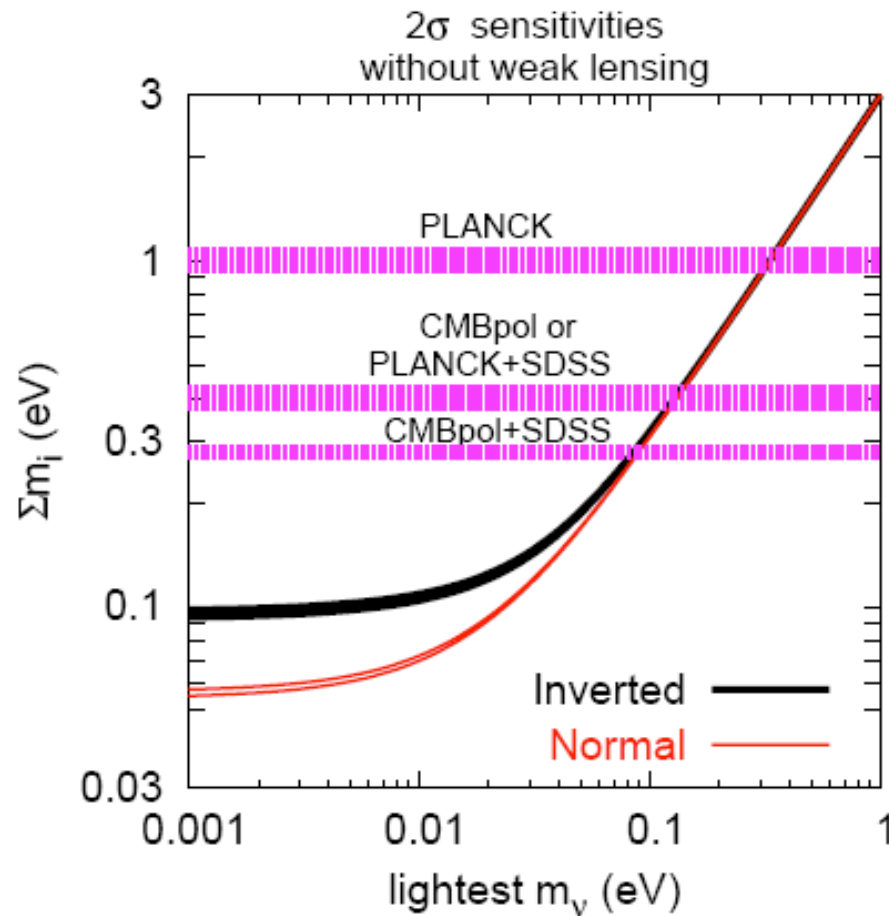
- o **Fluctuations in the 21 cm H line**

Loeb & Wyithe, PRL 100 (2008) 161301

Pritchard & Pierpaoli, PRD 78 (2008) 065009

Forecasts  
indicate  
7-100 meV  
sensitivities on  
 $\Sigma m_\nu$  are  
possible

# Summary of future sensitivities



Future cosmic shear surveys

Future high-z 21cm observations

# Summary of future sensitivities

| Probe                     | Potential sensitivity (short term) | Potential sensitivity (long term) |
|---------------------------|------------------------------------|-----------------------------------|
| CMB                       | 0.4-0.6                            | 0.4                               |
| CMB with lensing          | 0.1-0.15                           | 0.04                              |
| CMB + Galaxy Distribution | 0.2                                | 0.05-0.1                          |
| CMB + Lensing of Galaxies | 0.1                                | 0.03-0.04                         |
| CMB + Lyman- $\alpha$     | 0.1-0.2                            | Unknown                           |
| CMB + Galaxy Clusters     | -                                  | 0.05                              |
| CMB + 21 cm               | -                                  | 0.0003-0.1                        |

**Table 1.** Future probes of neutrino mass, as well as their projected sensitivity to neutrino mass. Sensitivity in the short term means achievable in approximately 5-7 years, while long term means 7-15 years.

Hannestad, arXiv:1007.0658



# Conclusions

Cosmological observables can be used to bound (or measure) neutrino properties, in particular the sum of neutrino masses (info **complementary** to laboratory results)

The **radiation content of the Universe** ( $N_{\text{eff}}$ ) will be very constrained in the near future (Planck)

Current bounds on the **sum of neutrino masses** from cosmological data  
(best  $\Sigma m_\nu < 0.4-0.6 \text{ eV}$ , conservative  $\Sigma m_\nu < 1 \text{ eV}$ )

**Different cosmological observations** in the next future  $\rightarrow$  **Sub-eV sensitivity** (0.1-0.2 eV and better)  $\rightarrow$  Test degenerate mass region and eventually the minimum total mass for IH case