

Benasque, IMFP 2005

March 10th, 2005

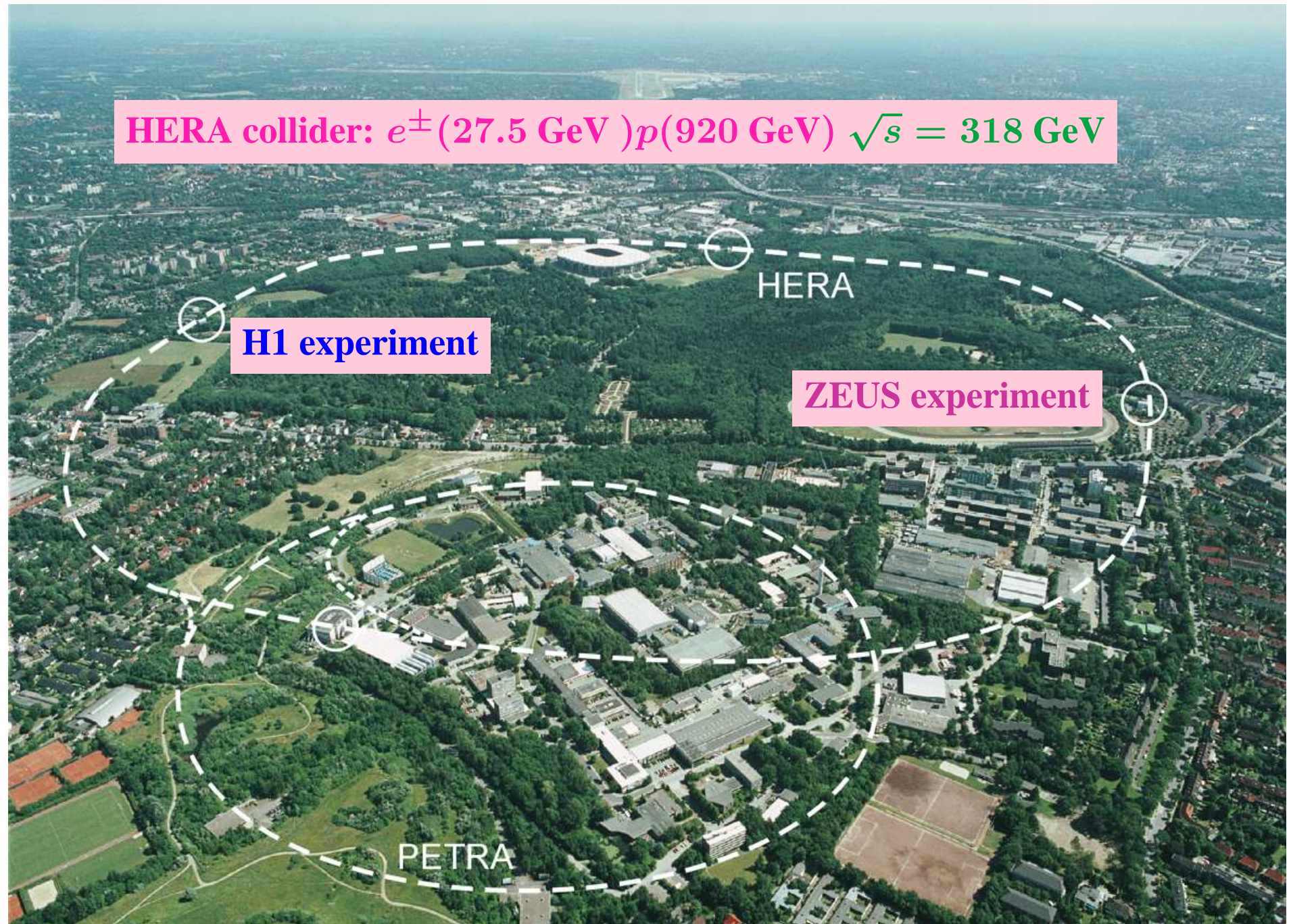
HERA PHYSICS

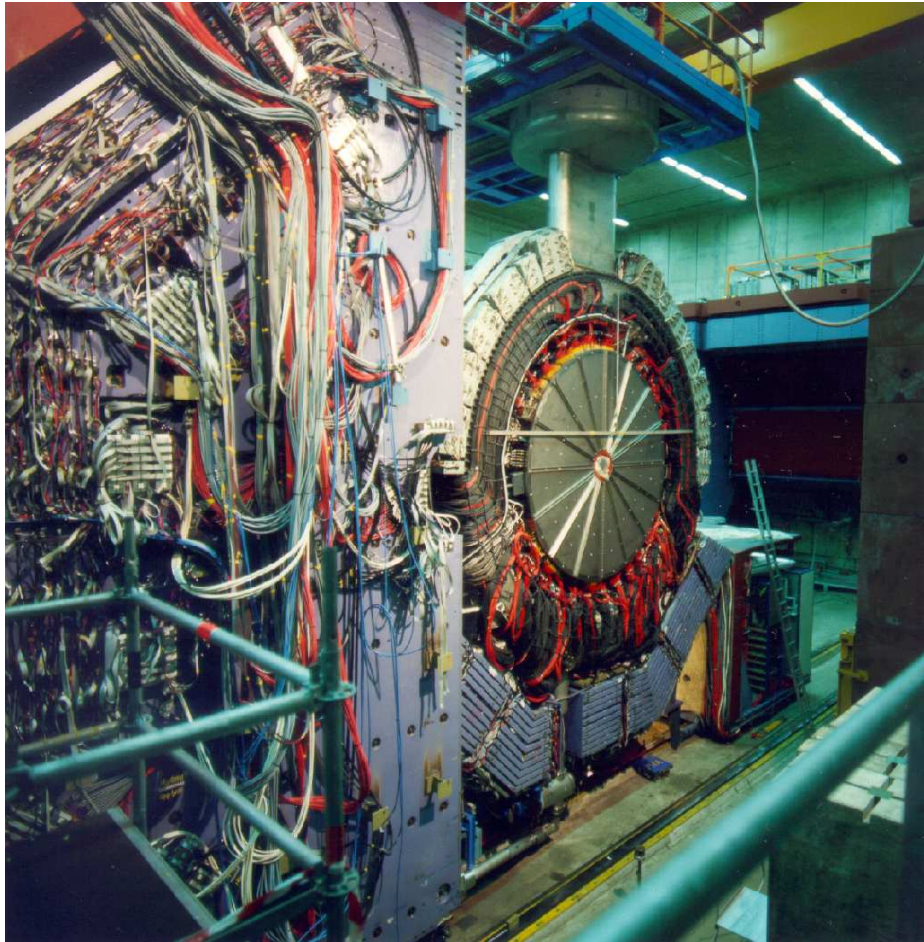
Juan Terrón (Universidad Autónoma de Madrid, Spain)



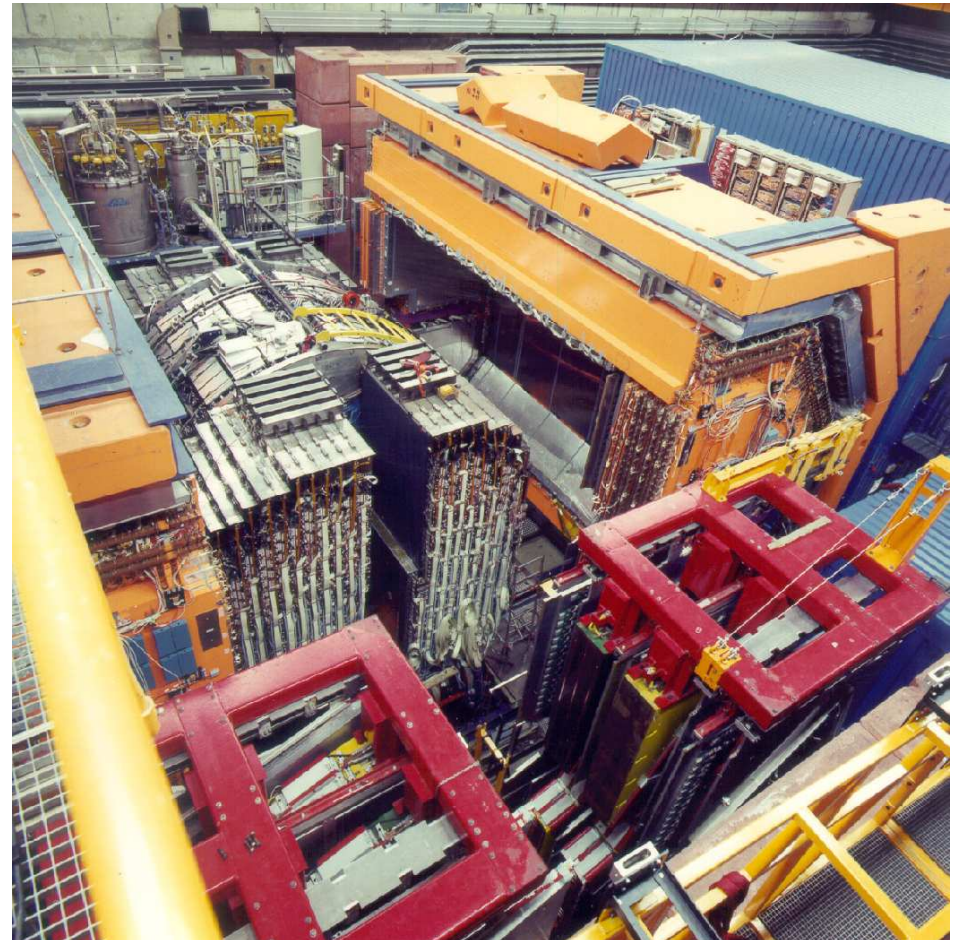
- **Outline**

- **Structure Functions**
- **Electroweak Measurements**
- **Jets and α_s**
- **HERA II**





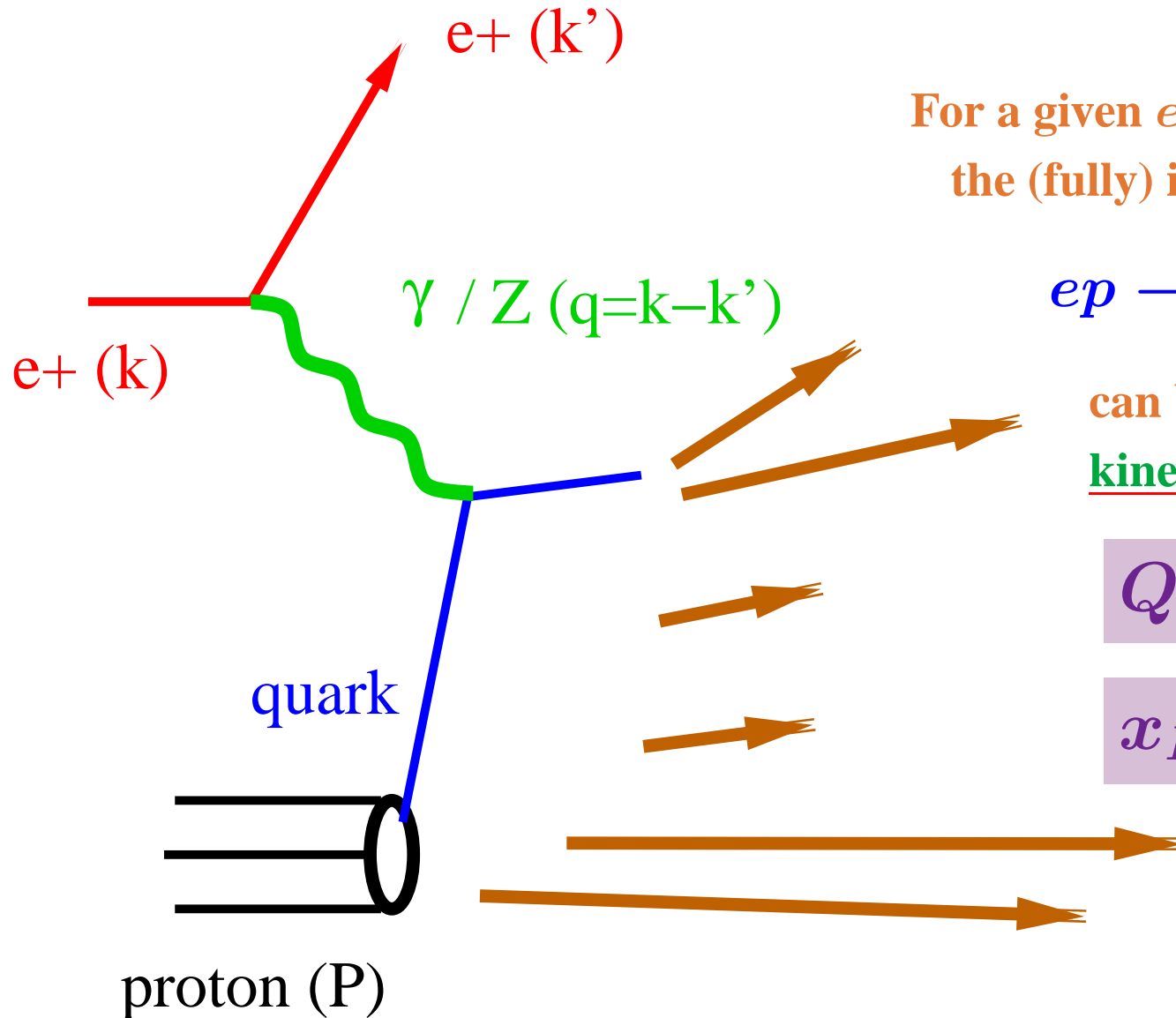
← H1 detector



ZEUS detector ⇒

Structure Functions

Kinematics of Neutral Current Deep Inelastic Scattering



For a given ep centre-of-mass energy, \sqrt{s} ,
the (fully) inclusive cross section for

$$ep \rightarrow e + X$$

can be described by two independent kinematic variables, e.g.

$$Q^2 = -(k - k')^2$$

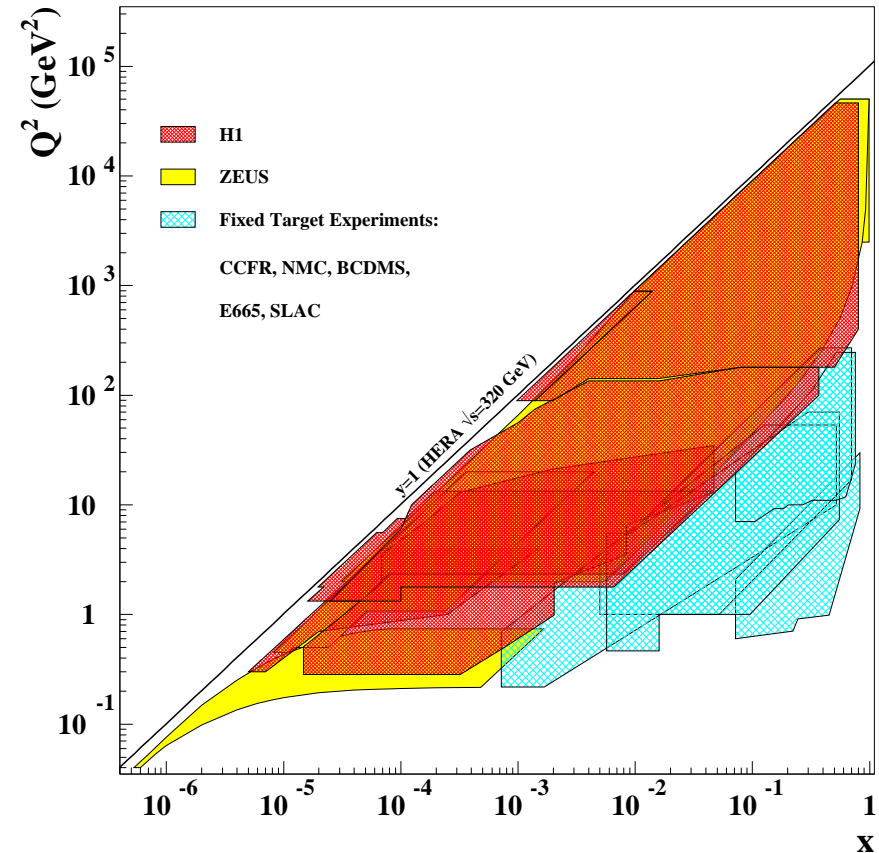
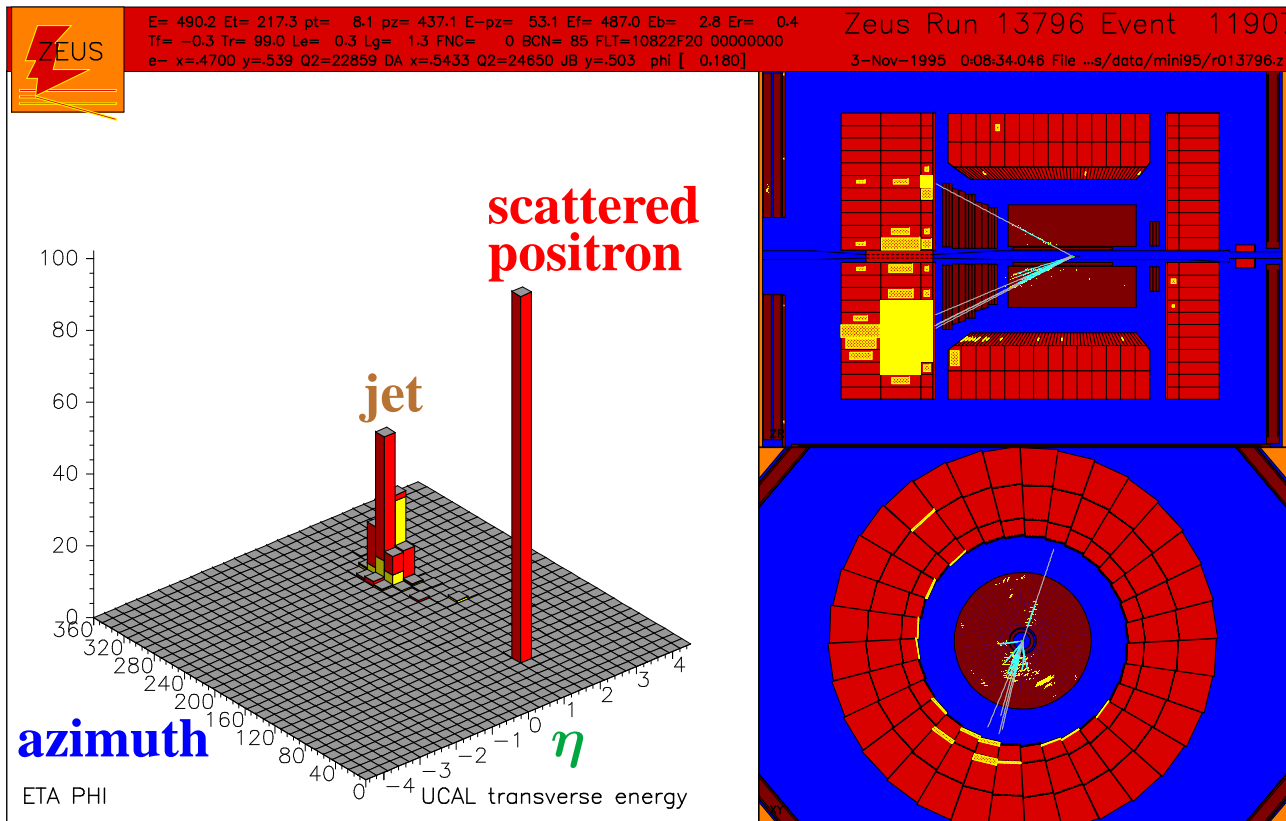
$$x_{Bj} = Q^2 / (2P \cdot q)$$

Neutral Current Deep Inelastic Scattering

- Neutral Current DIS event candidate

$Q^2 \sim 24000 \text{ GeV}^2$ and $x_{Bj} \sim 0.5$

- Coverage of kinematic plane (Q^2, x_{Bj})



Neutral Current Deep Inelastic Scattering

- Inclusive process $e^\pm p \rightarrow e^\pm + X$

$$\frac{d\sigma(e^\pm p)}{dx dQ^2} = \frac{2\pi\alpha^2}{xQ^4} \cdot \left(\underbrace{Y_+ \cdot F_2(x, Q^2)}_{\text{Dominant}} - \underbrace{y^2 \cdot F_L(x, Q^2)}_{\text{High } y} \mp \underbrace{Y_- \cdot x F_3(x, Q^2)}_{\text{High } Q^2} \right)$$

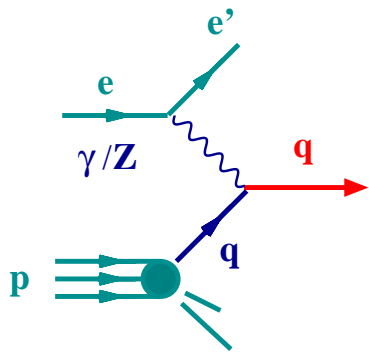
where $Y_\pm = 1 \pm (1 - y)^2$ and $y = Q^2 / (sx)$ (inelasticity parameter)

- Structure functions of the proton (F_2, F_L, F_3) and QCD

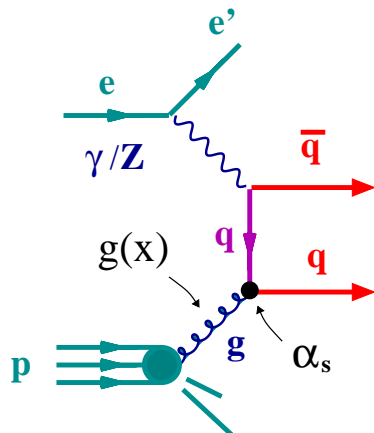
→ $F_2 \sim x \sum_i e_i^2 \cdot (q_i(x, Q^2) + \bar{q}_i(x, Q^2))$ for $Q^2 \ll M_Z^2$

→ the longitudinal structure function $F_L = 0$ in the quark-parton model

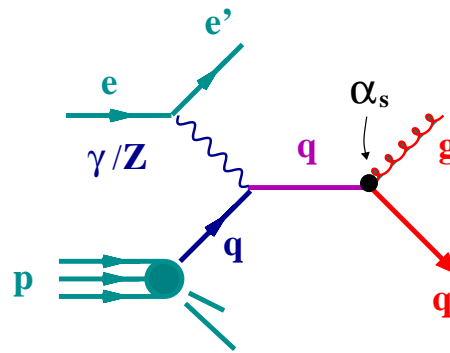
→ parity-violating term F_3 is small for $Q^2 \ll M_Z^2$



Quark-Parton Model



Boson-Gluon Fusion



QCD Compton

Clean probe of the
Parton Distribution
Functions in the Proton
 $q_i(x, Q^2), \bar{q}_i(x, Q^2)$
 $g(x, Q^2)$

Determination of $F_2^{\text{em}}(x, Q^2)$

- Measurement of the doubly-differential cross section $d\sigma(e^+p)/dx dQ^2$ for the reaction $e^+p \rightarrow e^+ + X$ over a large range $2.7 < Q^2 < 30000 \text{ GeV}^2$, $6 \cdot 10^{-5} < x < 0.65$
- Extraction of $F_2^{\text{em}}(x, Q^2)$ from the reduced cross section (corrected for QED effects):

$$\tilde{\sigma}(e^+p) = (2\pi\alpha^2 Y_+ / xQ^4)^{-1} d\sigma_{\text{Born}} / dx dQ^2$$

$$F_2 = F_2^{\text{em}} + F_2^{\text{int}} \cdot \eta_{\gamma Z} + F_2^{\text{wk}} \cdot \eta_{\gamma Z}^2$$

$$= F_2^{\text{em}}(1 + \Delta_{F_2})$$

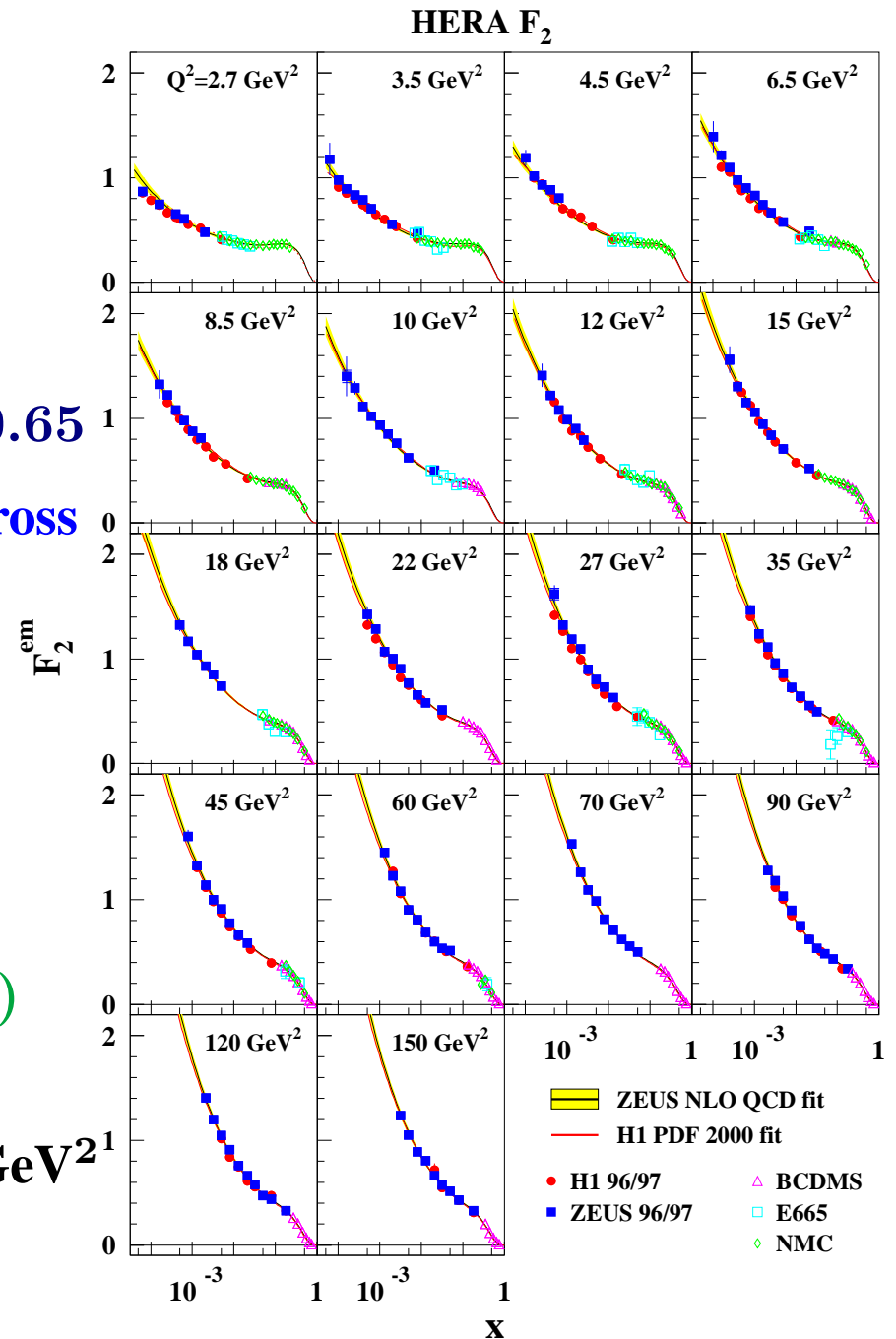
$$\text{where } \eta_{\gamma Z} = Q^2 / (Q^2 + M_Z^2)$$

$$\Rightarrow \tilde{\sigma}(e^+p) = F_2^{\text{em}}(1 + \Delta_{F_2} + \Delta_{F_3} + \Delta_{F_L})$$

- Typical precision 2-3%

→ systematic uncertainties dominate $Q^2 < 800 \text{ GeV}^2$

- Striking rise of F_2^{em} as x decreases



$F_2^{\text{em}}(x, Q^2)$ provides...

→ direct information on quark densities

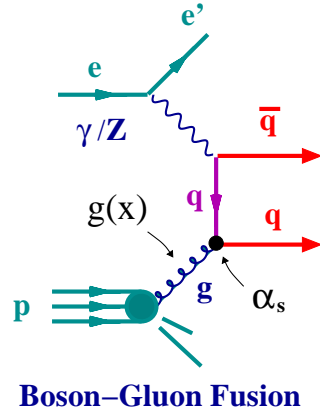
$$F_2 \sim x \sum_i e_i^2 \cdot (q_i + \bar{q}_i)$$

→ indirect information on gluon density

● Large and positive scaling violations at low x

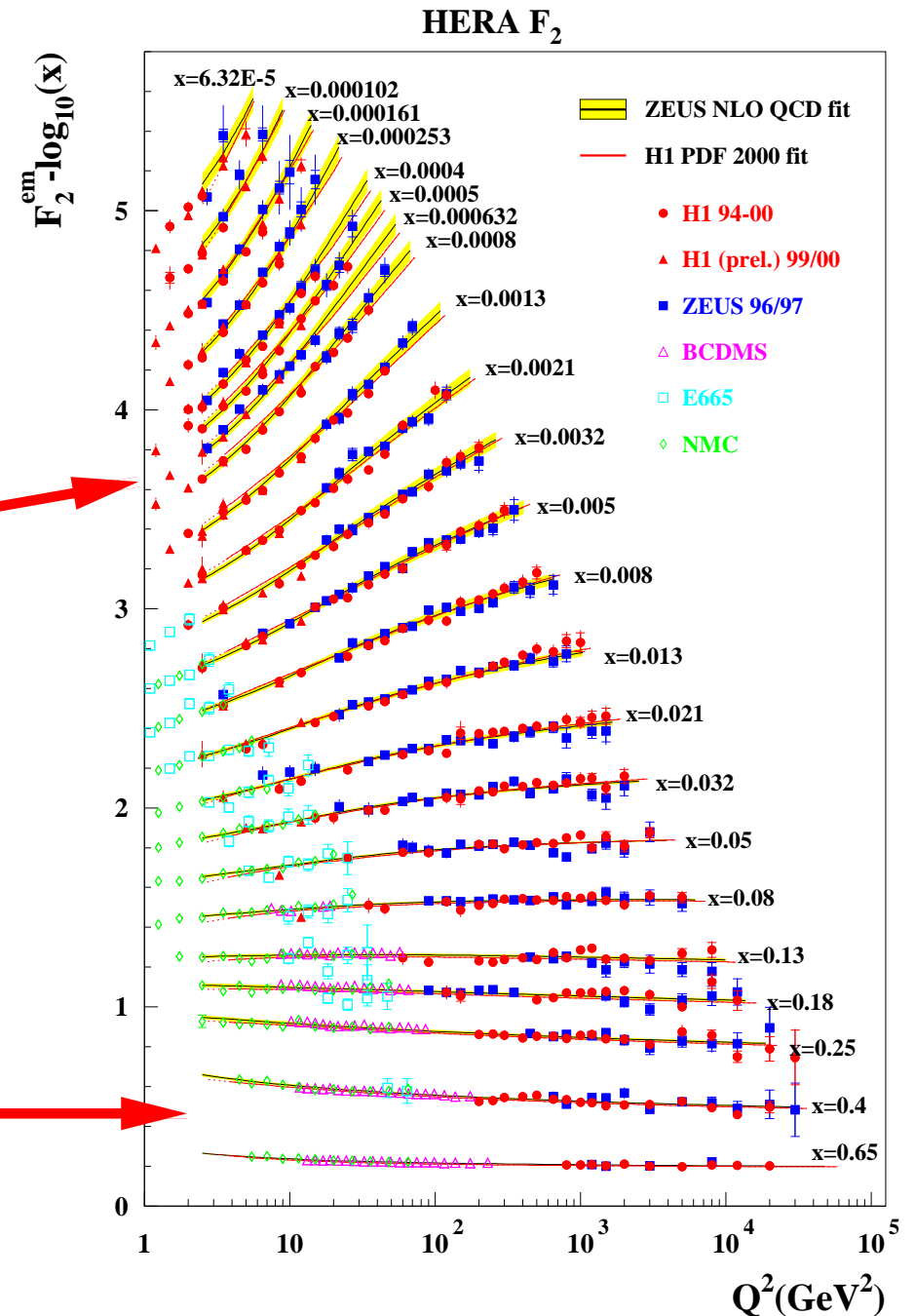
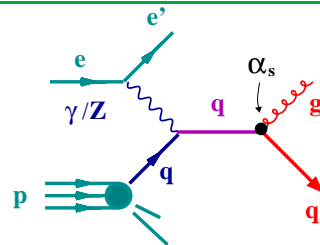
dominance of BGF

$$\partial F_2 / \partial \ln Q^2 \sim \alpha_s \cdot xg$$



● Aproximate scaling for $x \sim 0.1$

● Mild and negative scaling violations at high x



Determination of the Parton Distribution Functions in the Proton

- In order to determine the proton PDFs additional experimental information is needed on
 - quark densities at high x
 - **flavour composition of the sea**
- Additional data sets
 - F_2 data on μp scattering from BCDMS, NMC and E665 \Rightarrow mid/high- x
 - **Deuterium-target data from NMC and E665 $\Rightarrow \bar{u}, \bar{d}$**
 - NMC data on the ratio $F_2^D / F_2^P \Rightarrow$ high- x d/u
 - $x F_3$ data from CCFR (ν -Fe interactions) \Rightarrow high- x

- Global analysis using DGLAP evolution equations at next-to-leading order (NLO) in α_s

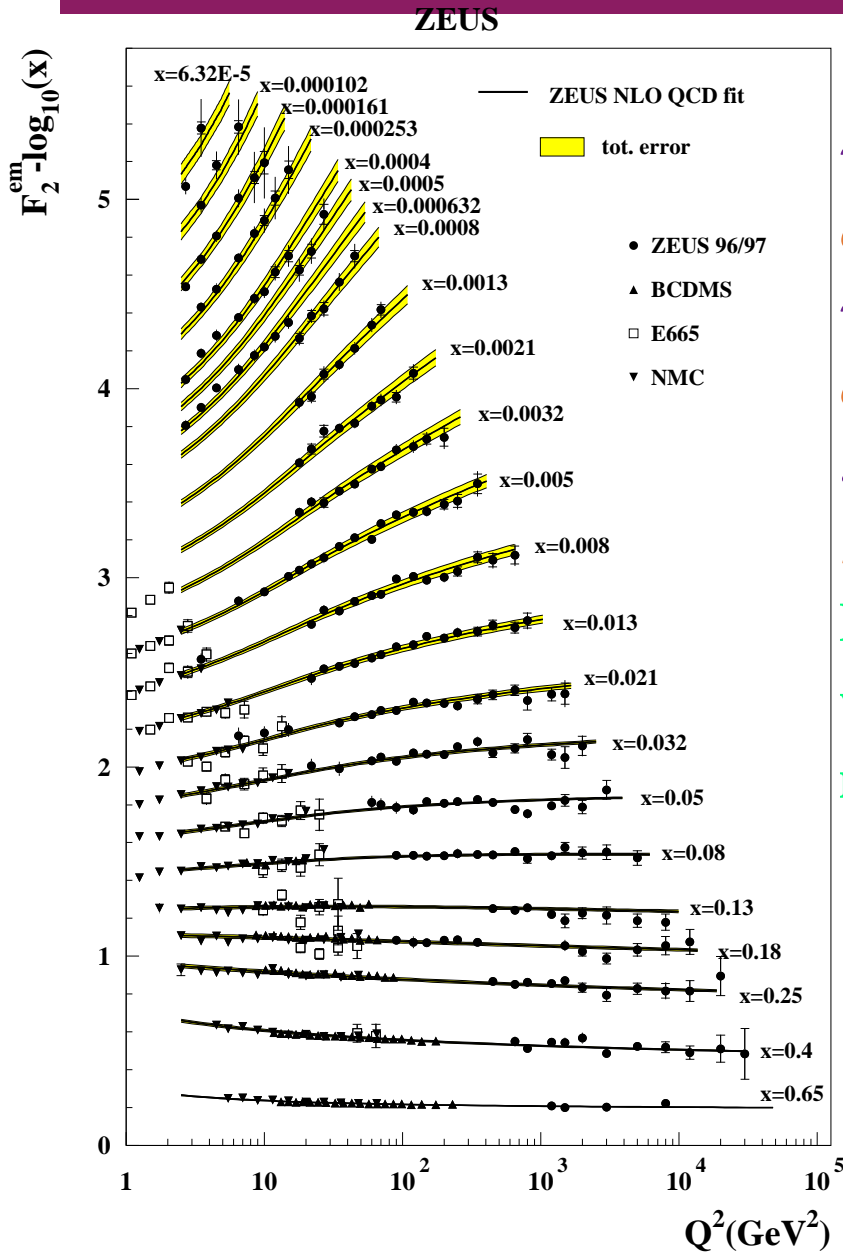
$$\frac{\partial q_i(x, \mu^2)}{\partial \ln \mu^2} = \frac{\alpha_s(\mu^2)}{2\pi} \int_x^1 \frac{dz}{z} \left(\sum_j P_{q_i q_j} \cdot q_j(x/z, \mu^2) + P_{q_i g} \cdot g(x/z, \mu^2) \right)$$

$$\frac{\partial g(x, \mu^2)}{\partial \ln \mu^2} = \frac{\alpha_s(\mu^2)}{2\pi} \int_x^1 \frac{dz}{z} \left(\sum_j P_{g q_j} \cdot q_j(x/z, \mu^2) + P_{g g} \cdot g(x/z, \mu^2) \right)$$

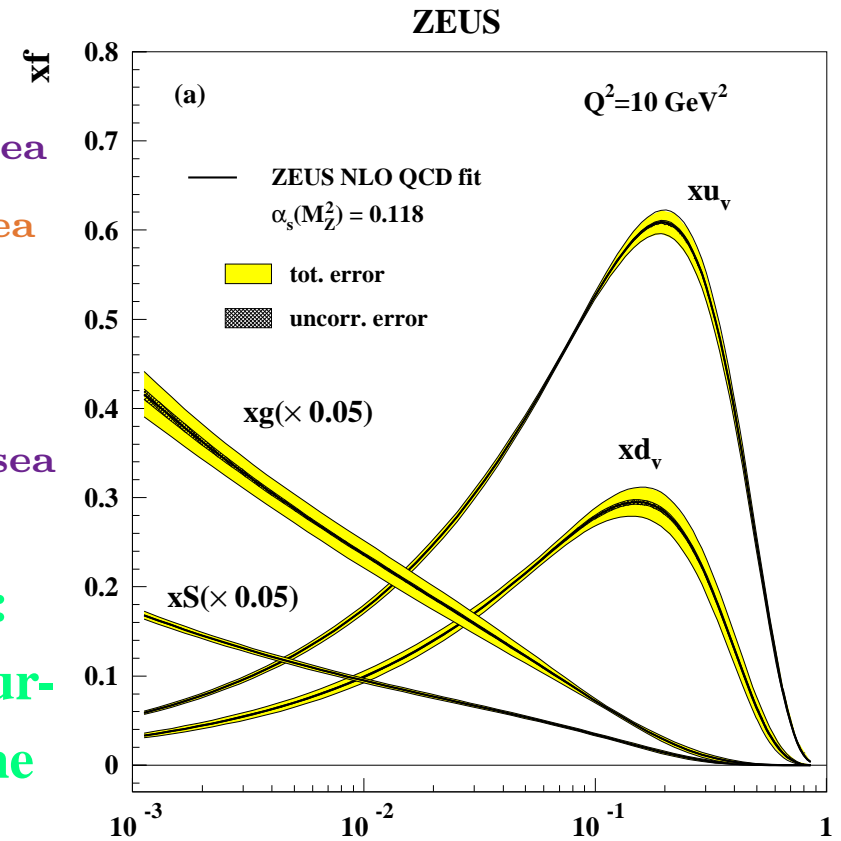
The DGLAP equations yield the proton PDFs at any value of Q^2 provided they are input as functions of x at some input scale Q_0^2

→ number sum rules and the momentum sum rule are imposed

Determination of the Parton Distribution Functions in the Proton



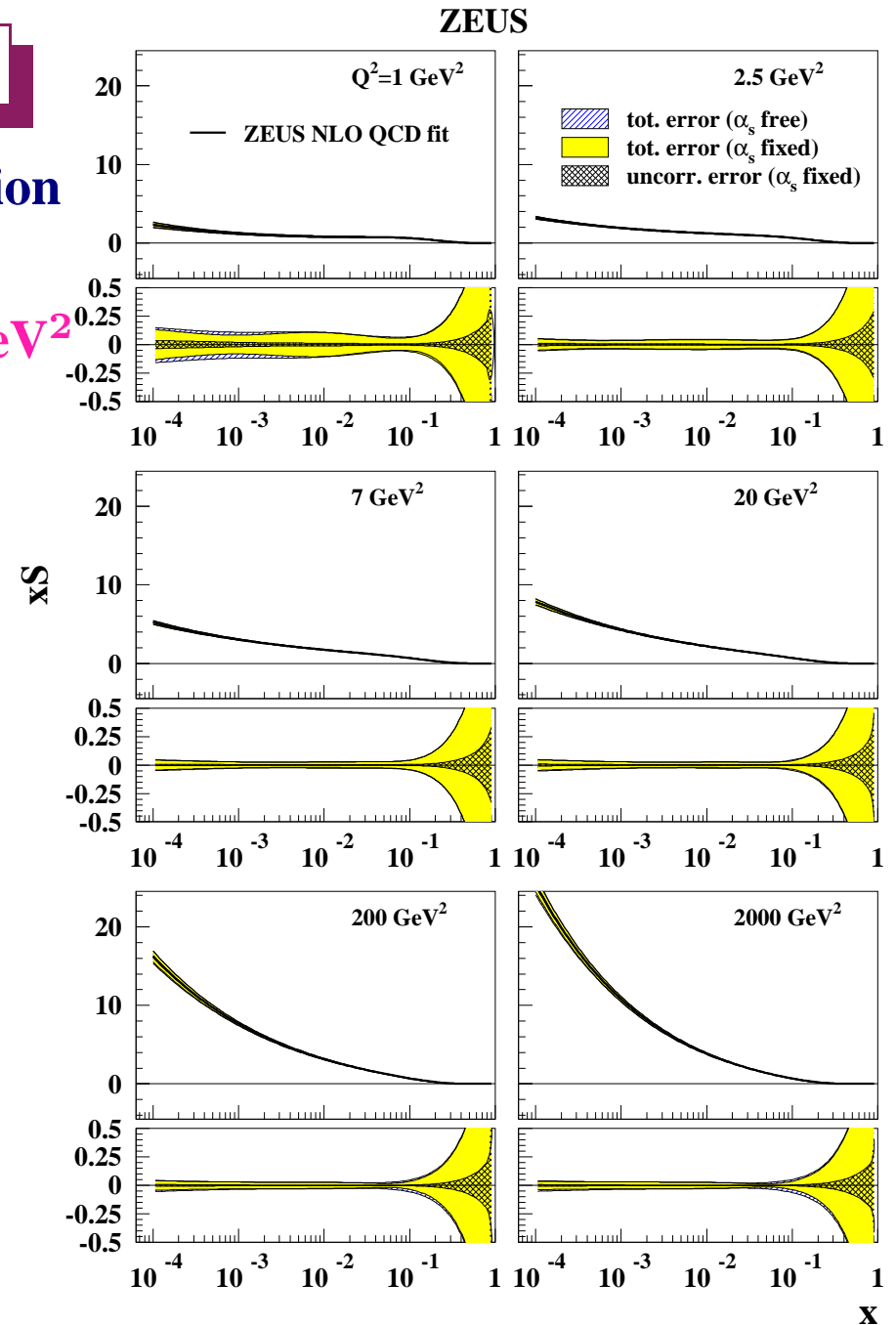
$u = u_V + u_{sea}$
 $d = d_V + d_{sea}$
 $\bar{u} = \bar{u}_{sea}$
 $\bar{d} = \bar{d}_{sea}$
 $s = s_{sea} = \bar{s}_{sea}$
 $S = \text{total sea}$
**Heavy quarks:
 variable-flavour-
 number scheme**



Fit of ZEUS data and fixed-target data in the region
 $2.5 < Q^2 < 30000 \text{ GeV}^2$, $6.3 \cdot 10^{-5} < x < 0.65$
and $W^2 > 20 \text{ GeV}^2$ (1263 data points)
Full account of correlated exp. uncertainties
→ Good description of Struct. Func. data
⇒ Determination of proton PDFs

Determination of the Sea Distribution

- The total sea distribution $xS(x, Q^2)$ as a function of x for different Q^2 values \Rightarrow
- Its uncertainty is below $\sim 5\%$ for $Q^2 > 2.5 \text{ GeV}^2$ and $10^{-4} < x < 0.1$

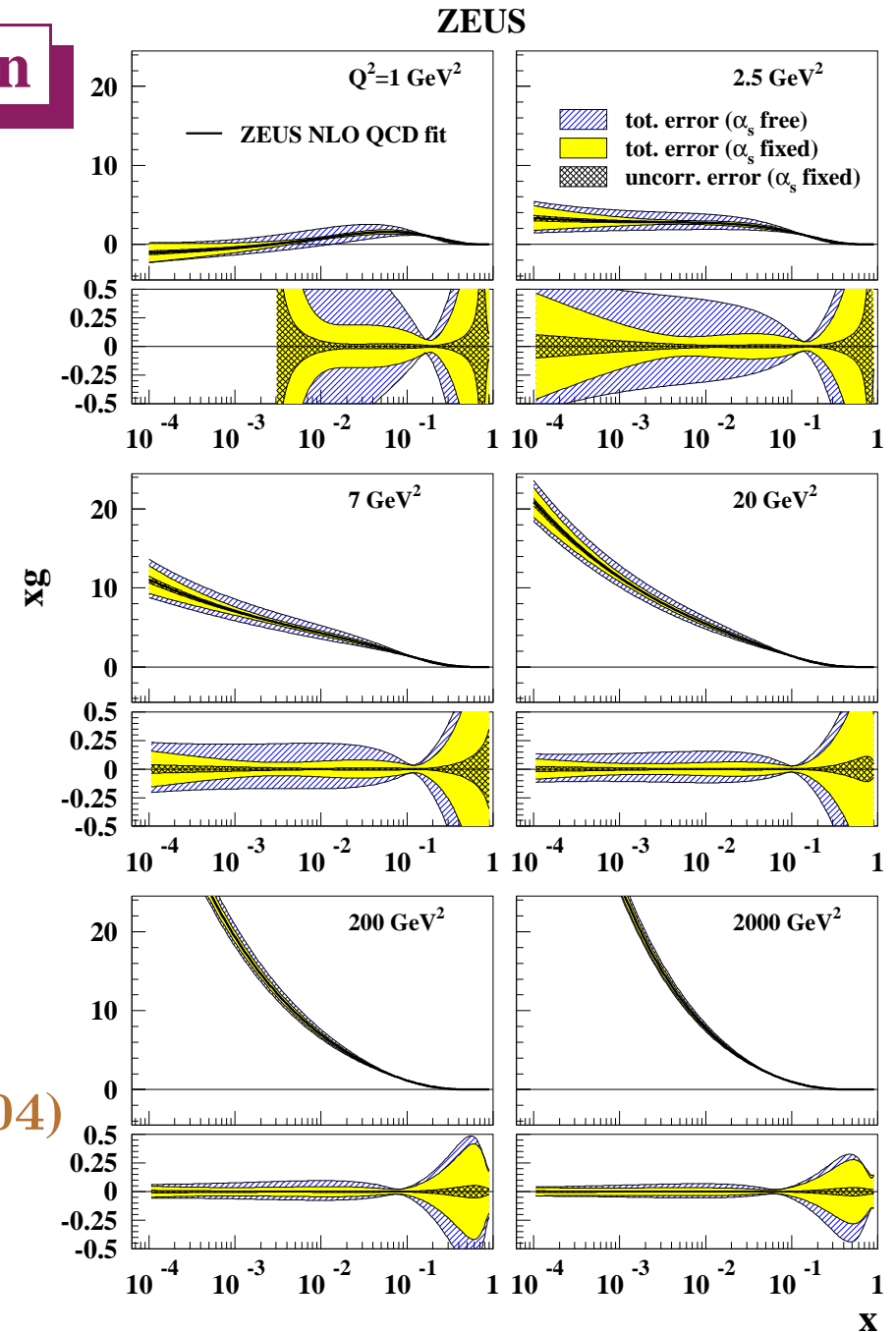


Determination of the Gluon Distribution

- The gluon distribution $xg(x, Q^2)$ as a function of x for different Q^2 values \Rightarrow
- Its uncertainty is $\sim 10\%$ for $Q^2 \sim 20 \text{ GeV}^2$ and $10^{-4} < x < 0.1$
 \rightarrow the uncertainty decreases as Q^2 increases

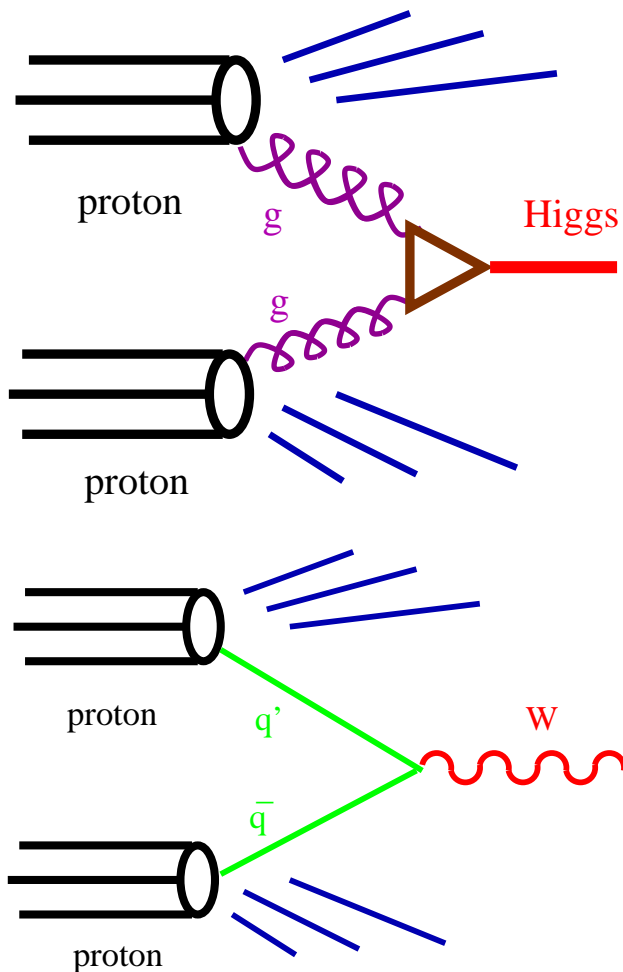
Determination of α_s

- Inclusion of low- x data allows a simultaneous (and precise) determination of PDFs and α_s :
 $\alpha_s(M_Z) = 0.1166 \pm 0.0008(\text{uncorr})$
 $\pm 0.0032(\text{corr}) \pm 0.0036(\text{norm})$
 $\pm 0.0018(\text{model}) \Rightarrow 0.1166 \pm 0.0052$
 (+theor. unc. due to terms beyond NLO $\sim \pm 0.004$)
- Consistent with world average (Bethke, 2004):
 $\rightarrow \alpha_s(M_Z) = 0.1182 \pm 0.0027$



Universality (and usefulness) of Proton PDFs

$$\sigma_{pp \rightarrow H(W,Z,\dots)+X} = \sum_{a,b} \int_0^1 dx_1 f_{a/p}(x_1, \mu_F^2) \int_0^1 dx_2 f_{b/p}(x_2, \mu_F^2) \hat{\sigma}_{ab \rightarrow H(W,Z,\dots)}$$



σ_H sensitive to gluon distribution at

$$x \sim \frac{M_H}{\sqrt{s}} \sim 8 \cdot 10^{-3}$$

and $\mu_F^2 \sim M_H^2 \sim 13000 \text{ GeV}^2$;

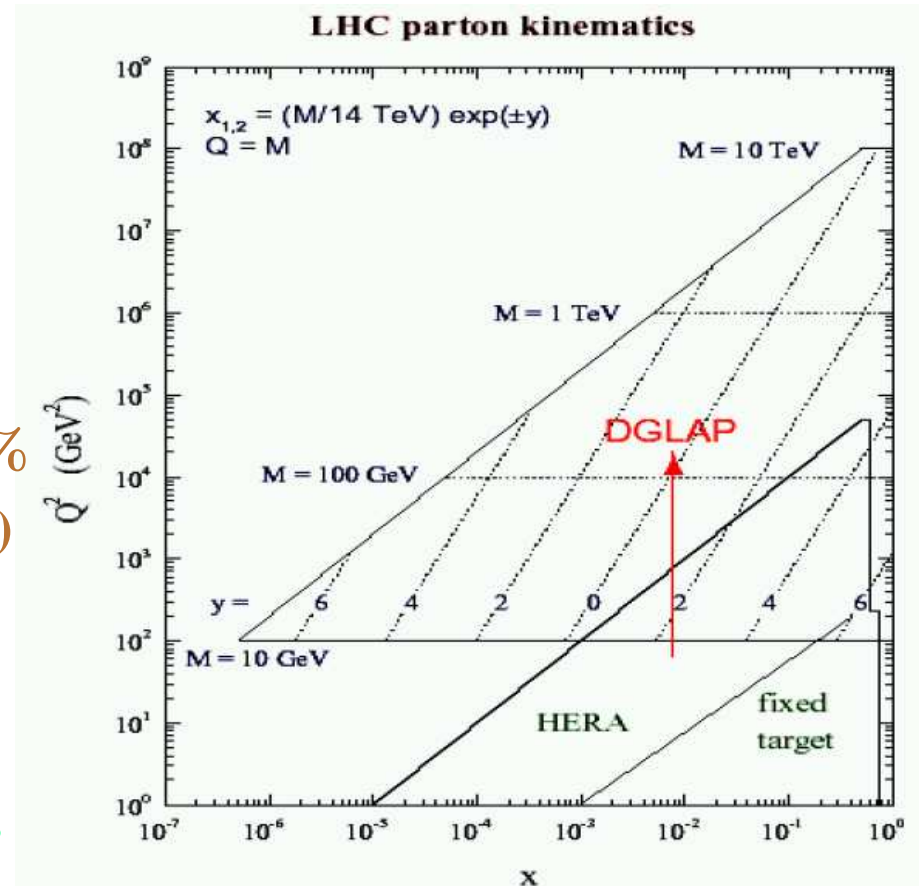
$$\Delta\sigma_H^{PDF} / \sigma_H \sim \pm 3\%$$

(for $M_H = 115 \text{ GeV}$)

σ_W sensitive to sea distribution at

$$x \sim \frac{M_W}{\sqrt{s}} \sim 6 \cdot 10^{-3}$$

$$\text{and } \mu_F^2 \sim M_W^2 \sim 6400 \text{ GeV}^2; \Delta\sigma_W^{PDF} / \sigma_W \sim \pm 3\%$$

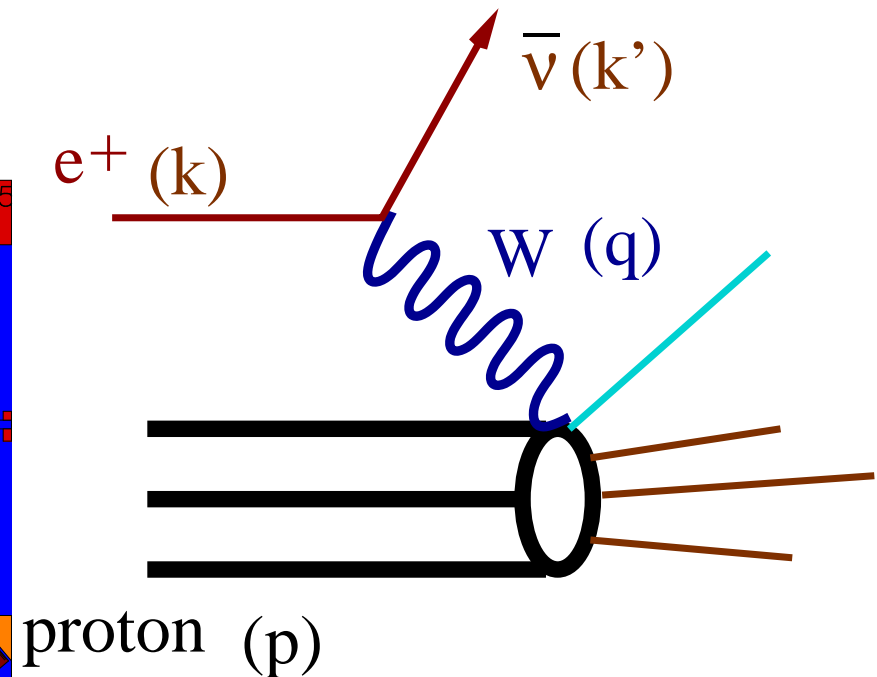
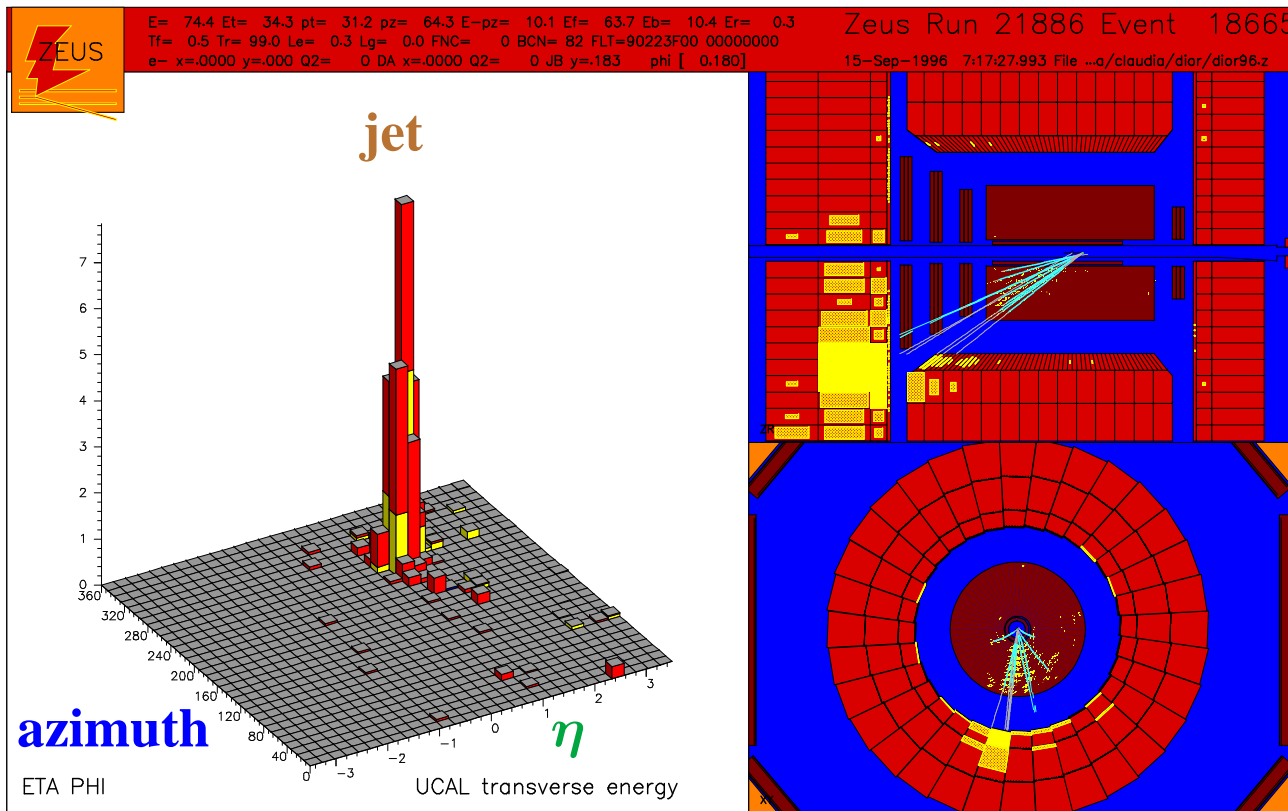


Electroweak Measurements

Charged Current Deep Inelastic Scattering

- Charged Current DIS event candidate

$$Q^2 \sim 1200 \text{ GeV}^2 \text{ and } x_{Bj} \sim 0.06$$



Charged Current Deep Inelastic Scattering

- Measurements of the differential cross section

$d\sigma/dQ^2$ in Charged Current DIS $e^\pm p$

$$ep \rightarrow \nu + X$$

- Cross-section formulae in LO QCD

$$\frac{d\sigma(e^+p)}{dx dQ^2} = \frac{G_F^2}{2\pi} \eta_W^2 \cdot \sum_i (\bar{u}_i + (1-y)^2 d_i)$$

$$\frac{d\sigma(e^-p)}{dx dQ^2} = \frac{G_F^2}{2\pi} \eta_W^2 \cdot \sum_i (u_i + (1-y)^2 \bar{d}_i)$$

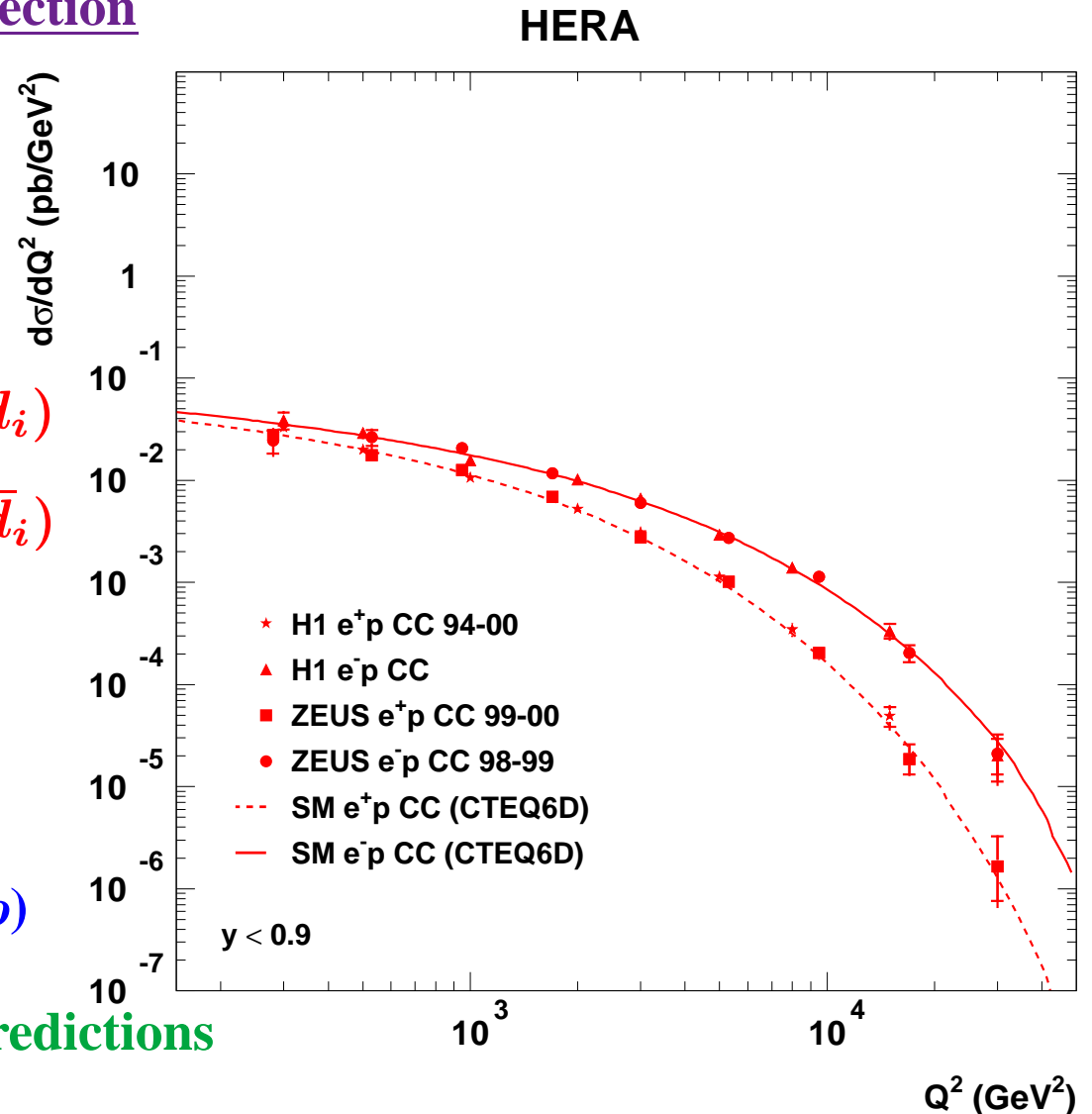
where $\eta_W = M_W^2 / (Q^2 + M_W^2)$

⇒ W -Propagator effects

⇒ flavour selection:

d (u)-quark contributes only to e^+p (e^-p)

- Good description by Standard Model Predictions up to the highest $Q^2 \sim 30000 \text{ GeV}^2$



Neutral Current Deep Inelastic Scattering

- Measurements of the differential cross section

$d\sigma/dQ^2$ in Neutral Current DIS $e^\pm p$

$$ep \rightarrow e + X$$

- Cross-section formulae in LO QCD

$$\frac{d\sigma(e^\pm p)}{dx dQ^2} = \frac{2\pi\alpha^2}{xQ^4} \cdot (Y_+ \cdot F_2(x, Q^2) -$$

$$-y^2 \cdot F_L(x, Q^2) \mp Y_- \cdot xF_3(x, Q^2))$$

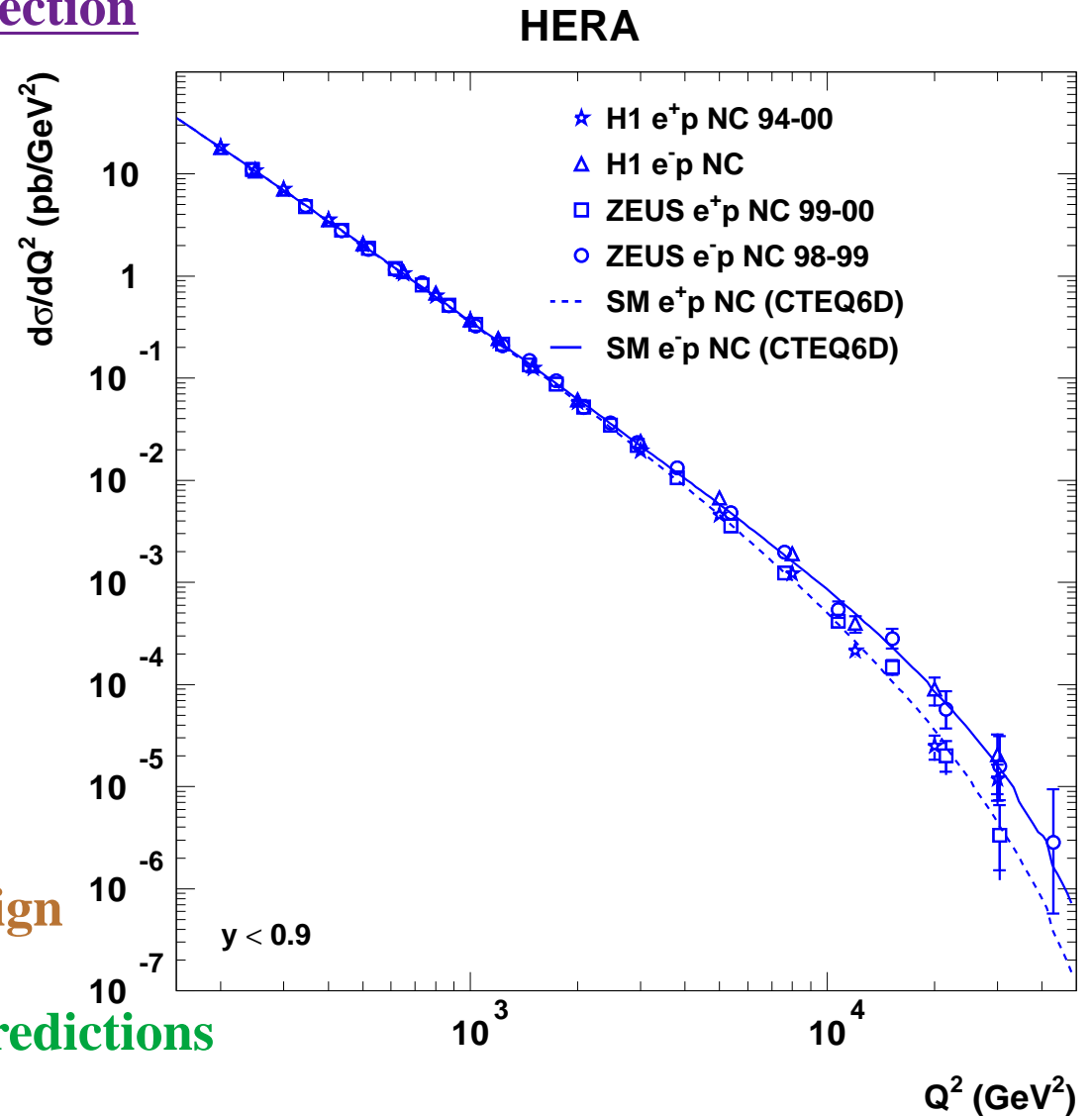
$$F_2 = F_2^{\text{em}} + F_2^{\text{int}} \cdot \eta_{\gamma Z} + F_2^{\text{wk}} \cdot \eta_{\gamma Z}^2$$

$$\text{where } \eta_{\gamma Z} = Q^2 / (Q^2 + M_Z^2)$$

⇒ **Z-Propagator effects**

⇒ **Parity-violating term (F_3) changes sign**

- **Good description by Standard Model Predictions**
up to the highest $Q^2 \sim 40000 \text{ GeV}^2$



Neutral vs Charged Current Deep Inelastic Scattering

Measurements of the differential cross section

$d\sigma/dQ^2$ in Neutral Current DIS $e^\pm p$

$$\frac{d\sigma(e^\pm p)}{dx dQ^2} = \frac{2\pi\alpha^2}{xQ^4} \cdot (Y_+ \cdot F_2(x, Q^2) - y^2 \cdot F_L(x, Q^2) \mp Y_- \cdot xF_3(x, Q^2))$$

$$F_2 = F_2^{\text{em}} + F_2^{\text{int}} \cdot \eta_{\gamma Z} + F_2^{\text{wk}} \cdot \eta_{\gamma Z}$$

$$\text{where } \eta_{\gamma Z} = Q^2 / (Q^2 + M_Z^2)$$

and Charged Current DIS $e^\pm p$

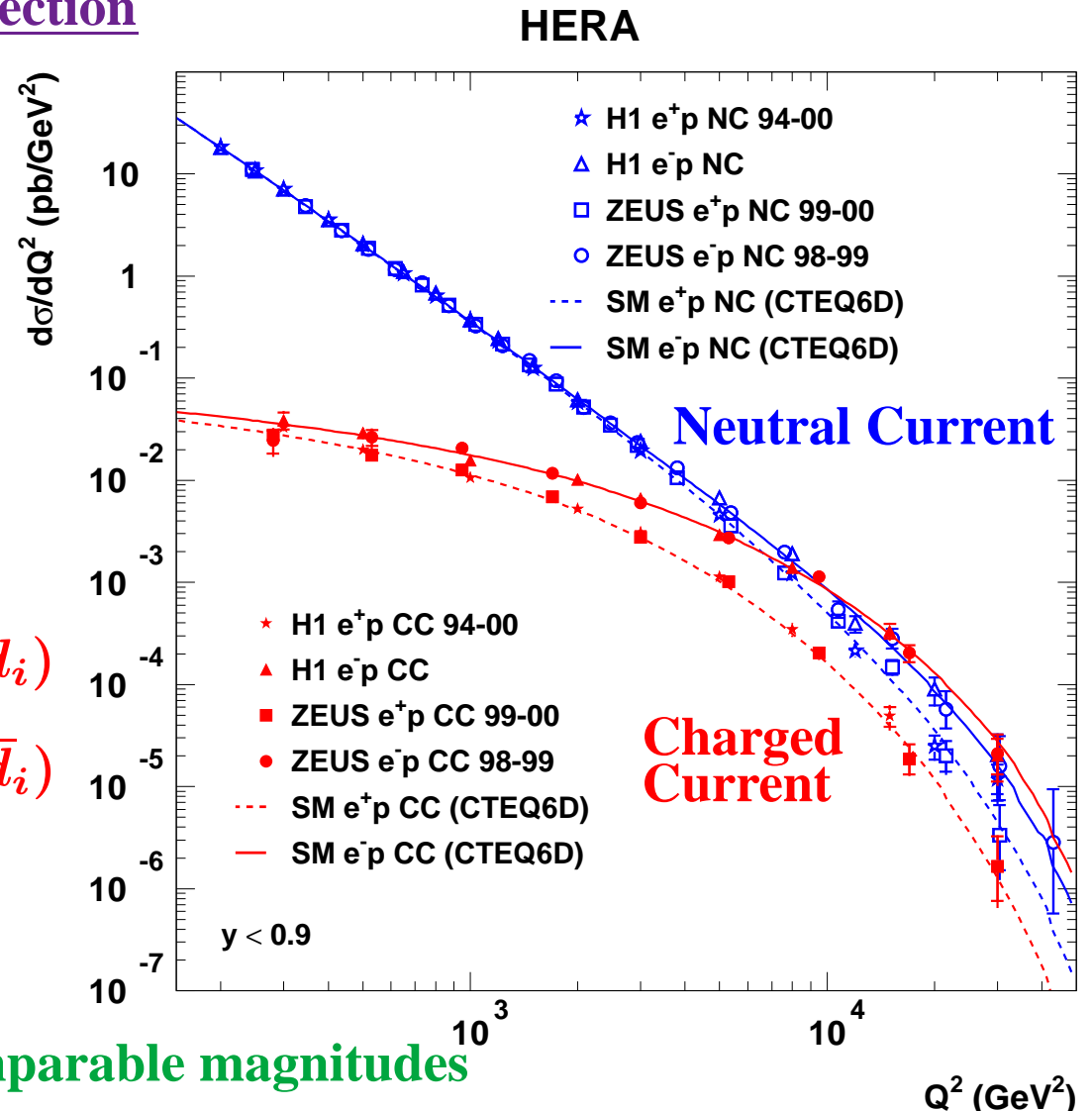
$$\frac{d\sigma(e^+ p)}{dx dQ^2} = \frac{G_F^2}{2\pi} \eta_W^2 \cdot \sum_i (\bar{u}_i + (1-y)^2 d_i)$$

$$\frac{d\sigma(e^- p)}{dx dQ^2} = \frac{G_F^2}{2\pi} \eta_W^2 \cdot \sum_i (u_i + (1-y)^2 \bar{d}_i)$$

$$\text{where } \eta_W = M_W^2 / (Q^2 + M_W^2)$$

NC and CC DIS cross sections have comparable magnitudes

at $Q^2 \sim M_W^2 \sim M_Z^2 \sim 10^4 \text{ GeV}^2 \Rightarrow$ **Direct observation of electroweak unification**



Charged Current Deep Inelastic e^+p Scattering

- Measurement of the reduced cross section in CC DIS:

$$\tilde{\sigma}(e^+p) = (G_F^2 \eta_W^2 / 2\pi x)^{-1} d\sigma_{\text{Born}} / dx dQ^2$$

→ Sensitivity to flavour composition

$$\tilde{\sigma}(e^+p) = x(\bar{u} + \bar{c} + (1-y)^2(d+s))$$

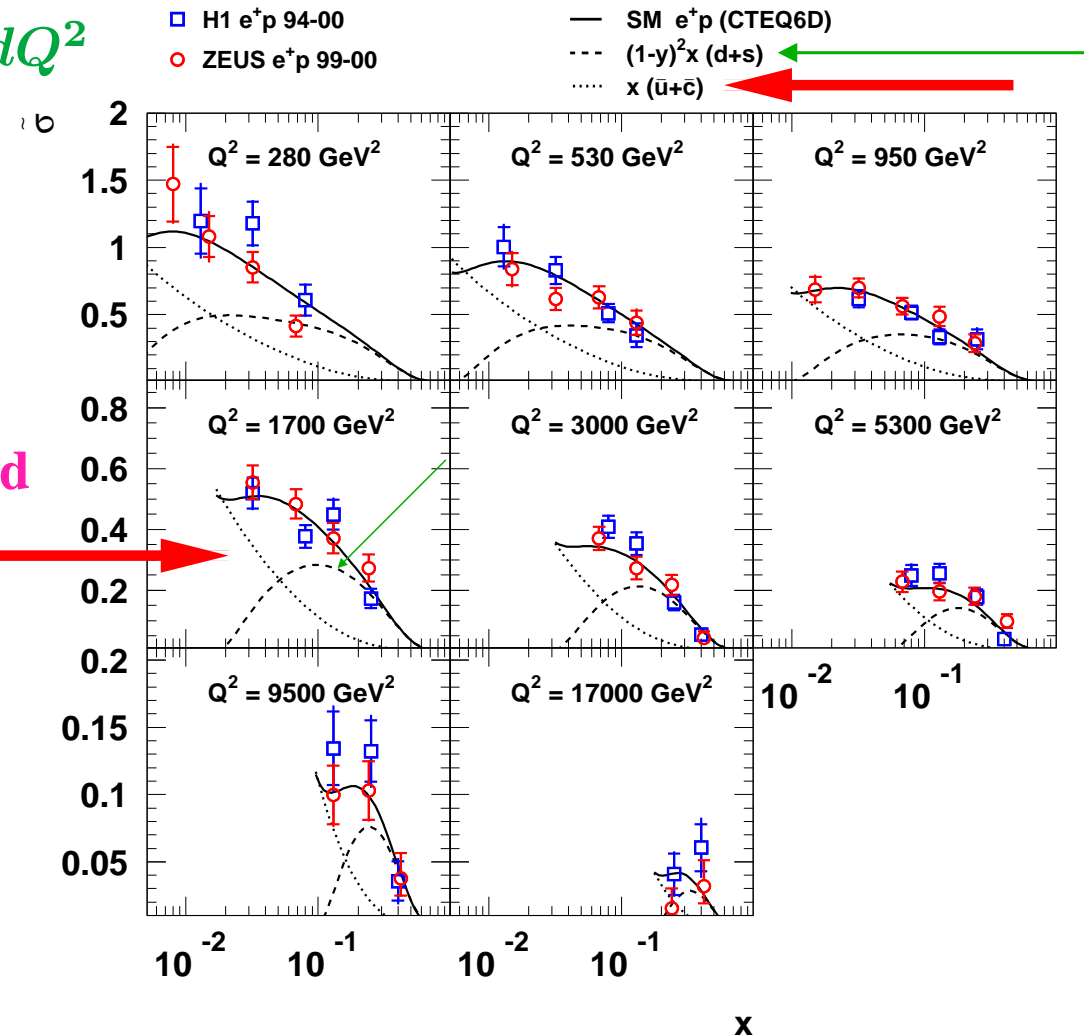
→ Sensitivity to valence quarks

$$\tilde{\sigma}(e^+p) \rightarrow x(1-y)^2 d_V \text{ (high-}x\text{)}$$

- Good description by SM predictions based on CTEQ6 parametrizations of PDFs

→ valence quarks and flavour composition determined from fixed-target data

HERA e^+p Charged Current



Charged Current Deep Inelastic e^-p Scattering

- Measurement of the reduced cross section in CC DIS:

$$\tilde{\sigma}(e^-p) = (G_F^2 \eta_W^2 / 2\pi x)^{-1} d\sigma_{\text{Born}} / dx dQ^2$$

→ Sensitivity to flavour composition

$$\tilde{\sigma}(e^-p) = x(u + c + (1 - y)^2(\bar{d} + \bar{s}))$$

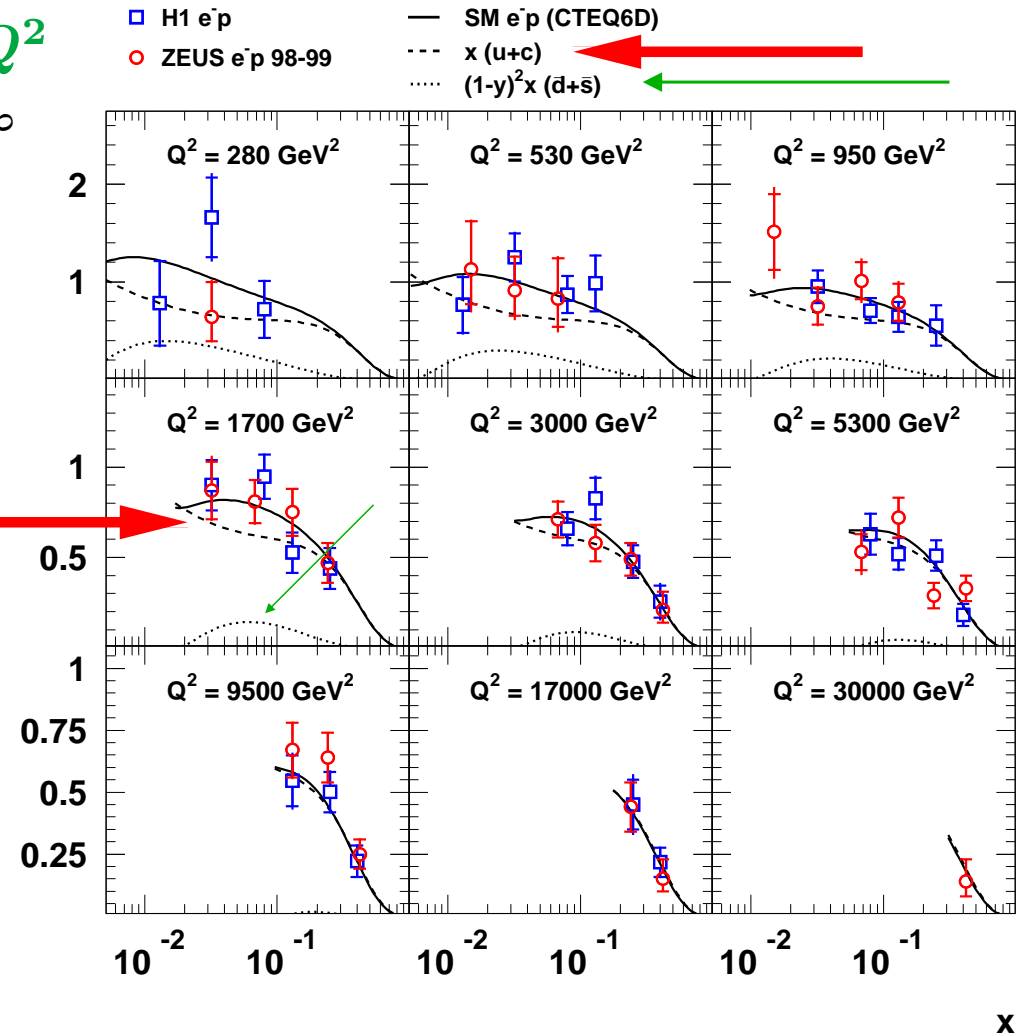
→ Sensitivity to valence quarks

$$\tilde{\sigma}(e^-p) \rightarrow xu_V \text{ (high-}x\text{)}$$

- Good description by SM predictions based on CTEQ6 parametrizations of PDFs

→ valence quarks and flavour composition determined from fixed-target data

HERA e^-p Charged Current



Charged Current Deep Inelastic e^+p and e^-p Scattering

- Measurements of the reduced cross section in CC DIS:

$$\tilde{\sigma}(e^\pm p) = (G_F^2 \eta_W^2 / 2\pi x)^{-1} d\sigma_{\text{Born}} / dx dQ^2$$

→ Sensitivity to flavour composition

$$\tilde{\sigma}(e^+p) = x(\bar{u} + \bar{c} + (1-y)^2(d + s))$$

$$\tilde{\sigma}(e^-p) = x(u + c + (1-y)^2(\bar{d} + \bar{s}))$$

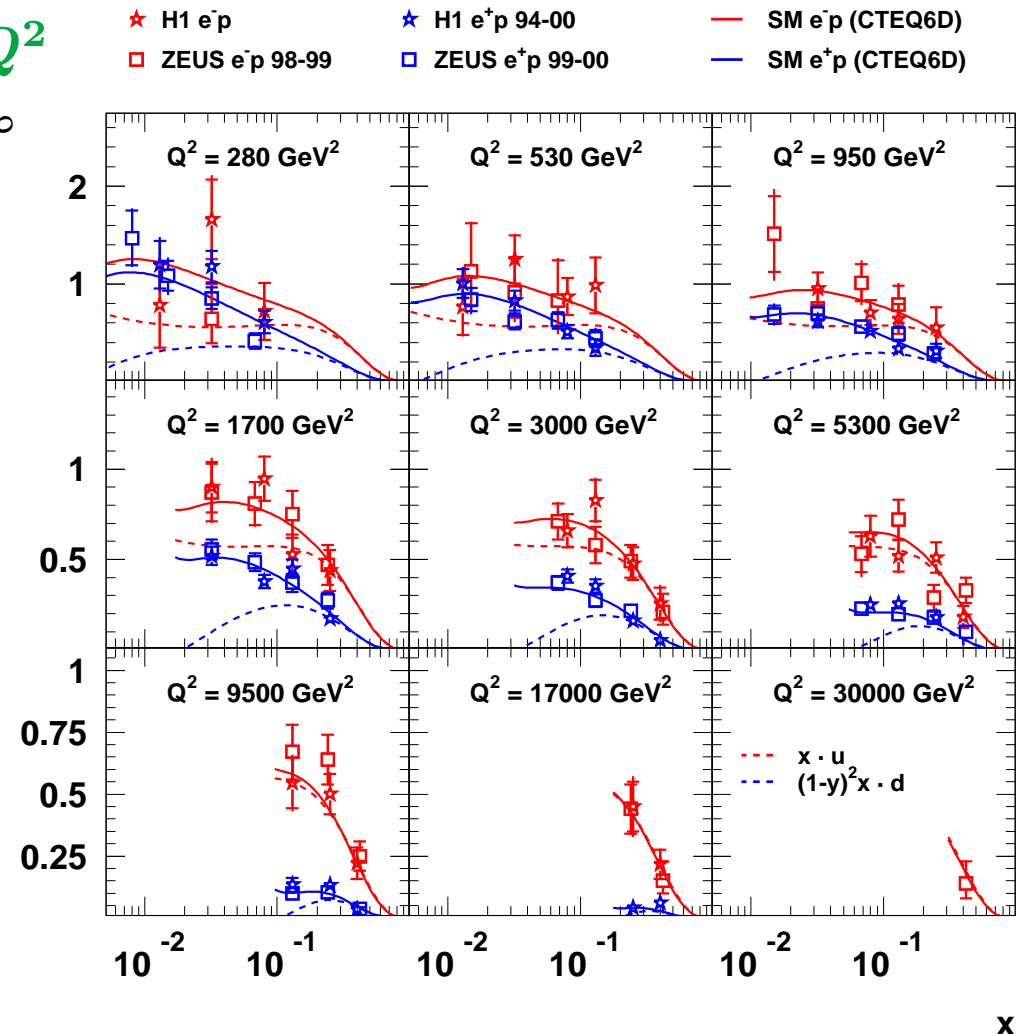
→ Sensitivity to valence quarks

$$\tilde{\sigma}(e^+p) \rightarrow x(1-y)^2 d_V \text{ (high-}x\text{)}$$

$$\tilde{\sigma}(e^-p) \rightarrow xu_V \text{ (high-}x\text{)}$$

⇒ In combination with the reduced NC cross section at large Q^2 and high x

HERA Charged Current



Neutral Current Deep Inelastic e^+p and e^-p Scattering at high x

- Measurements of the reduced cross section in CC DIS:

$$\tilde{\sigma}(e^\pm p) = (G_F^2 \eta_W^2 / 2\pi x)^{-1} d\sigma_{\text{Born}} / dx dQ^2$$

→ Sensitivity to flavour composition

$$\tilde{\sigma}(e^+p) = x(\bar{u} + \bar{c} + (1-y)^2(d + s))$$

$$\tilde{\sigma}(e^-p) = x(u + c + (1-y)^2(\bar{d} + \bar{s}))$$

→ Sensitivity to valence quarks

$$\tilde{\sigma}(e^+p) \rightarrow x(1-y)^2 d_V \text{ (high-}x\text{)}$$

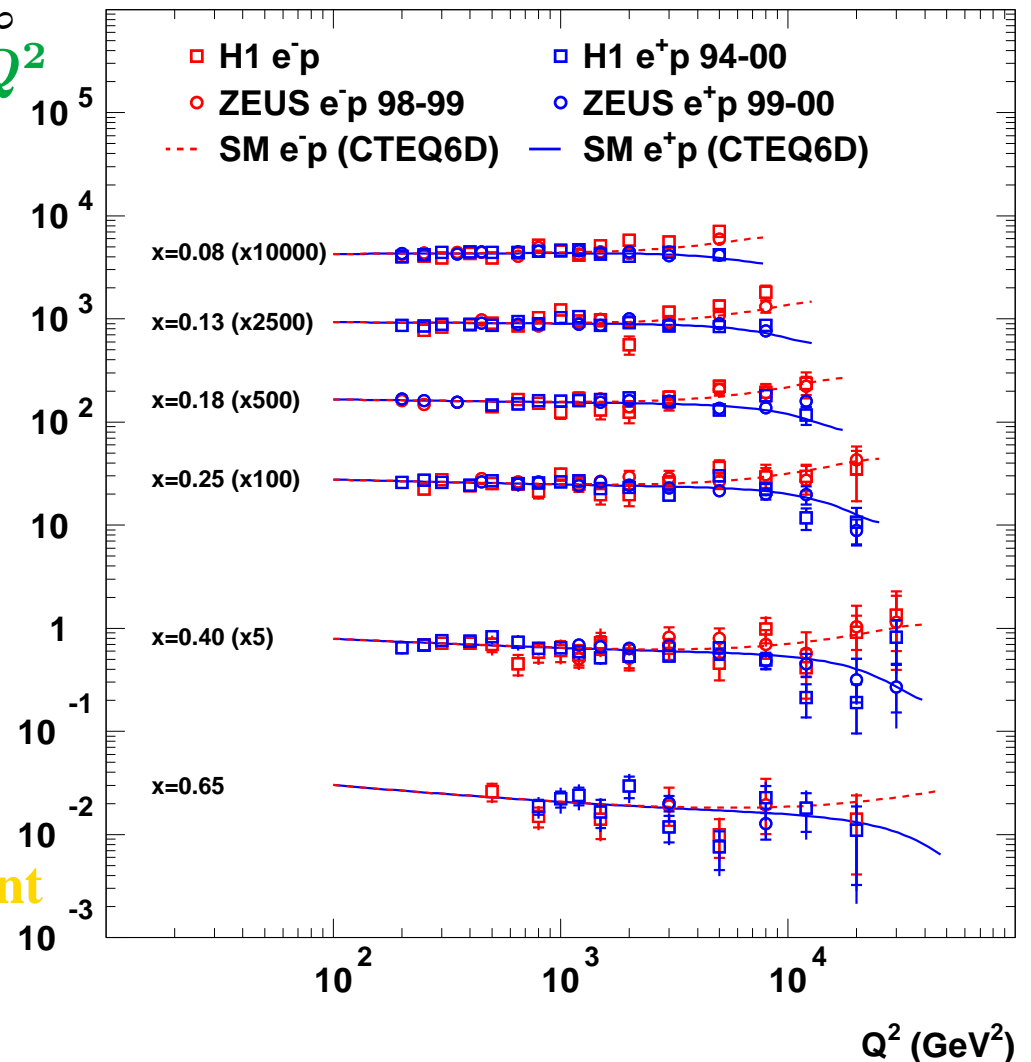
$$\tilde{\sigma}(e^-p) \rightarrow xu_V \text{ (high-}x\text{)}$$

⇒ In combination with the reduced NC cross section at large Q^2 and high x provide sufficient sensitivity to determine the proton PDFs within a single experiment

→ free from nuclear corrections

→ free from higher-twists effects

HERA Neutral Current at high x



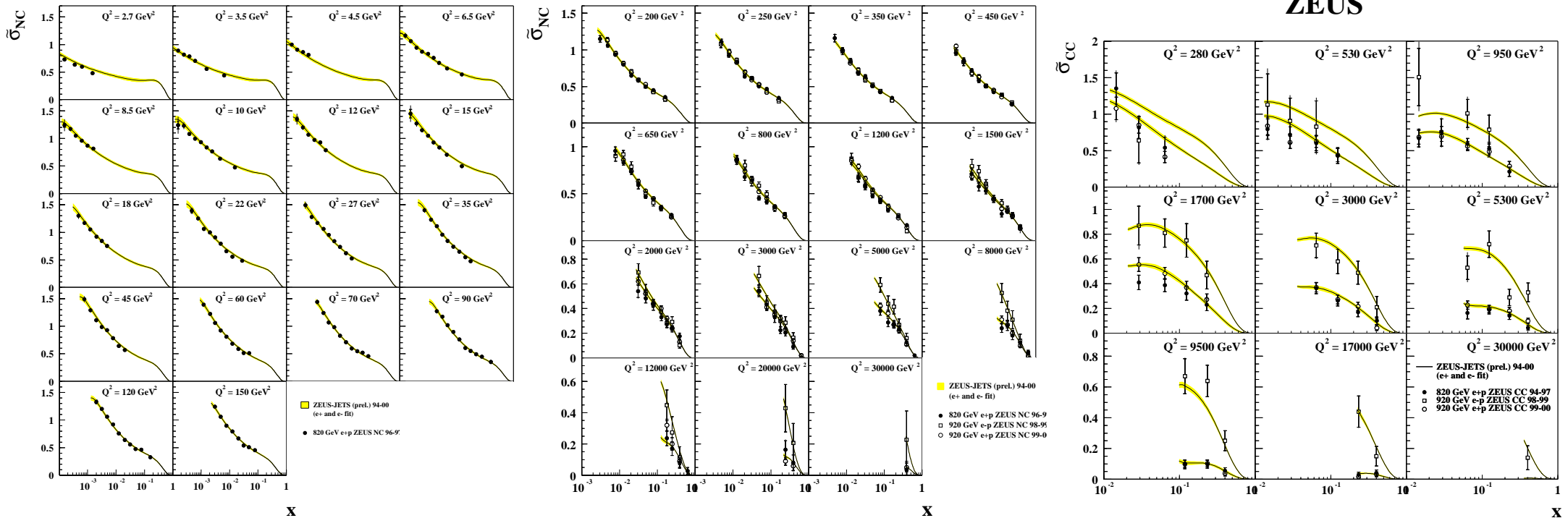
Structure Functions (Continued)

Determination of the Proton PDFs with ZEUS data alone

ZEUS NC DIS low Q^2

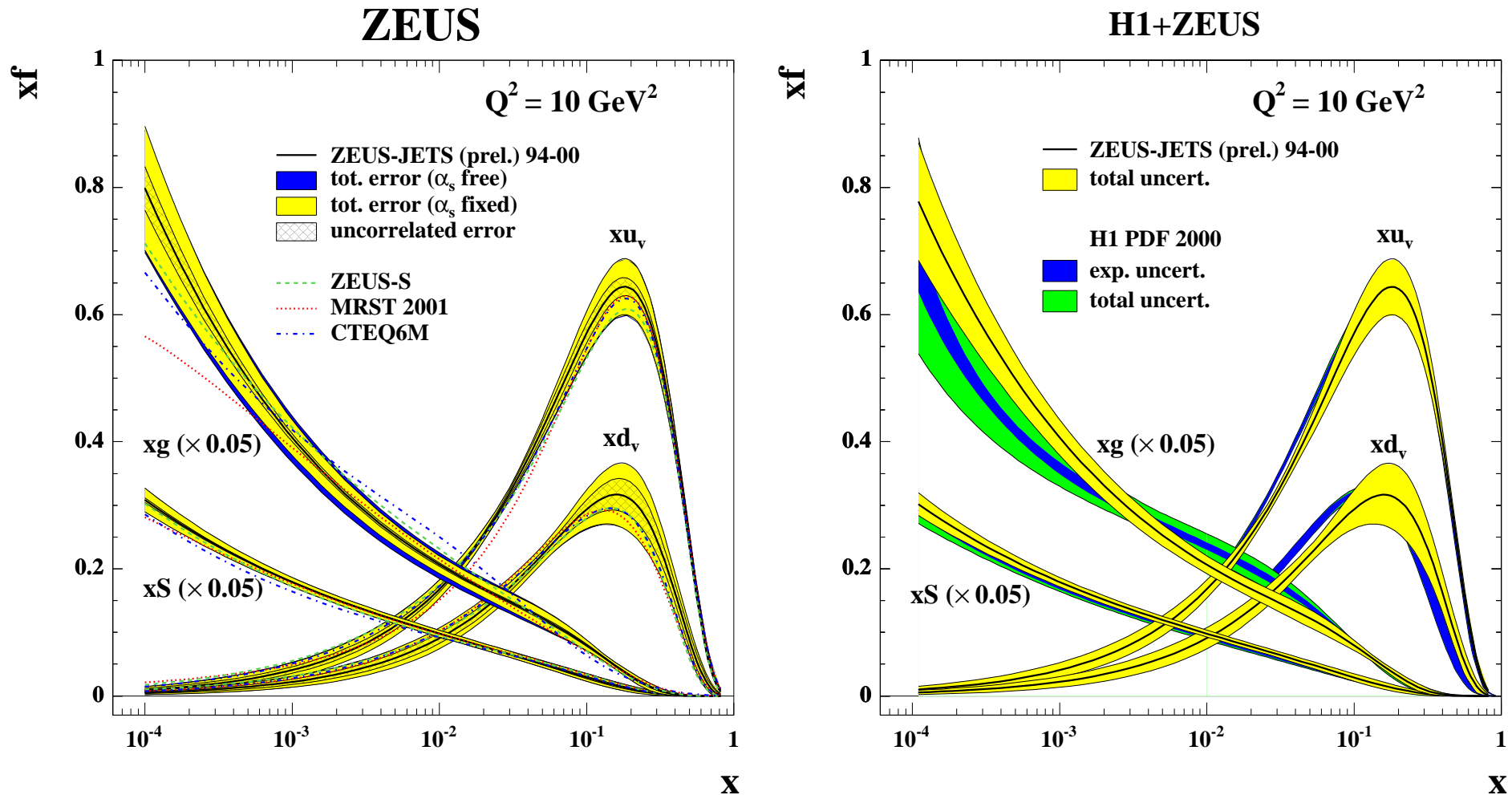
ZEUS NC DIS high Q^2

CC DIS high Q^2 ZEUS



- Fit of **ZEUS-only** data: **NC DIS $e^\pm p$** and **CC DIS $e^\pm p$** in the region $2.5 < Q^2 < 30000 \text{ GeV}^2$, $6.3 \cdot 10^{-5} < x < 0.65$ and $W^2 > 20 \text{ GeV}^2$ using **DGLAP** evolution equations at **NLO**: $\rightarrow xu_V, xd_V, xS, xg$ (no HERA information on flavour composition of the sea: flavour-averaged sea)
 \Rightarrow **Good description of Structure Function data (577 data points)**

Determination of the Proton PDFs with HERA data alone



⇒ HERA determination of proton PDFs in agreement with global fits (CTEQ, MRST)

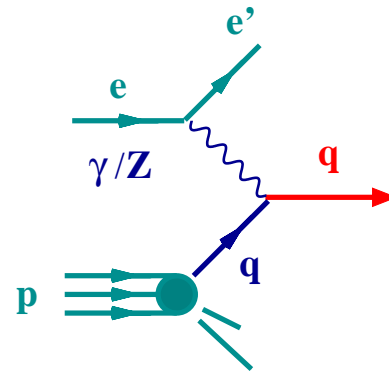
HERA-I data: $\mathcal{L}(e^+p) \approx 110 \text{ pb}^{-1}$ and $\mathcal{L}(e^-p) \approx 15 \text{ pb}^{-1}$

→ room for improvement from HERA-II data

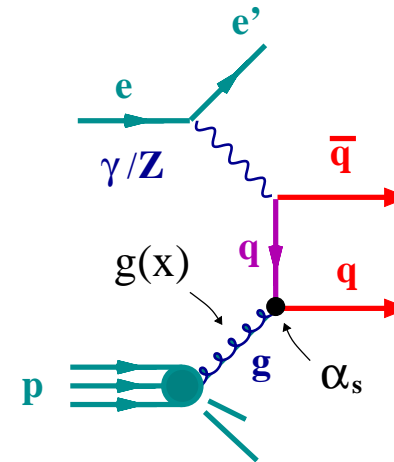
Jets and α_s

Jet Production in Neutral Current Deep Inelastic Scattering

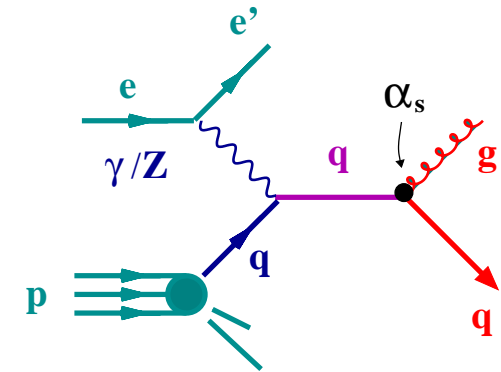
- Jet production in neutral current deep inelastic scattering up to $\mathcal{O}(\alpha_s)$:



Quark-Parton Model



Boson-Gluon Fusion



QCD Compton

- Perturbative QCD calculations of jet cross sections:

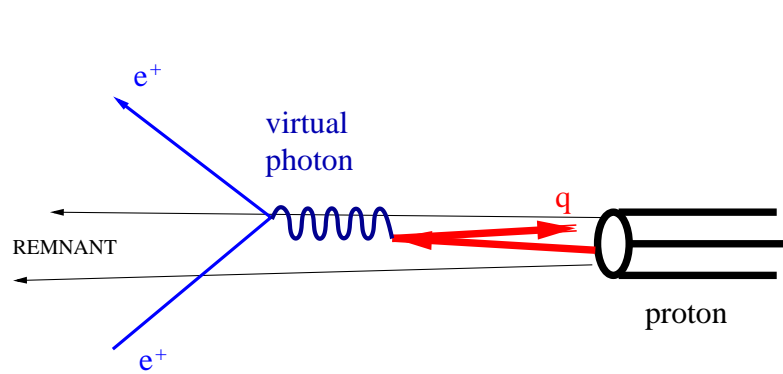
$$\sigma_{jet} = \sum_{a=q,\bar{q},g} \int dx f_a(x, \mu_F^2) \hat{\sigma}_a(x, \alpha_s(\mu_R), \mu_R^2, \mu_F^2)$$

- f_a : parton a density in the proton, determined from experiment; **long-distance structure of the target**
- $\hat{\sigma}_a$: subprocess cross section, calculable in pQCD; **short-distance structure of the interaction**

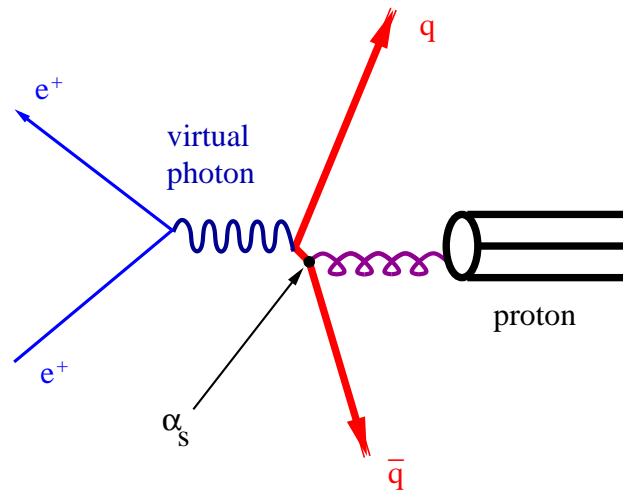
Jet Production in Neutral Current Deep Inelastic Scattering

- In the region where the wealth of data from fixed-target and collider experiments has allowed **an accurate determination of the proton PDFs**, **measurements of jet production in NC DIS provide**
 - a sensitive test of the pQCD predictions of the short-distance structure
 - a determination of the strong coupling constant α_s
- To perform a **stringent test of the pQCD predictions** and a **precise determination of α_s** :
 - * **Observables for which the predictions are directly proportional to α_s**
 - Jet cross sections in the Breit frame
 - * **Small experimental uncertainties** → Jets with relatively high transverse energy
 - * **Small theoretical uncertainties** → NLO QCD calculations
 - **Jet algorithm: longitudinally invariant k_T cluster algorithm** (Catani et al)
(small parton-to-hadron effects, infrared safe, suppression of beam-remnant jet)
 - Jet selection criteria
- Exploration of the parton evolution at low x \Rightarrow footprints of BFKL effects?
- Exploration of the low Q^2 (transition) region \Rightarrow resolved virtual photons?

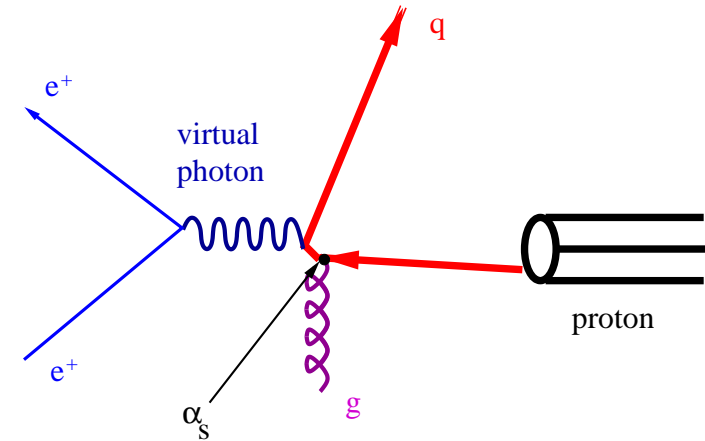
High- E_T Jet Production in the Breit Frame



BORN PROCESS



BOSON-GLUON FUSION



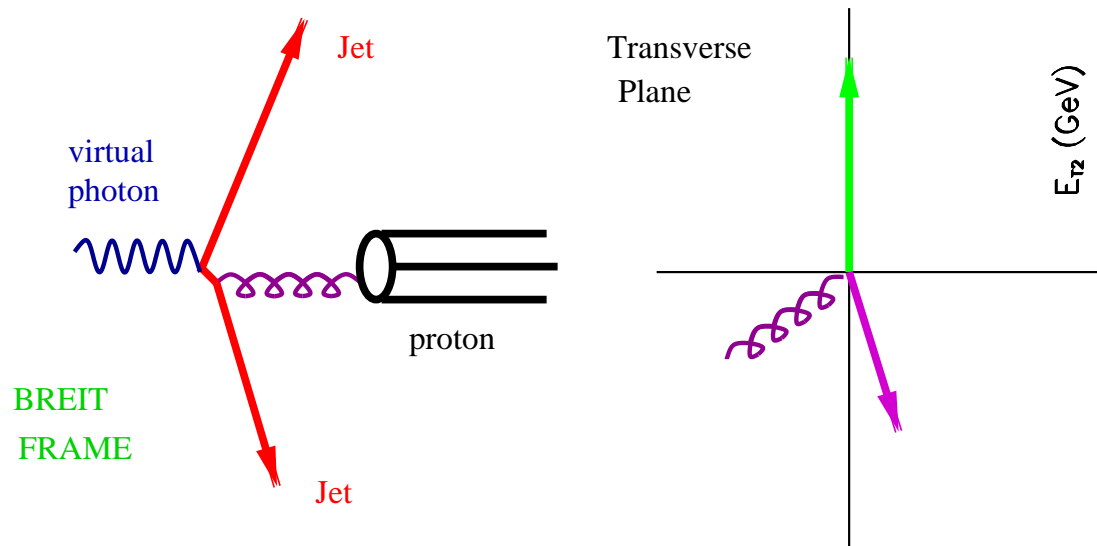
OCD COMPTON

- In the Breit frame the virtual boson collides head-on with the proton
- High- E_T jet production in the Breit frame
 - suppression of the Born contribution (struck quark has zero E_T)
 - suppression of the beam-remnant jet (zero E_T)
 - lowest-order non-trivial contributions from $\gamma^* g \rightarrow q\bar{q}$ and $\gamma^* q \rightarrow qg$
 - ⇒ directly sensitive to hard QCD processes (α_s)

NLO QCD Calculations of Jet Cross Sections in DIS

- **Several NLO QCD programs are available for performing jet cross section calculations** → **DISENT** (Catani and Seymour), **MEPJET** (Mirkes and Zeppenfeld), **DISASTER++** (Graudenz), **NLOJET** (Nagy and Trocsanyi)
- **NLO corrections** → **virtual corrections with internal particle loops**
→ **real corrections with a third parton in the final state**
- **Different methods to calculate real corrections:**
→ **phase space slicing method (M), subtraction method (D, D++, NJ)**
- **Since there are two hard scales in jet production, the renormalisation and factorisation scales can be chosen as one of the two, $\mu_R, \mu_F = Q$ or E_T^{jet}**
- **The calculations are for jets of partons and the measurements are done at the hadron level** → **need to correct the calculations for hadronisation effects**
- **Theoretical uncertainties:**
→ **terms beyond NLO, which are usually estimated by varying μ_R by factor 2**
→ **uncertainties on $\alpha_s(M_Z)$ and the proton PDFs**
→ **uncertainty coming from the hadronisation corrections**

Jet Finding and Selection Criteria for Dijet Events



- Longitudinally invariant k_T -cluster algorithm in the η - ϕ plane of Breit frame

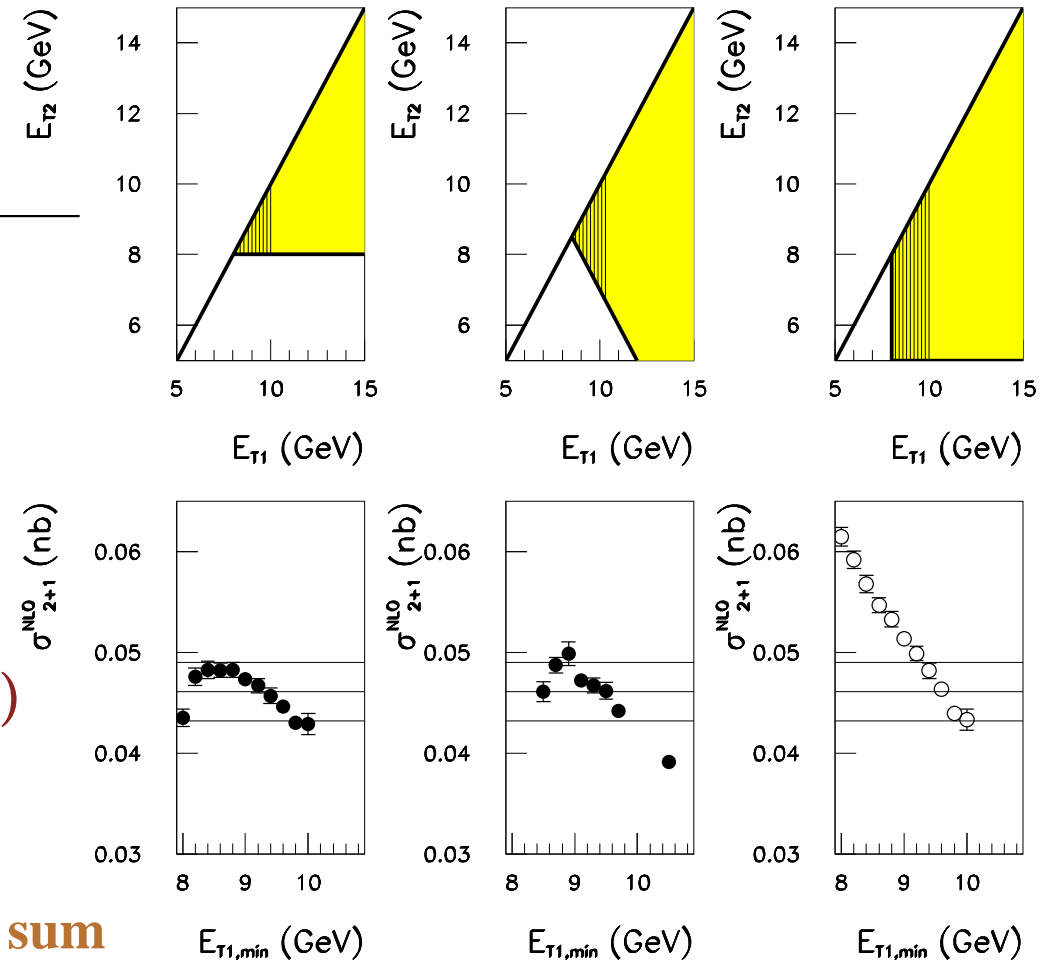
$$d_{ij} = \min(E_{T,i}^2, E_{T,j}^2) \cdot (\Delta\eta_{ij}^2 + \Delta\phi_{ij}^2)$$

- Dijet selection criteria:

- Symmetric cuts on $E_T^{jet,1(2)} \Rightarrow$ danger
- Symmetric cuts on $E_T^{jet,1(2)}$ and cut on sum
- Asymmetric cuts on $E_T^{jet,1(2)}$

\Rightarrow NLO calculations for dijet cross sections can be (infrared) sensitive to the selection criteria

NLO QCD Dijet Cross Section ($\mu_R=Q$) $Q^2 > 470 \text{ GeV}^2$



Dijet Cross Sections in NC DIS ($5 < Q^2 < 15000 \text{ GeV}^2$)

- **Measurement of differential dijet cross sections over a wide range in $Q^2 \rightarrow 5 < Q^2 < 15000 \text{ GeV}^2$ and $0.2 < y < 0.6$ for dijet production with**

$$E_T^{jet,1(2)}(\text{Breit}) > 5 \text{ GeV}$$

$$E_T^{jet,1}(\text{Breit}) + E_T^{jet,2}(\text{Breit}) > 17 \text{ GeV}$$

$$-1 < \eta^{jet,1(2)}(\text{Lab}) < 2.5$$

- **Detailed investigation of the jet algorithms:**

→ **Smallest parton-to-hadron effects: inclusive k_T**

- **Comparison with NLO QCD calculations:**

→ $\mu_R = \bar{E}_T, \mu_F = \sqrt{200} \text{ GeV}$

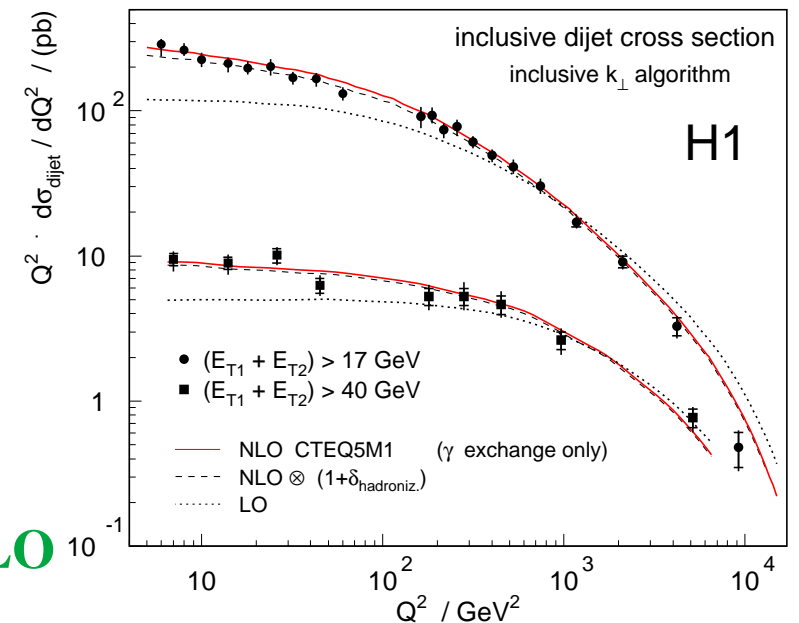
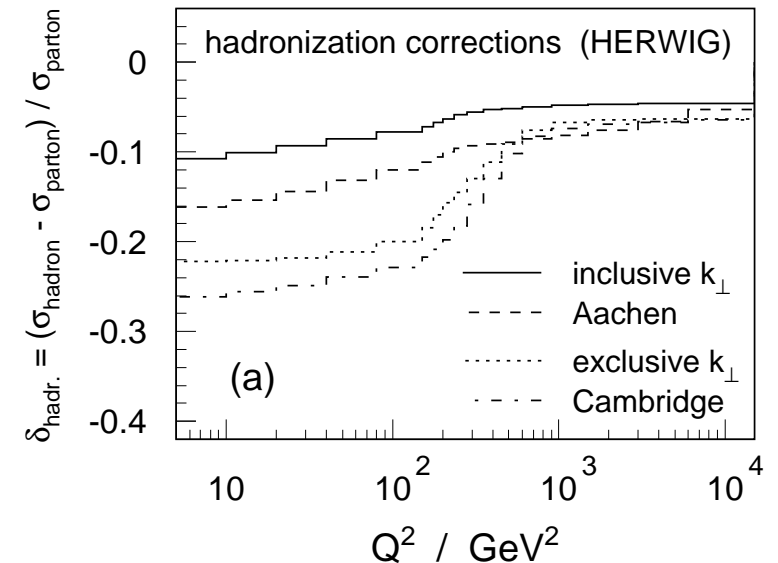
→ **CTEQ5M1 parametrisations of proton PDFs**

→ **parton-to-hadron corrections applied**

- **NLO QCD gives a good description of the data over**

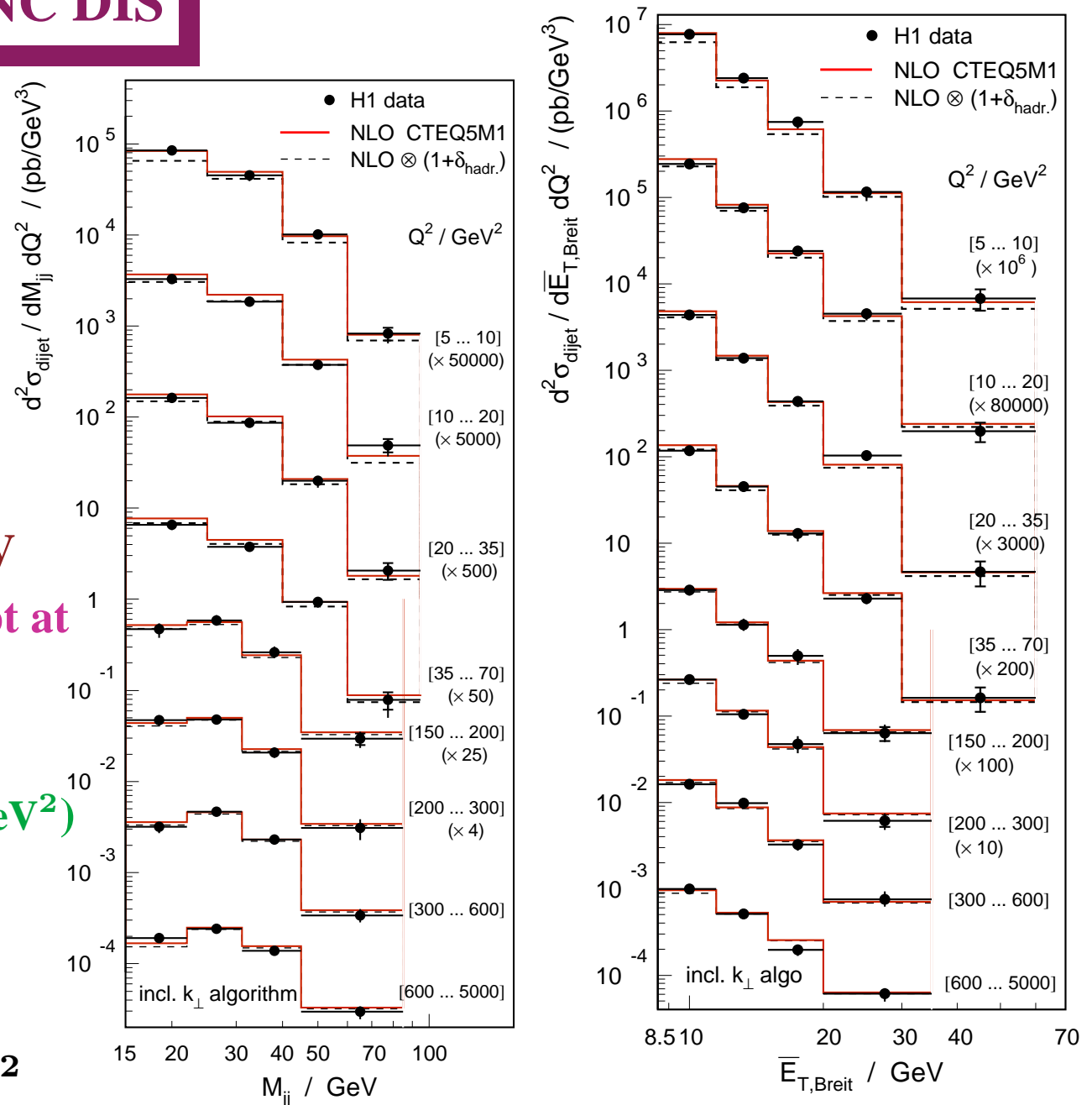
a wide range in Q^2 and E_T ; the Q^2 dependence is

observed to be reduced at high- E_T and described by NLO



Dijet Cross Sections in NC DIS

- **Measurement of double differential cross sections**
 $d\sigma/dM_{JJ}dQ^2$, $d\sigma/d\bar{E}_T dQ^2$
 over $5 < Q^2 < 5000 \text{ GeV}^2$
- It is observed that the spectra get harder as Q^2 increases
- **NLO QCD describes well the data over $15 < M_{JJ} < 95 \text{ GeV}$ and $8.5 < \bar{E}_T < 60 \text{ GeV}$ except at low Q^2 , where the shape is ok but not the normalisation**
- **Overview: at high $Q^2 (> 70 \text{ GeV}^2)$ NLO describes the data well; as Q^2 decreases the theoretical uncertainties become large and NLO fails for $Q^2 < 10 \text{ GeV}^2$**

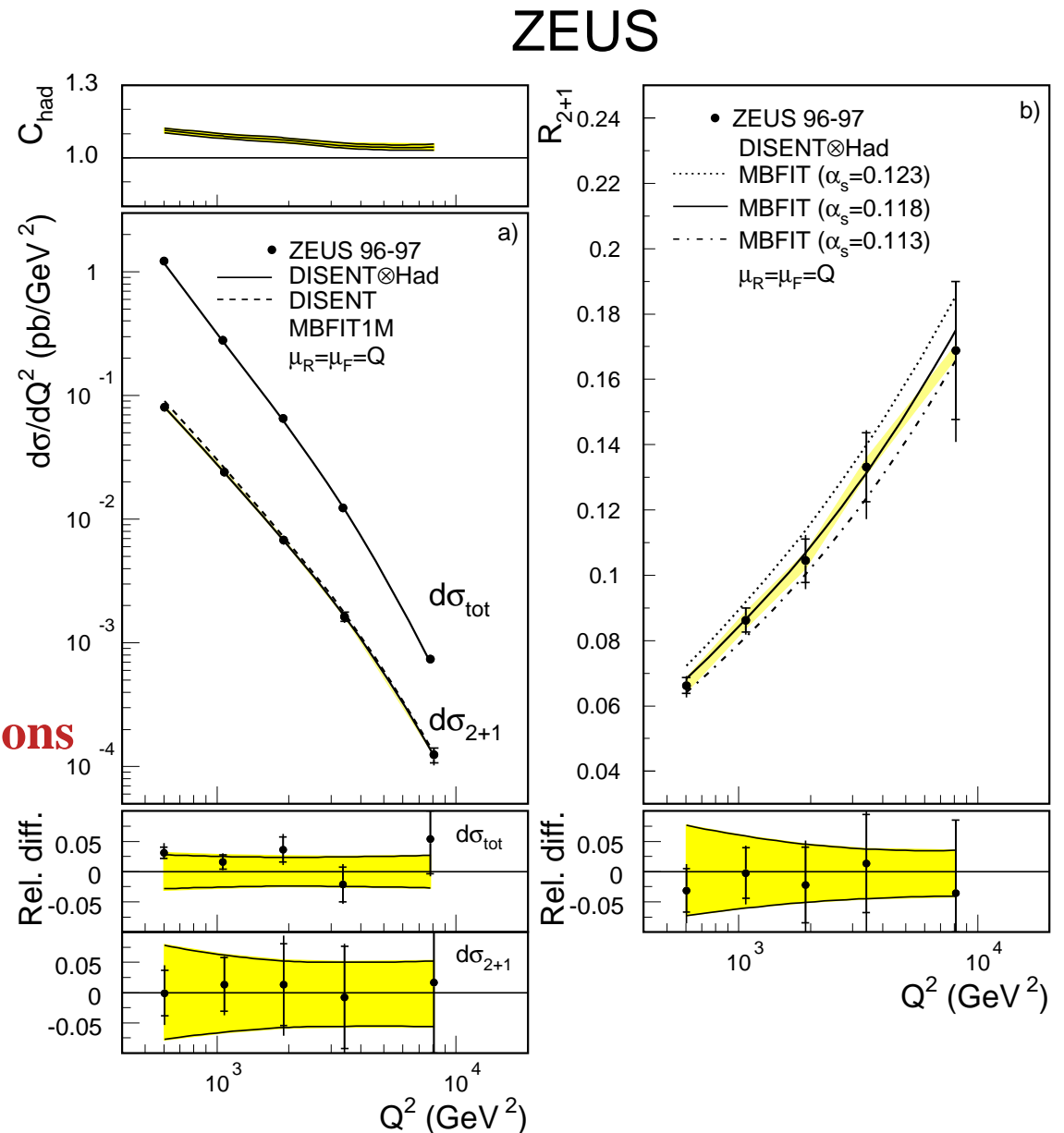


Dijet Cross Sections at $Q^2 > 470 \text{ GeV}^2$ and extraction of α_s

- Dijet cross section $d\sigma_{2+1}/dQ^2$ for $470 < Q^2 < 20000 \text{ GeV}^2$
 $E_T^{jet,1}(\text{Breit}) > 8 \text{ GeV}$
 $E_T^{jet,2}(\text{Breit}) > 5 \text{ GeV}$
 $-1 < \eta^{jet,1(2)}(\text{Lab}) < 2$

→ **Ratio** $R_{2+1} \equiv \frac{d\sigma_{2+1}/dQ^2}{d\sigma_{tot}/dQ^2}$

- Small experimental uncertainties.
- Comparison with NLO QCD calculations
- Small theoretical uncertainties:
 - uncertainties on the proton PDFs
 - hadronisation corrections
 - higher-order terms ($> \text{NLO}$)



Dijet Cross Sections at $Q^2 > 470 \text{ GeV}^2$

- Measurement of dijet differential cross section as a function of

$$z_{p,1} = \frac{(E - p_z)_{\text{jet},1}}{\sum_{k=1,2} (E - p_z)_{\text{jet},k}} \simeq \frac{1}{2} \cdot (1 - \cos \theta^*)$$

θ^* is the scattering angle in the γ^* -parton CMS

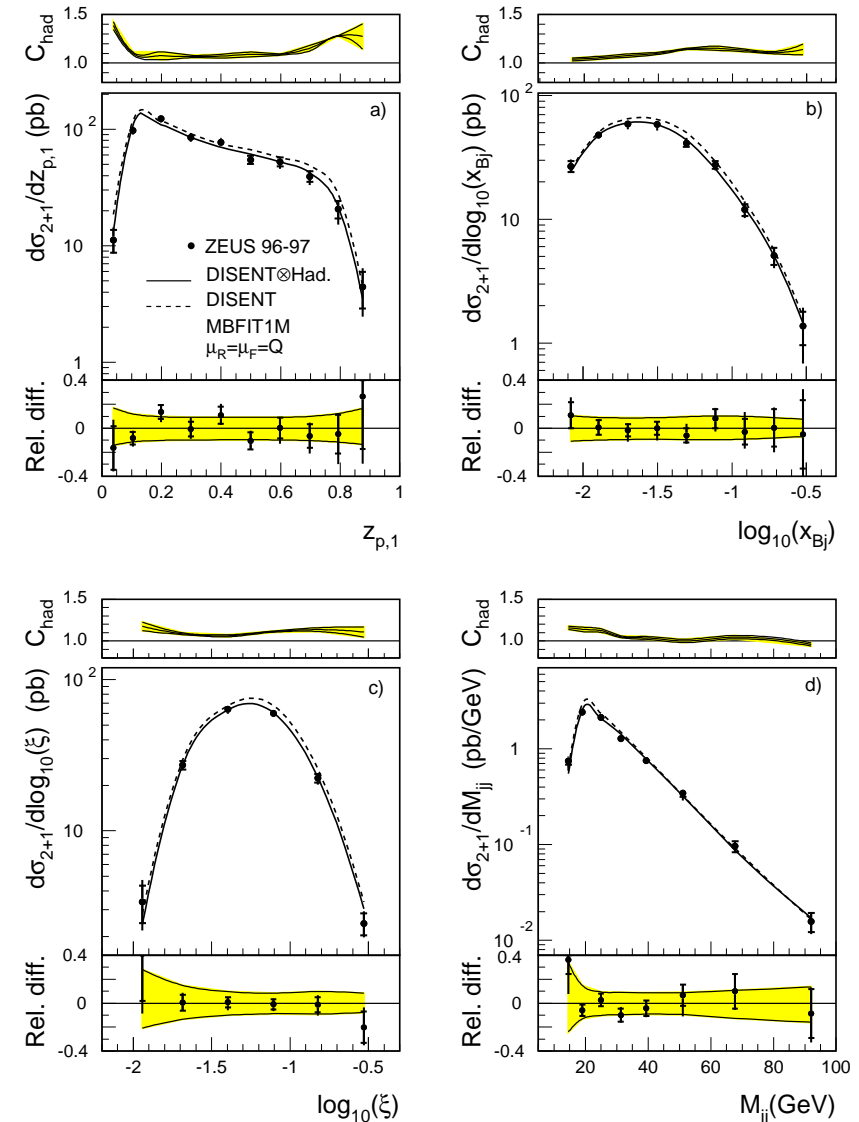
x_{Bj} = Bjorken's x variable

ξ = fraction of proton momentum carried by incoming parton, $\xi = x_{Bj} \cdot (1 + M_{jj}^2/Q^2)$

M_{jj} = dijet invariant mass

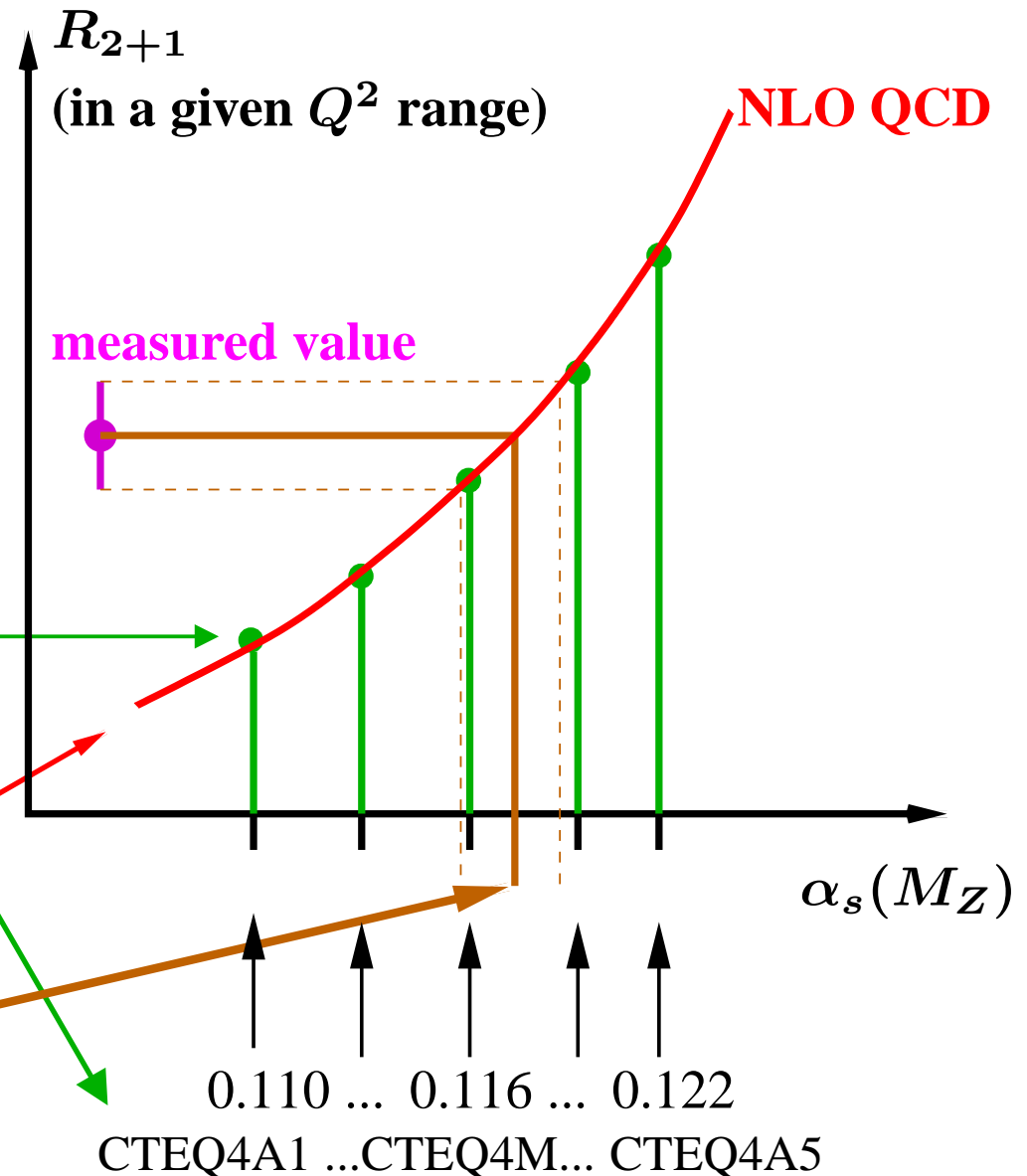
- NLO QCD calculations provide a good description of the data
→ validity of the description of the dynamics of dijet production by pQCD at $\mathcal{O}(\alpha_s^2)$

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Dijet Cross Sections at $Q^2 > 470 \text{ GeV}^2$ and extraction of $\alpha_s(M_Z)$

- **NLO QCD calculations of $d\sigma_{2+1}/dQ^2$ depend on $\alpha_s(M_Z)$ through**
 - **Matrix Elements:** $\hat{\sigma} \sim A \cdot \alpha_s + B \cdot \alpha_s^2$
 - **proton PDFs:** α_s assumed in evolution
- **To take into account the correlation the NLO QCD calculations are performed using various sets of proton PDFs which assume different values of α_s**
- **The resulting NLO QCD calculations are parametrised as a function of $\alpha_s(M_Z)$ in each region of Q^2 of the measurements**
- **From the measured value of R_{2+1} in each region of Q^2 the value of $\alpha_s(M_Z)$ and its uncertainty are extracted**



Dijet Cross Sections at $Q^2 > 470 \text{ GeV}^2$ and extraction of α_s

- Study of the scale dependence of $\alpha_s(Q)$:
from the measured $R_{2+1}(Q^2)$ in each Q^2 region
→ $\alpha_s(\langle Q \rangle)$ is extracted
The measurements are consistent with
the running of α_s predicted by perturbative QCD
- A combined value of $\alpha_s(M_Z)$ has been extracted:

$$\alpha_s(M_Z) = 0.1166 \pm 0.0019 \text{ (stat.)}$$

$$+0.0024 \text{ (exp.)} +0.0057 \text{ (th.)}$$

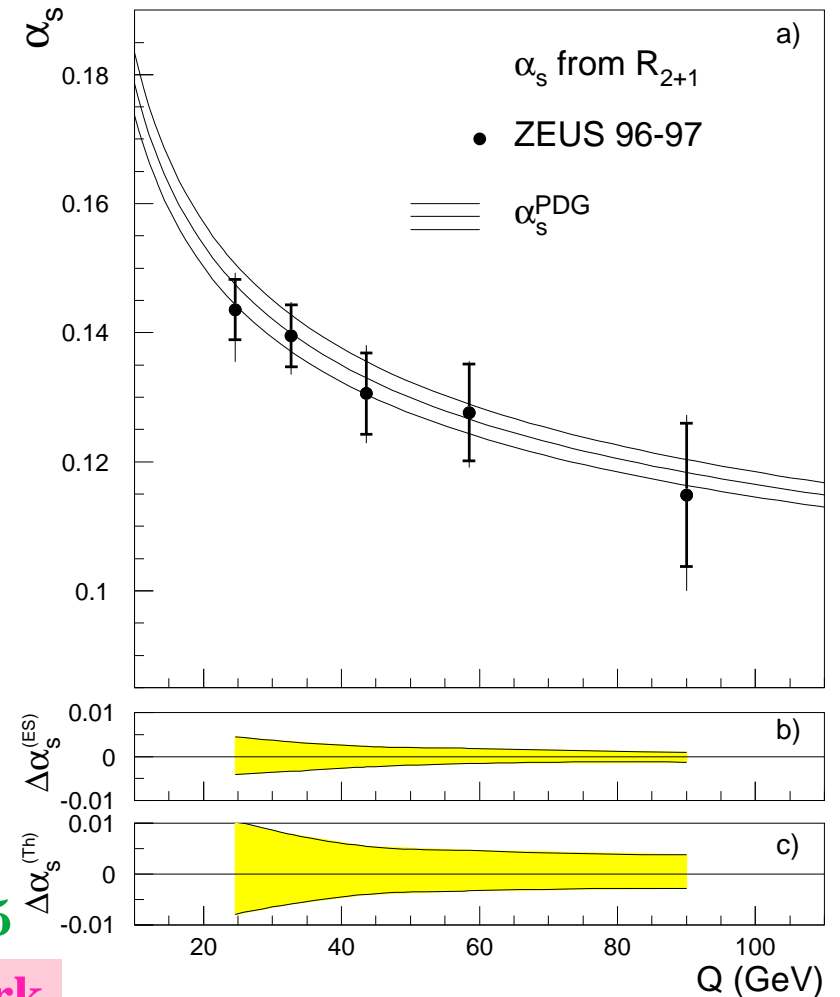
$$-0.0033 \text{ (exp.)} -0.0044 \text{ (th.)}$$

- The theoretical uncertainty dominates:

- terms beyond NLO $\Delta\alpha_s(M_Z) = \begin{matrix} +0.0055 \\ -0.0042 \end{matrix}$
- uncertainties proton PDFs $\Delta\alpha_s(M_Z) = \begin{matrix} +0.0012 \\ -0.0011 \end{matrix}$
- hadronisation corrections $\Delta\alpha_s(M_Z) = \pm 0.0005$

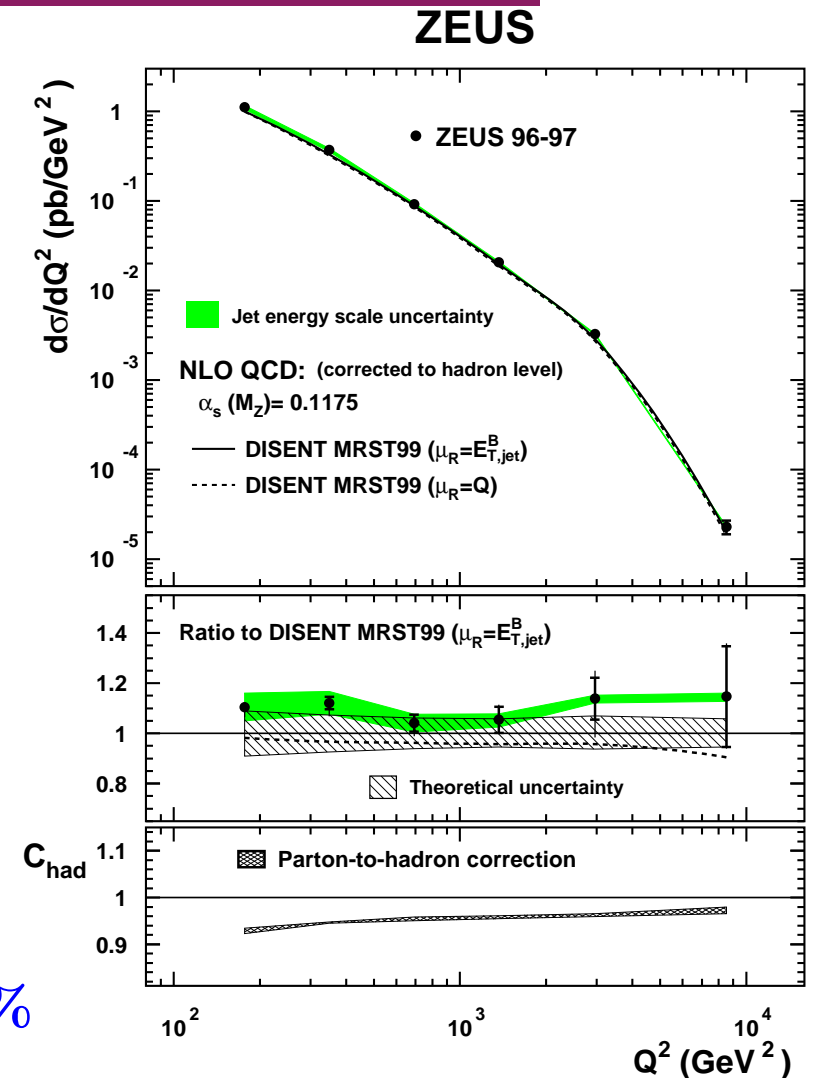
Improvements depend upon further Theoretical Work

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Inclusive Jet Cross Sections in NC DIS at $Q^2 > 125 \text{ GeV}^2$

- Measurement of inclusive jet cross sections in the kinematic region defined by $Q^2 > 125 \text{ GeV}^2$ and $-0.7 < \cos \gamma < 0.5$ for jets with $E_{T,jet}^B > 8 \text{ GeV}$ and $-2 < \eta_{jet}^B < 1.8$
 - no cut is applied in the laboratory frame
- Advantages:
 - infrared insensitivity (no dijet cuts!)
 - suited to test resummed calculations
 - smaller theoretical uncertainties than for dijet
- Small experimental uncertainties:
 - jet energy scale (1% for $E_{T,jet} > 10 \text{ GeV}$)
 - ⇒ $\sim \pm 5\%$ on the cross sections
- Small parton-to-hadron corrections (C_{had}): $< 10\%$
- NLO QCD calculations ($\mathcal{O}(\alpha_s^2)$) using $\mu_R = E_{T,jet}^B$, $\mu_F = Q$ and the MRST99 parametrisations of the proton PDFs describe the measurements well



Inclusive Jet Cross Sections in NC DIS at $Q^2 > 125 \text{ GeV}^2$

- Measurement of the inclusive jet cross section

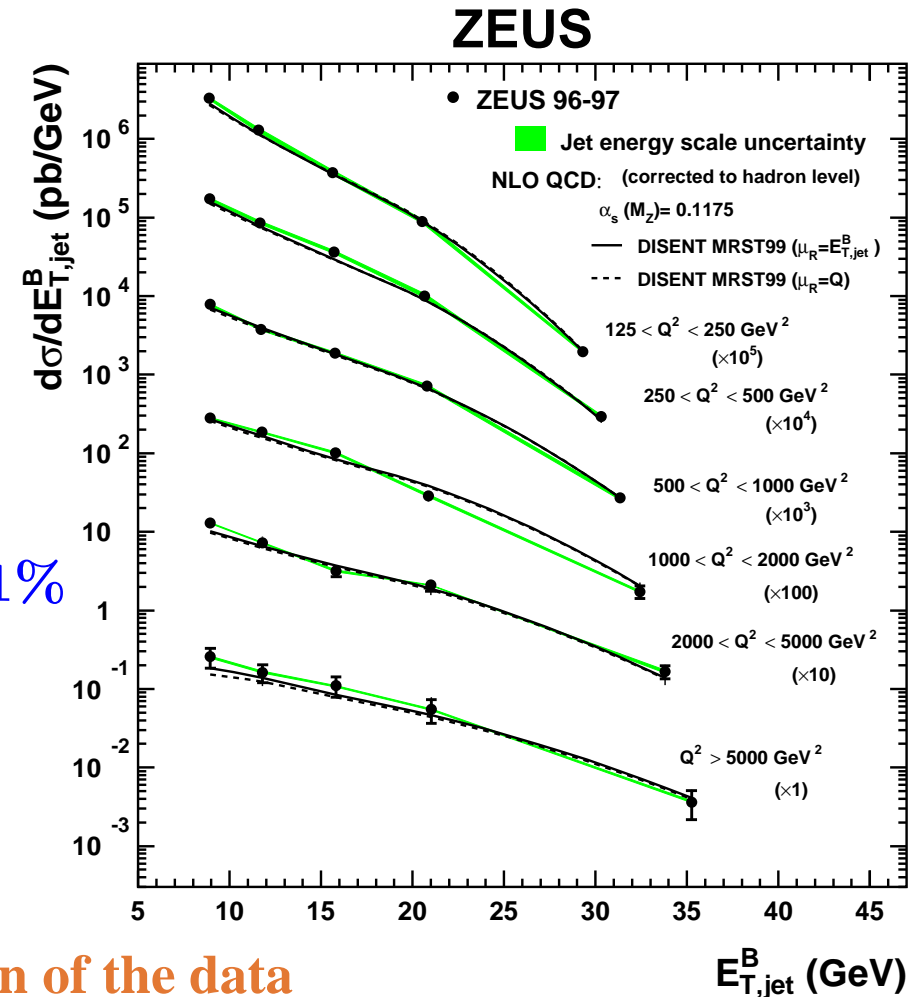
$d\sigma/dE_{T,jet}^B$ in different regions of Q^2

- Small theoretical uncertainties:

- higher-order terms ($> \text{NLO}$); varying μ_R between $\frac{1}{2} \cdot E_{T,jet}^B$ and $2 \cdot E_{T,jet}^B \Rightarrow \pm 5\%$
- uncertainty on $\alpha_s(M_Z)$ (± 0.003); $\Rightarrow \pm 5\%$
- hadronisation corrections; variance of C_{had} values (ARIADNE, LEPTO, HERWIG) $\Rightarrow < 1\%$
- uncertainties on the proton PDFs
 - experimental uncertainties $\Rightarrow \pm 3\%$
 - theoretical assumptions $\Rightarrow \pm 3\%$

- NLO QCD calculations provide a good description of the data

- validity of the description of the dynamics of inclusive jet production by pQCD at $\mathcal{O}(\alpha_s^2)$



Inclusive Jet Cross Sections and extraction of α_s

- The inclusive jet cross section $d\sigma/dQ^2$ at $Q^2 > 500 \text{ GeV}^2$ has been used to extract $\alpha_s(M_Z)$

$$\alpha_s(M_Z) = 0.1212 \pm 0.0017 \text{ (stat.)}$$

$$+0.0023 \text{ (exp.) } +0.0028 \text{ (th.)}$$

$$-0.0031 \text{ (exp.) } -0.0027 \text{ (th.)}$$

- Experimental uncertainties:

→ jet energy scale (1% for $E_{T,jet} > 10 \text{ GeV}$)

- Theoretical uncertainties:

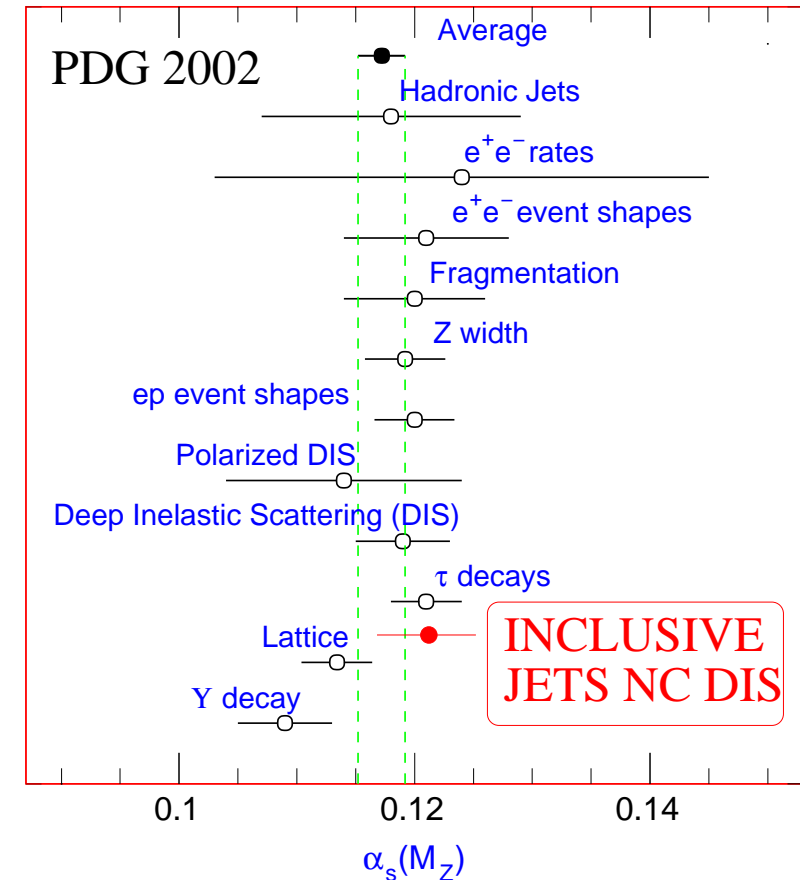
→ terms beyond NLO $\Delta\alpha_s(M_Z) = 3\%$

→ uncertainties proton PDFs $\Delta\alpha_s(M_Z) = 1\%$

→ hadronisation corrections $\Delta\alpha_s(M_Z) = 0.2\%$

- Consistent with other determinations of α_s and PDG

- Very precise determination of $\alpha_s(M_Z)$!



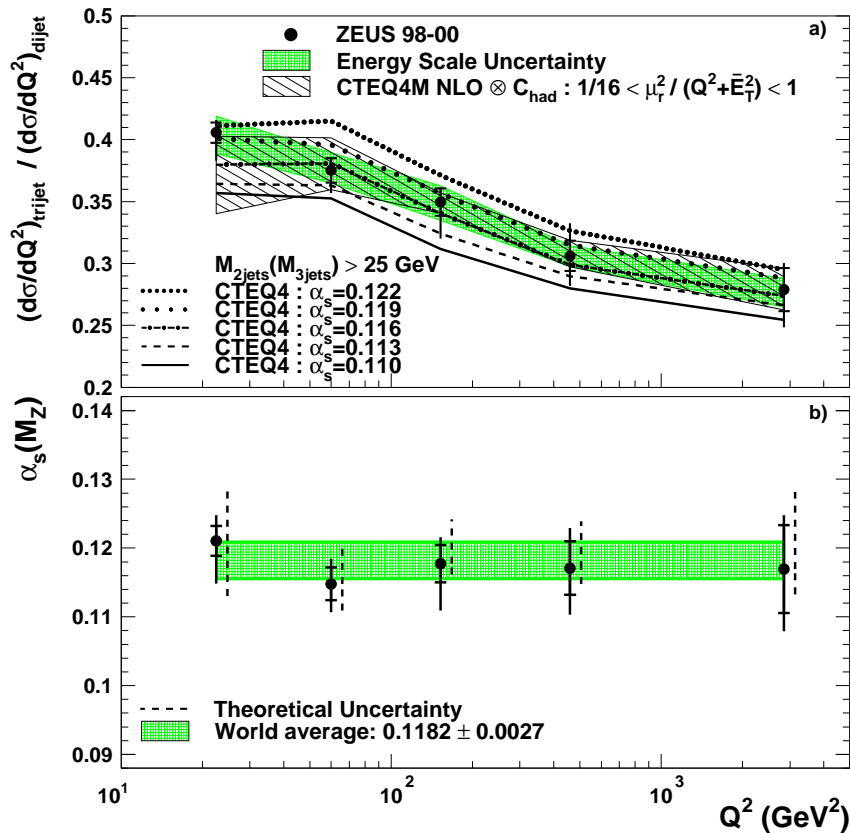
Further improvement depends upon further Experimental and Theoretical Work

Three-jet cross sections in NC DIS

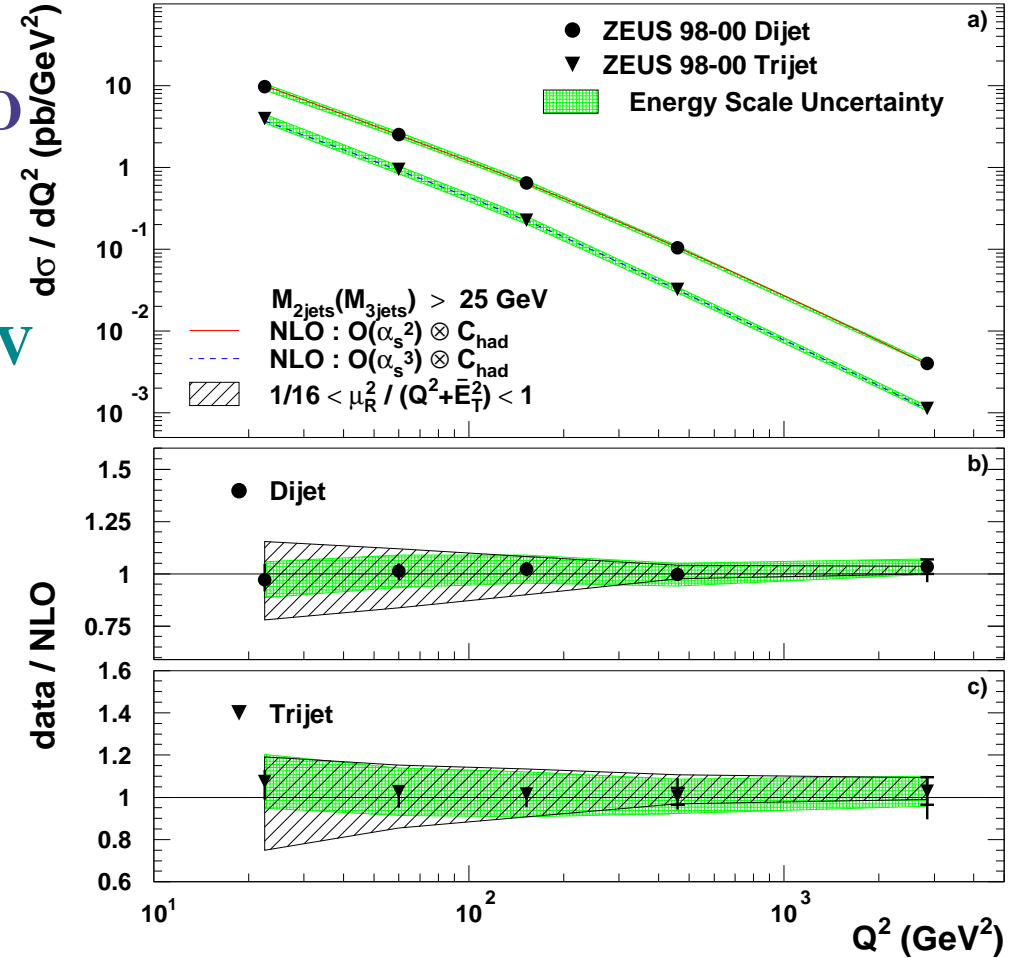
• Three-jet cross sections test QCD beyond LO directly $\rightarrow \sigma_{3jet} \propto \alpha_s^2$

• At least three jets with $E_T^{jet}(\text{Breit}) > 5 \text{ GeV}$ and $-1 < \eta^{jet}(\text{Lab}) < 2.5, M_{3jets} > 25 \text{ GeV}$

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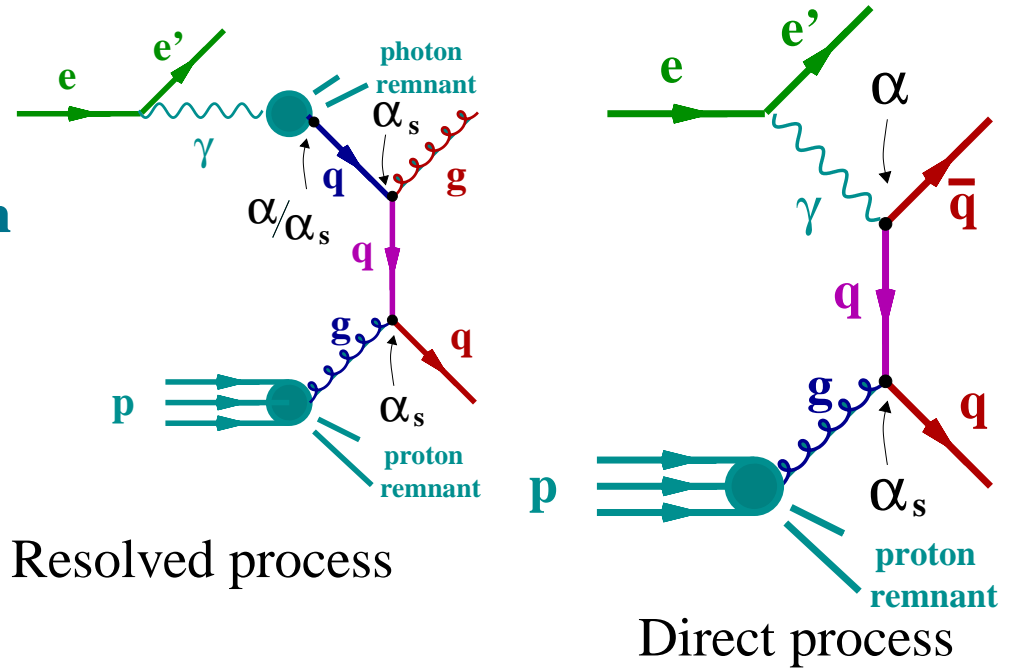


\rightarrow NLO calculations ($\mathcal{O}(\alpha_s^3)$): good description of the data over the whole range $10 < Q^2 < 5000 \text{ GeV}^2$

$\rightarrow \alpha_s(M_Z) = 0.1179 \pm 0.0013$ (stat.)^{+0.0028}_{-0.0046} (exp.)^{+0.0064}_{-0.0046} (th.)

Photoproduction of Jets

- Production of jets in γp collisions has been measured via ep scattering at $Q^2 \approx 0$
- At lowest order QCD, two hard scattering processes contribute to jet production \Rightarrow
- pQCD calculations of jet cross sections



$$\sigma_{jet} = \sum_{a,b} \int_0^1 dy f_{\gamma/e}(y) \int_0^1 dx_\gamma f_{a/\gamma}(x_\gamma, \mu_{F\gamma}^2) \int_0^1 dx_p f_{b/p}(x_p, \mu_{Fp}^2) \hat{\sigma}_{ab \rightarrow jj}$$

longitudinal momentum fraction of γ/e^+ (y), **parton a/γ** (x_γ), **parton b/proton** (x_p)

$\rightarrow f_{\gamma/e}(y)$ = flux of photons in the positron (WW approximation)

$\rightarrow f_{a/\gamma}(x_\gamma, \mu_{F\gamma}^2)$ = **parton densities in the photon** (for direct processes $\delta(1 - x_\gamma)$)

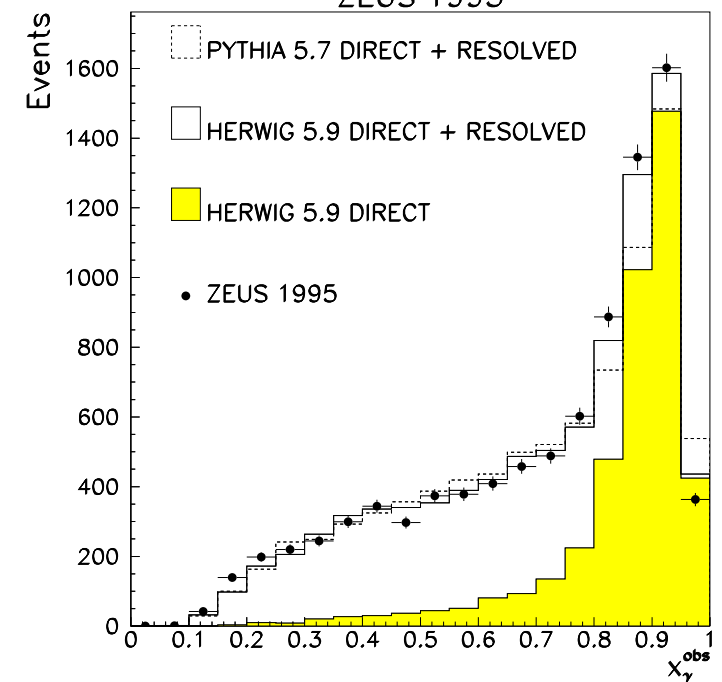
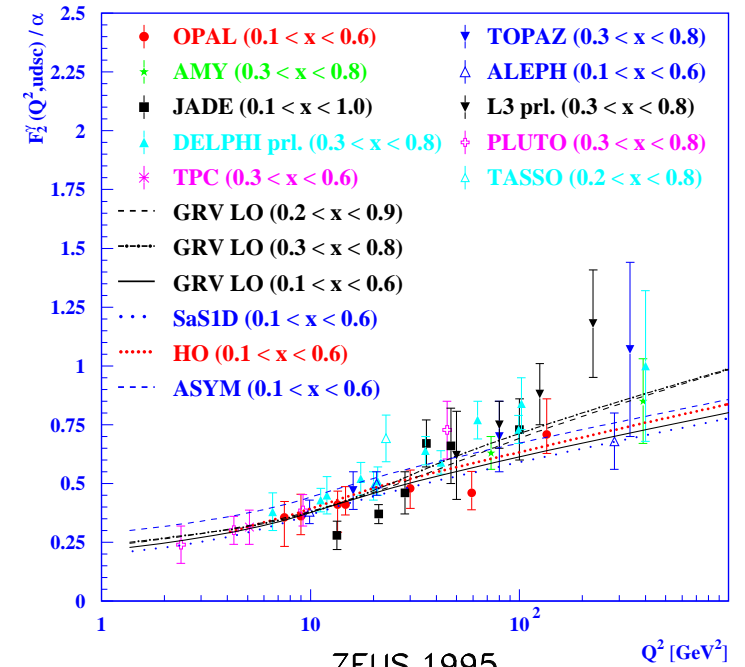
$\rightarrow f_{b/p}(x_p, \mu_{Fp}^2)$ = **parton densities in the proton**

$\rightarrow \sigma_{ab \rightarrow jj}$ **subprocess cross section; short-distance structure of the interaction**

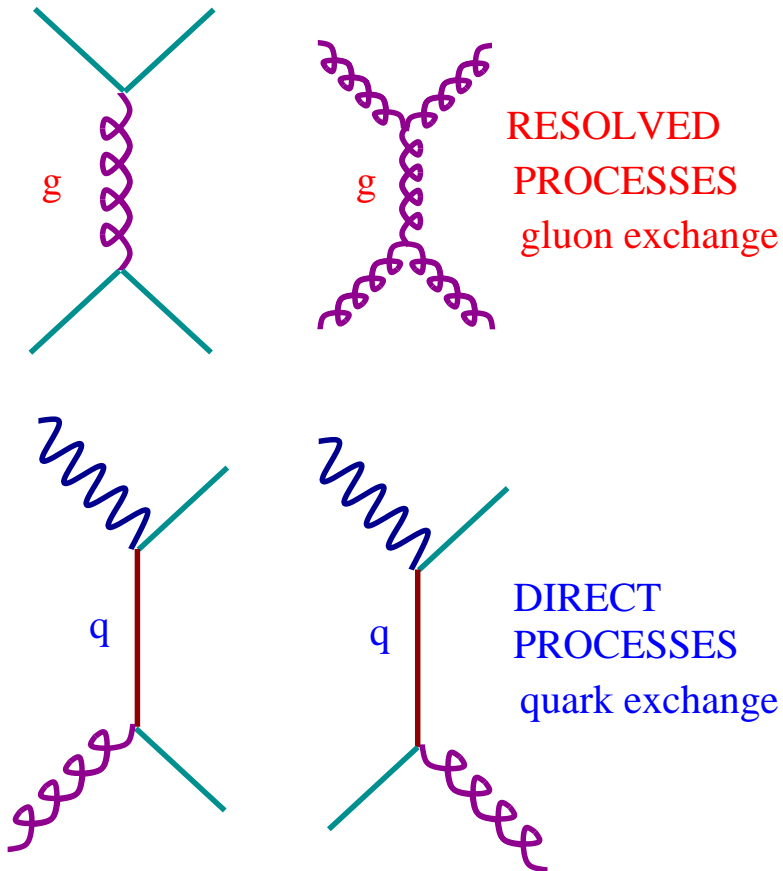
Photoproduction of Jets

- Measurements of jet photoproduction provide
 - Test of NLO QCD predictions based on current parametrisations of the proton and photon PDFs
 - Dynamics of resolved and direct processes
 - Photon structure: information on quark densities from F_2^γ in e^+e^- ; gluon density poorly constrained.
- Jet cross sections in photoproduction are sensitive to both the quark and gluon densities in the photon at larger scales $\mu_{F\gamma}^2 \sim E_{T,jet}^2$ (200 – 10⁴ GeV²)
- Proton structure: well constrained by DIS except for the gluon density at high x . Jet cross sections in γp are sensitive to parton densities at x_p up to ~ 0.6
- Observable to separate the contributions: the fraction of the photon's energy participating in the production of the dijet system

$$x_\gamma^{OBS} = \frac{1}{2E_\gamma} \sum_{i=1}^2 E_T^{jet_i} e^{-\eta^{jet_i}}$$



Dijet Photoproduction: the dynamics of resolved and direct processes



- The dynamics of dijet production has been investigated by studying the variable:

$$\cos \theta^* \equiv \tanh\left(\frac{1}{2}(\eta^{jet,1} - \eta^{jet,2})\right)$$

→ for two-to-two parton scattering θ^* coincides with the scattering angle in the dijet CMS

- QCD predicts different dijet angular distributions for resolved and direct:

→ **Resolved (gluon-exchange dominated)**

$$d\sigma/d|\cos \theta^*| \sim \frac{1}{(1-|\cos \theta^*|)^2}$$

→ **Direct (quark-exchange only)**

$$d\sigma/d|\cos \theta^*| \sim \frac{1}{(1-|\cos \theta^*|)^1}$$

- The dijet angular distribution $d\sigma/d|\cos \theta^*|$ for $x_\gamma^{OBS} < 0.75$ (“resolved”) should be steeper than that of $x_\gamma^{OBS} > 0.75$ (“direct”) as $|\cos \theta^*| \rightarrow 1$

Dijet Photoproduction: the dynamics of resolved and direct processes

- Measurement of the dijet differential cross section $d\sigma/d|\cos\theta^*|$ for dijet events with

$$E_T^{jet,1} > 14 \text{ GeV}, E_T^{jet,2} > 11 \text{ GeV}$$

$$-1 < \eta^{jet} < 2.4 \text{ (both jets)}$$

in the kinematic region

$$Q^2 < 1 \text{ GeV}^2 \text{ and } 134 < W_{\gamma p} < 277 \text{ GeV}$$

- Phase-space region:

$$|\cos\theta^*| < 0.8, M_{JJ} > 42 \text{ GeV}$$

$$0.1 < \frac{1}{2}(\eta^{jet,1} + \eta^{jet,2}) < 1.3$$

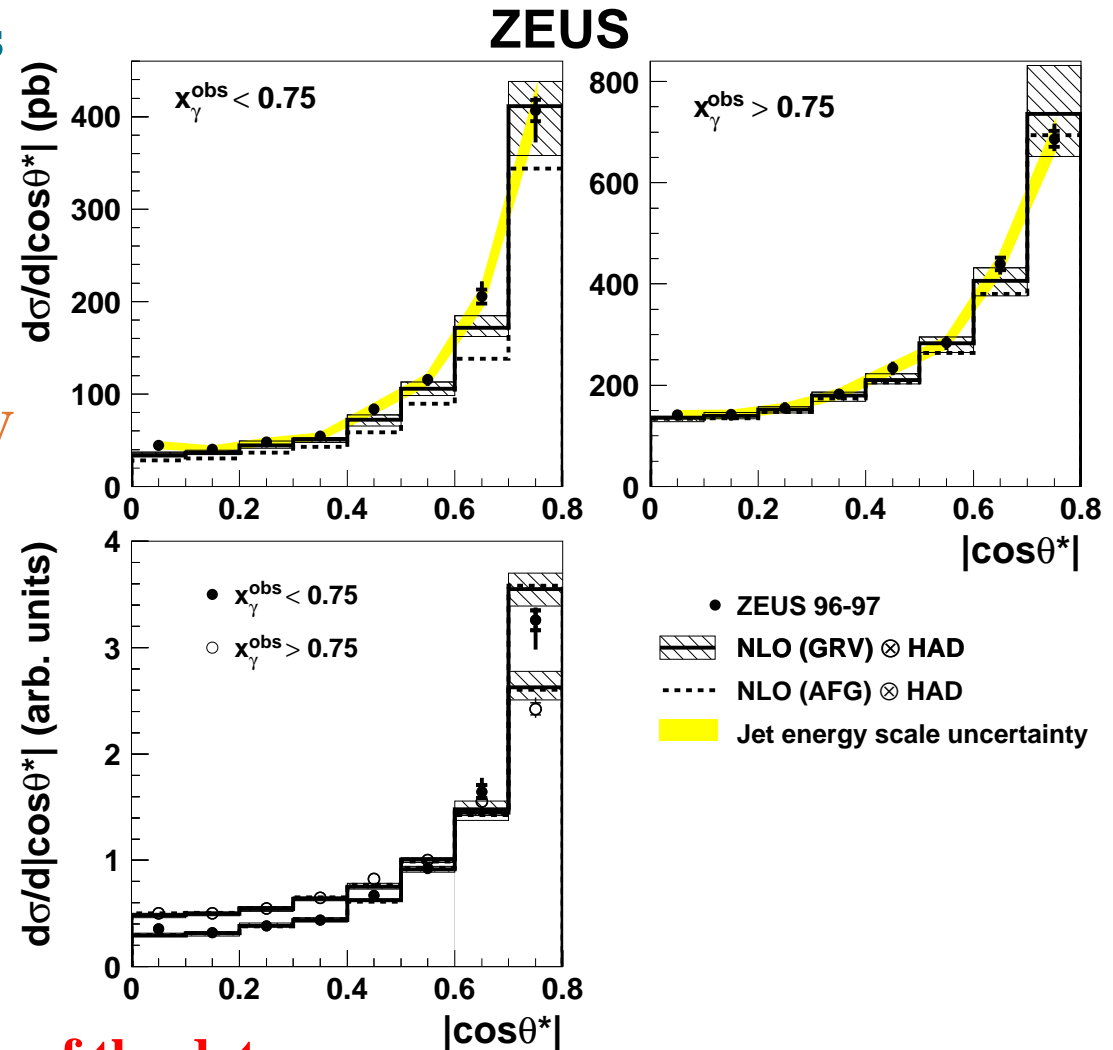
- Comparison with NLO QCD calculations:

→ High- x_γ^{OBS} (“direct”): NLO describes the shape and normalisation of the data

→ Low- x_γ^{OBS} (“resolved”): NLO describes

the shape and (reasonably) the normalisation of the data

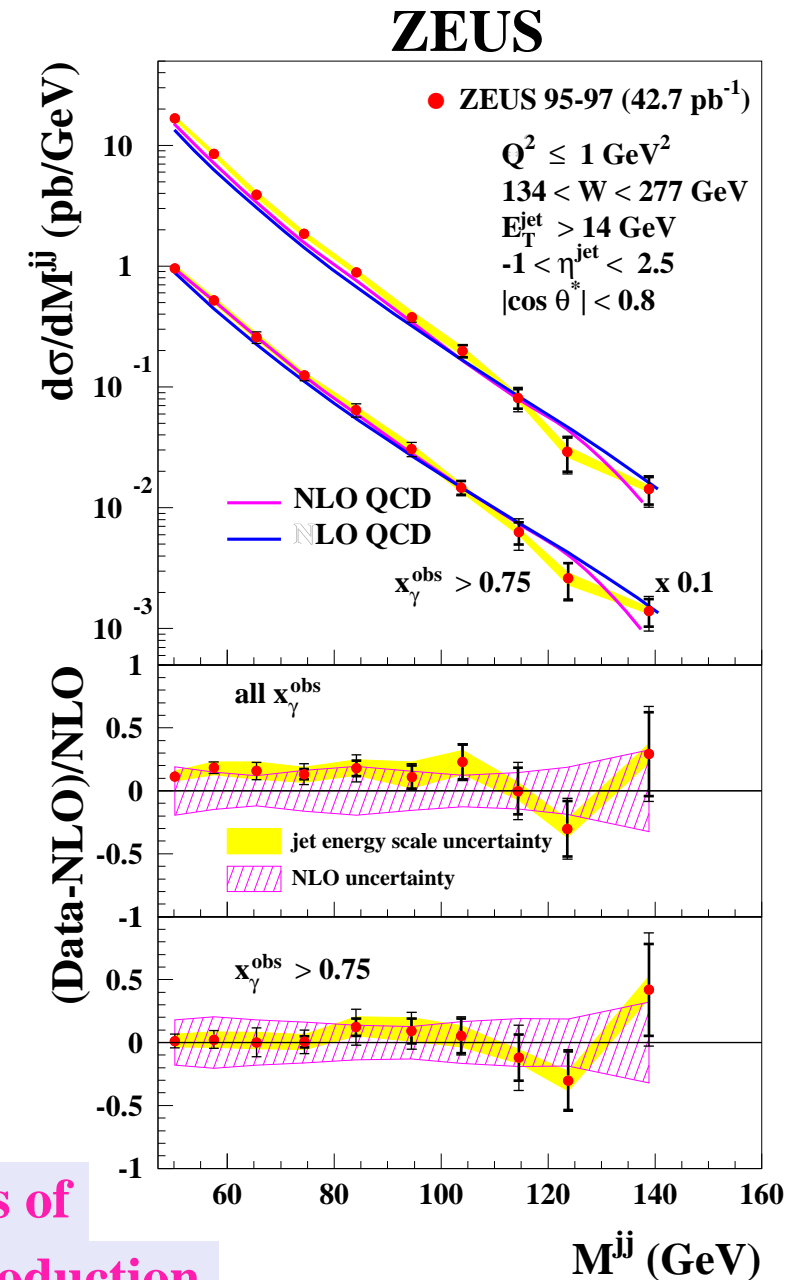
- The dijet angular distribution of the “resolved” sample is steeper than that of “direct”



High- M_{JJ} Dijet Photoproduction

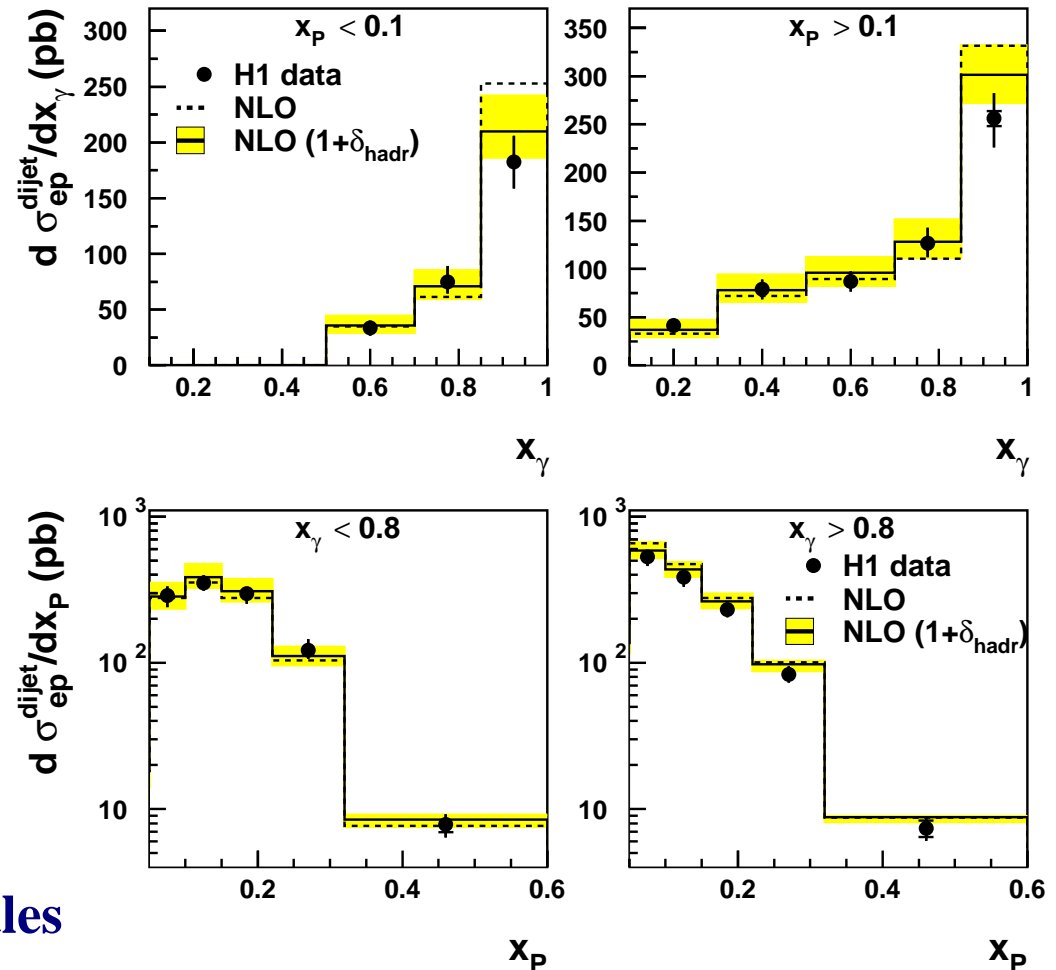
- Measurement of the dijet differential cross section $d\sigma/dM_{JJ}$ in the range $47 < M_{JJ} < 160$ GeV for dijet events with $E_T^{jet} > 14$ GeV, $-1 < \eta^{jet} < 2.5$ and $|\cos \theta^*| < 0.8$
- Small experimental uncertainties:
 - jet energy scale known to 1% \Rightarrow 5% on $d\sigma/dM_{JJ}$
- Small theoretical uncertainties:
 - higher-order terms (varying μ_R) below 15%
 - γ PDFs (GRV-HO, AFG-HO) below 10%
 - resolved processes suppressed at high M_{JJ}
 - small hadronisation corrections, below 5%
- NLO QCD calculations describe the shape and normalisation of the measurements well

→ Validity of the pQCD description of the dynamics of parton-parton and γ -parton interactions in photoproduction



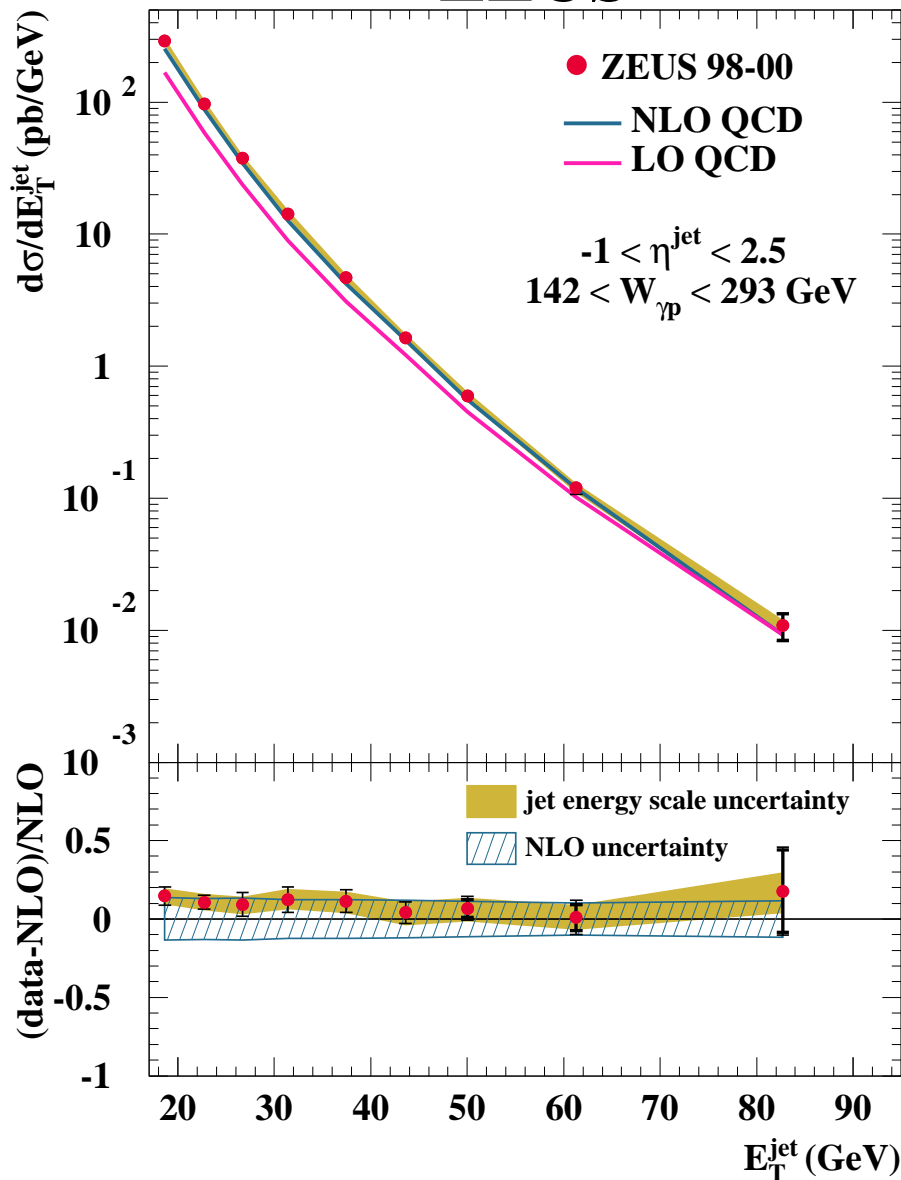
Dijet Photoproduction: photon and proton structure

- Measurement of the dijet cross sections $d\sigma/dx_\gamma$ and $d\sigma/dx_p$ for dijet events with $E_{T,max} > 25$ GeV, $E_{T,second} > 15$ GeV and $-0.5 < \eta^{jet} < 2.5$ (both jets) in the kinematic region $Q^2 < 1$ GeV² and $95 < W_{\gamma p} < 285$ GeV
- x_p variable: $x_p = \frac{1}{2E_p} \sum_{i=1}^2 E_T^{jet_i} e^{\eta^{jet_i}}$
- NLO calculations using CTEQ5M (proton) and GRV-HO (photon) describe the data
- Theoretical uncertainties:
 - terms beyond NLO \Rightarrow 10-20%
 - uncertainties of proton PDFs $< 5\%$ (up to 15%) for $x_p < 0.1$ (> 0.1)
- Even up to the highest x_p , where 40% of $d\sigma/dx_p$ arises from gluon_p-induced processes, the data is described by NLO
- Consistent with QCD-evolved photon PDFs determined from measurements at lower scales



Inclusive Jet Photoproduction

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- Measurement of the differential cross section $d\sigma/dE_T^{\text{jet}}$ for inclusive jet photoproduction with $E_T^{\text{jet}} > 17$ GeV and $-1 < \eta^{\text{jet}} < 2.5$ in the kinematic region

$Q^2 < 1$ GeV² and $142 < W_{\gamma p} < 293$ GeV

- Small experimental uncertainties

→ jet-energy scale known to $\pm 1\%$

⇒ $\sim \pm 5-10\%$ on the cross sections

- Small theoretical uncertainties

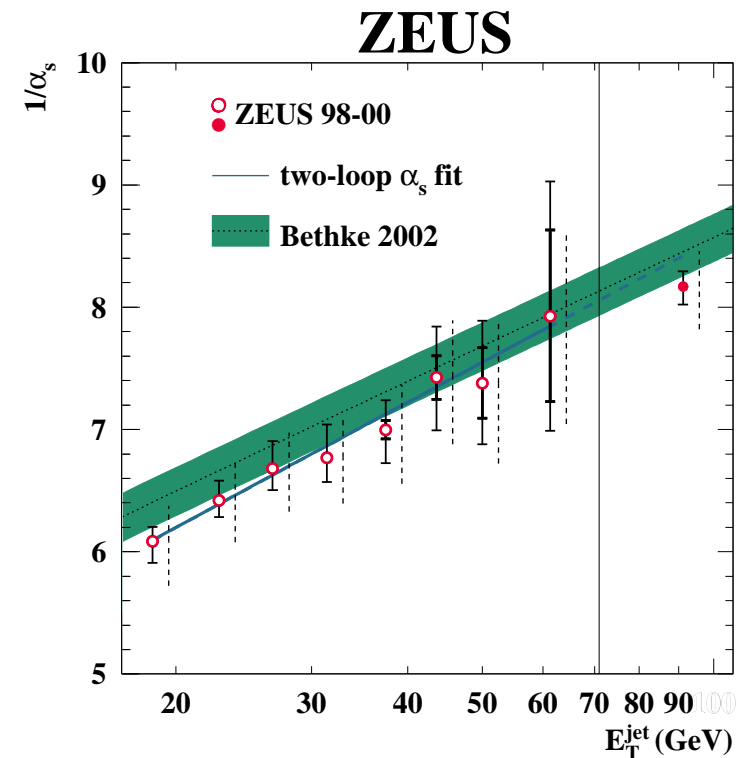
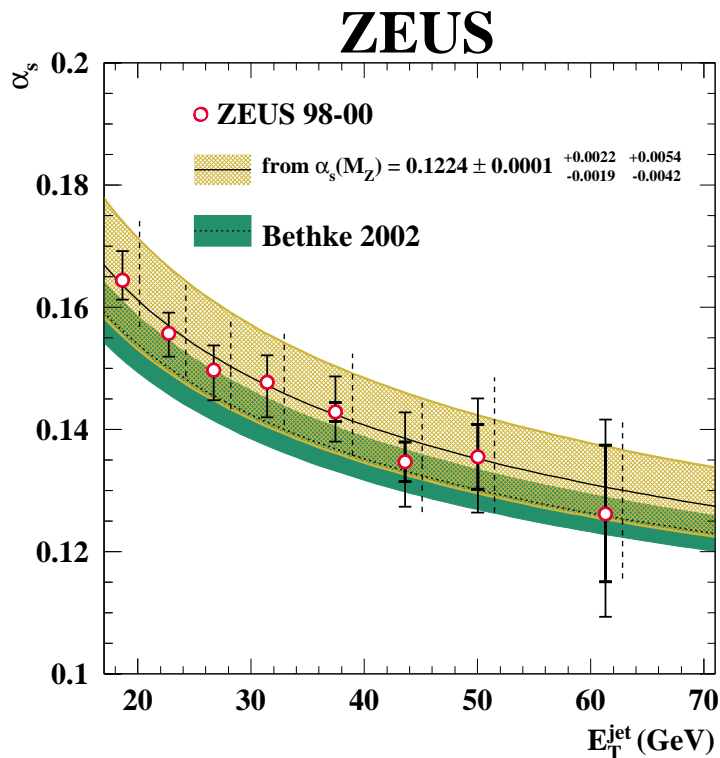
→ terms beyond NLO ⇒ below 10%

→ proton PDFs ⇒ 1-5%

→ photon PDFs ⇒ below 5%

- Precise test of NLO QCD calculations: good description of the data in shape and normalization

Inclusive Jet Photoproduction and Determination of α_s

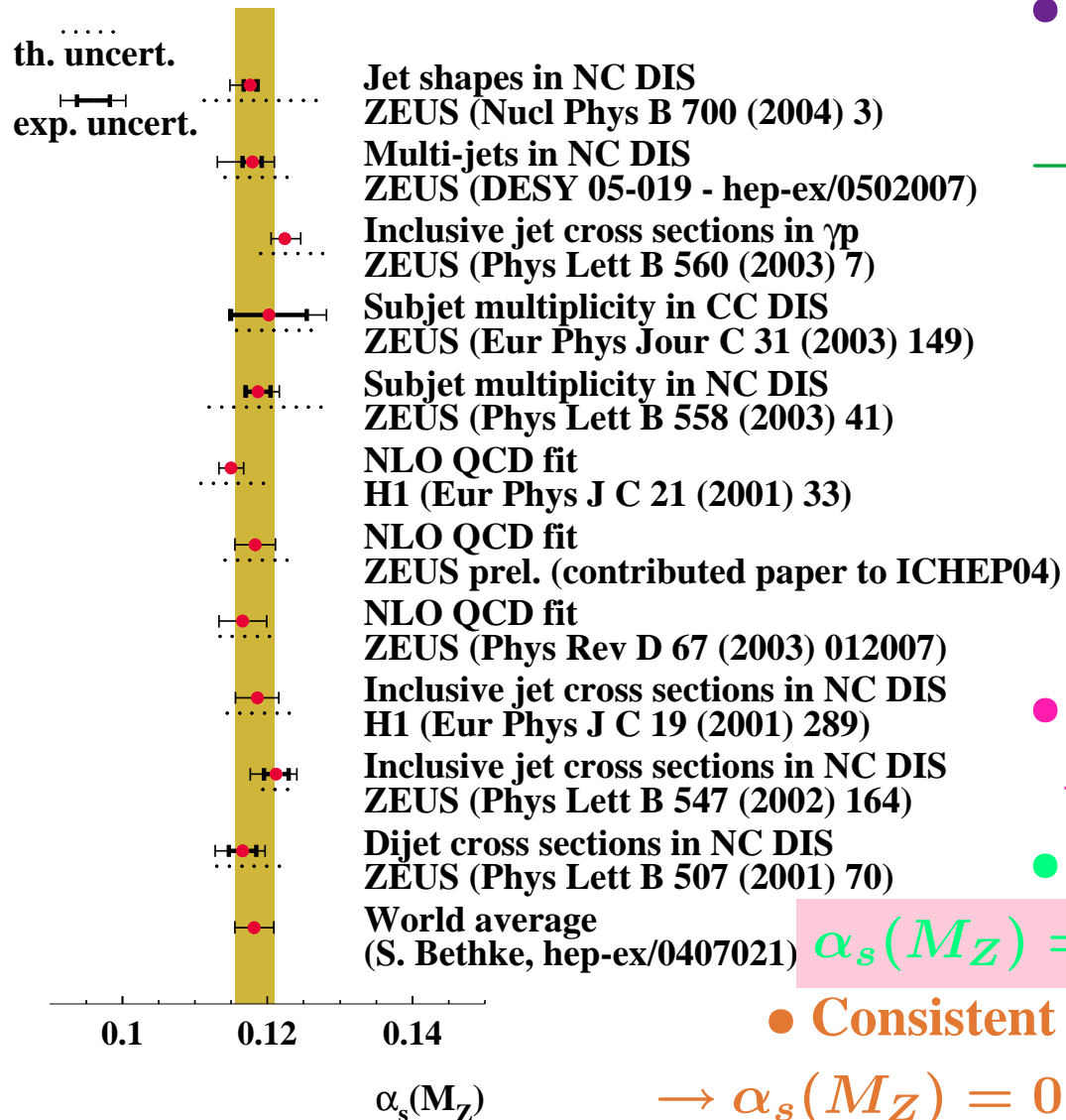


$$\alpha_s(M_Z) = 0.1224 \pm 0.0001 \text{ (stat.) } ^{+0.0022}_{-0.0019} \text{ (exp.) } ^{+0.0054}_{-0.0042} \text{ (th.)}$$

- Determination of $\alpha_s(E_T^{\text{jet}})$: the measured energy-scale dependence of α_s is **in good agreement with the running predicted by QCD over a large range in E_T^{jet}**
- Fit with two-loop formulae $\alpha_s^{-1}(E_T^{\text{jet}}) = \beta_0/2\pi \cdot \ln E_T^{\text{jet}} \cdot (1 - \dots)$

$$\beta_0 = 8.53 \pm 0.22 \text{ (stat.) } ^{+0.56}_{-0.53} \text{ (exp.) } ^{+1.34}_{-0.82} \text{ (th.)} \quad (\text{QCD: } \beta_0 = 7.67 \text{ for } n_f = 5)$$

Summary of α_s determinations



$$\alpha_s(M_Z) = 0.1186 \pm 0.0011(\text{exp.}) \pm 0.0050(\text{th.})$$

• Consistent with world average (Bethke, 2004):

$$\rightarrow \alpha_s(M_Z) = 0.1182 \pm 0.0027 \text{ (only NNLO results)}$$

• Wealth of determinations of α_s at HERA from a variety of observables:

→ NLO QCD analyses of structure functions

→ Inclusive jet production in NC DIS

→ Dijet production in NC DIS

→ Tri-jet/Dijet rate in NC DIS

→ Jet substructure in NC DIS

→ Jet substructure in CC DIS

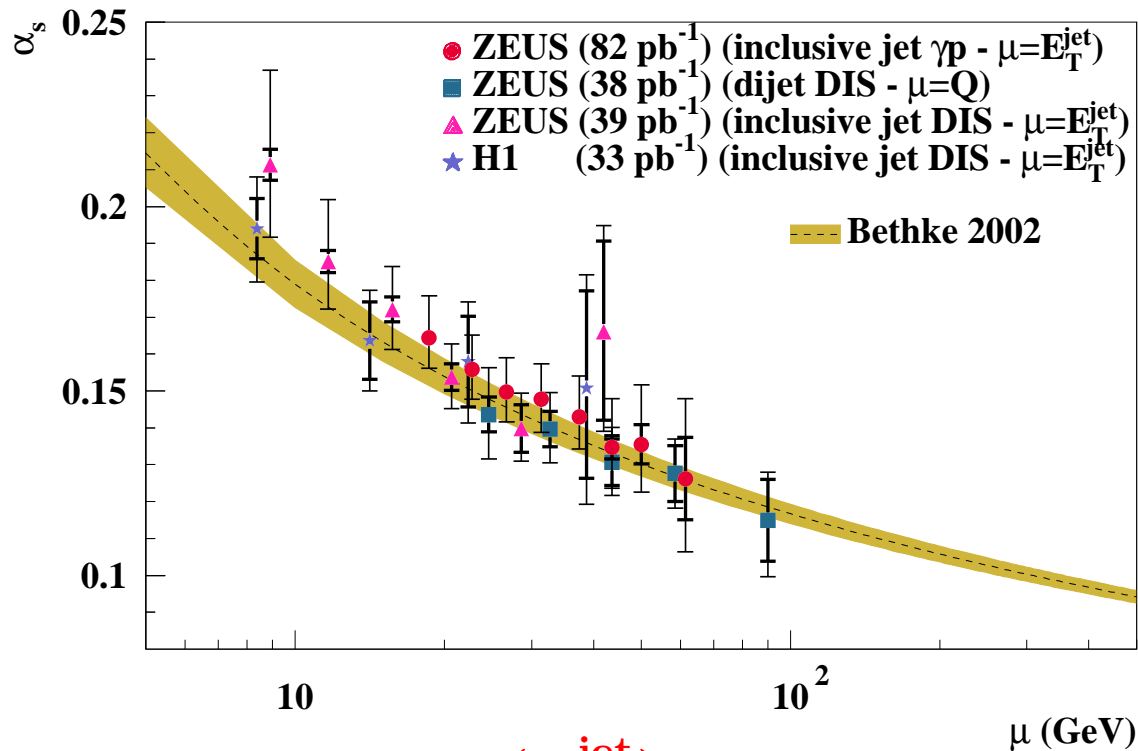
→ Inclusive jet photoproduction

• Theoretical uncertainties are dominant

→ Biggest contrib. from terms beyond NLO

• Average of HERA determinations

The running of α_s from HERA data alone

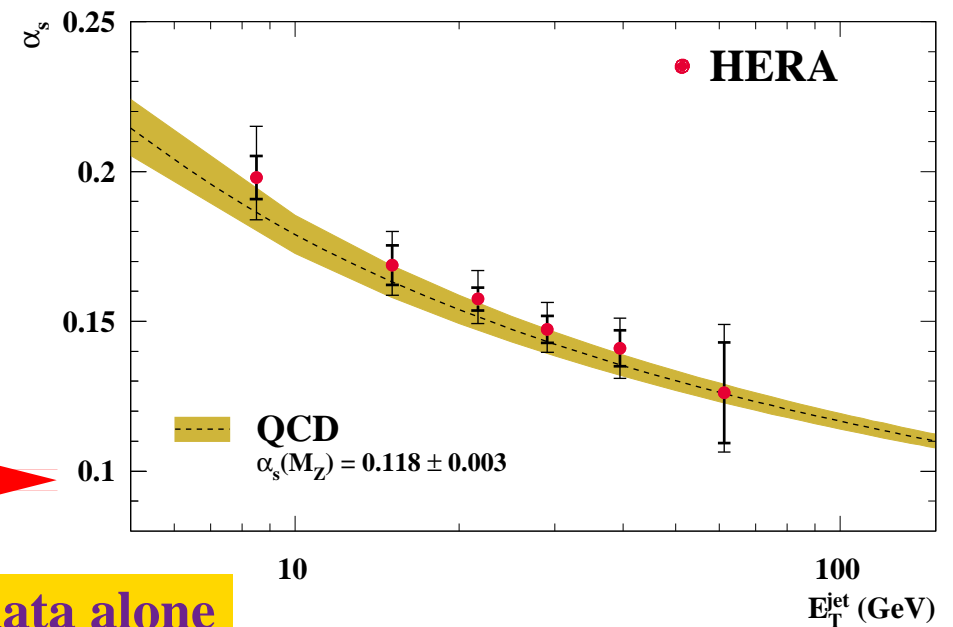


● Determinations of $\alpha_s(\mu)$:

→ Dijet NC DIS ($\mu = Q$)

→ Inclusive jet NC DIS ($\mu = E_T^{\text{jet}}$)

→ Inclusive jet γp ($\mu = E_T^{\text{jet}}$)



● Combination of $\alpha_s(E_T^{\text{jet}})$ determinations
at similar energy scales

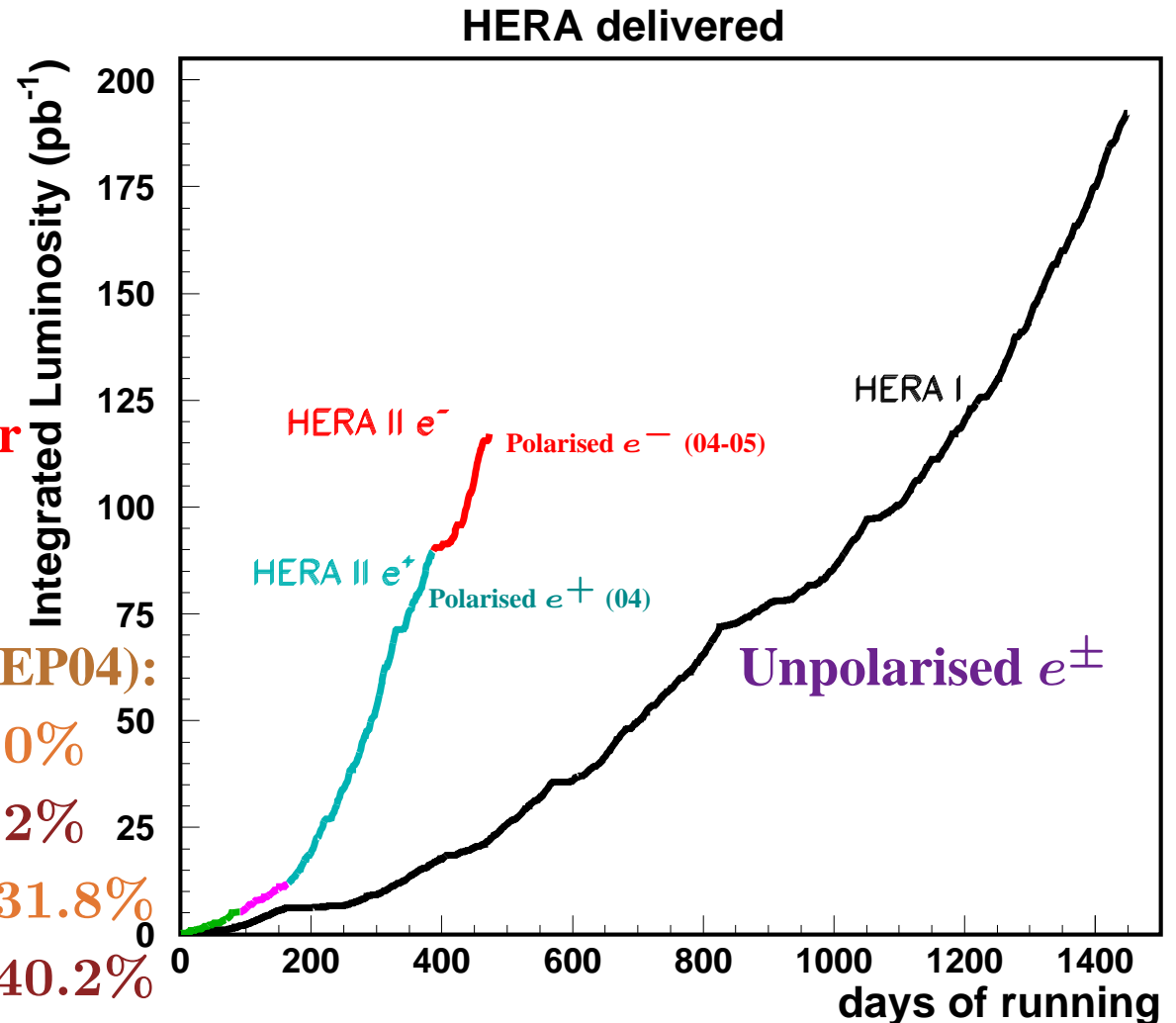
Observation of the running of α_s from HERA data alone

→ Consistent with the running predicted by QCD over a large range in E_T^{jet}

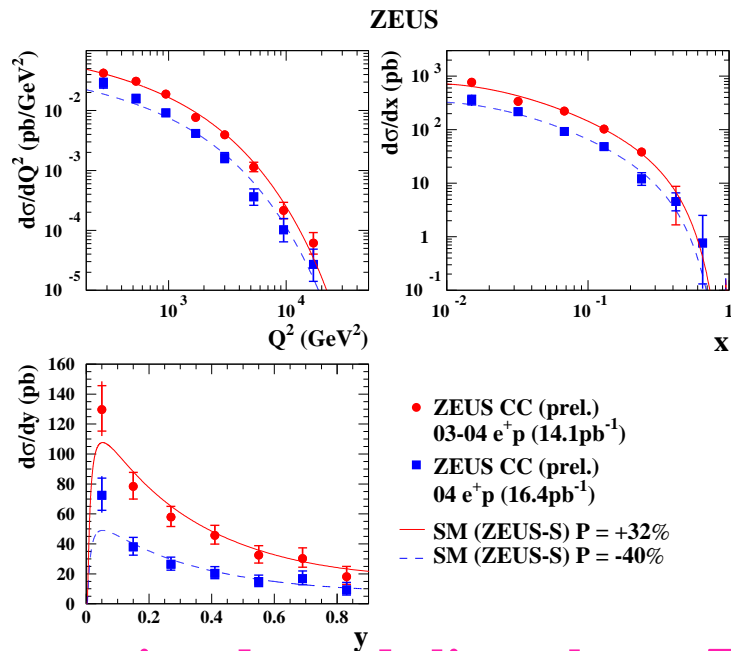
HERA II

First results from HERA II data

- Luminosity and detector upgrade
 - Long run period until 2007
 - Installation of spin rotators in collider experiments: H1 and ZEUS
 - Longitudinally polarised e^\pm beams
- New window into Electroweak Sector
- First results on NC and CC DIS $e_L^+ p$ and $e_R^+ p$ at high Q^2
 - Results presented last summer (ICHEP04):
 - H1: $\mathcal{L} = 15.3 \text{ pb}^{-1}$ at $P = +33.0\%$
 - H1: $\mathcal{L} = 21.7 \text{ pb}^{-1}$ at $P = -40.2\%$
 - ZEUS: $\mathcal{L} = 14.1 \text{ pb}^{-1}$ at $P = +31.8\%$
 - ZEUS: $\mathcal{L} = 16.4 \text{ pb}^{-1}$ at $P = -40.2\%$
 - Longitudinal Polarisation: $P = \frac{N_R - N_L}{N_R + N_L}$



Charged Current Deep Inelastic $e_{L,R}^+ p$ scattering



- Cross section depends linearly on P

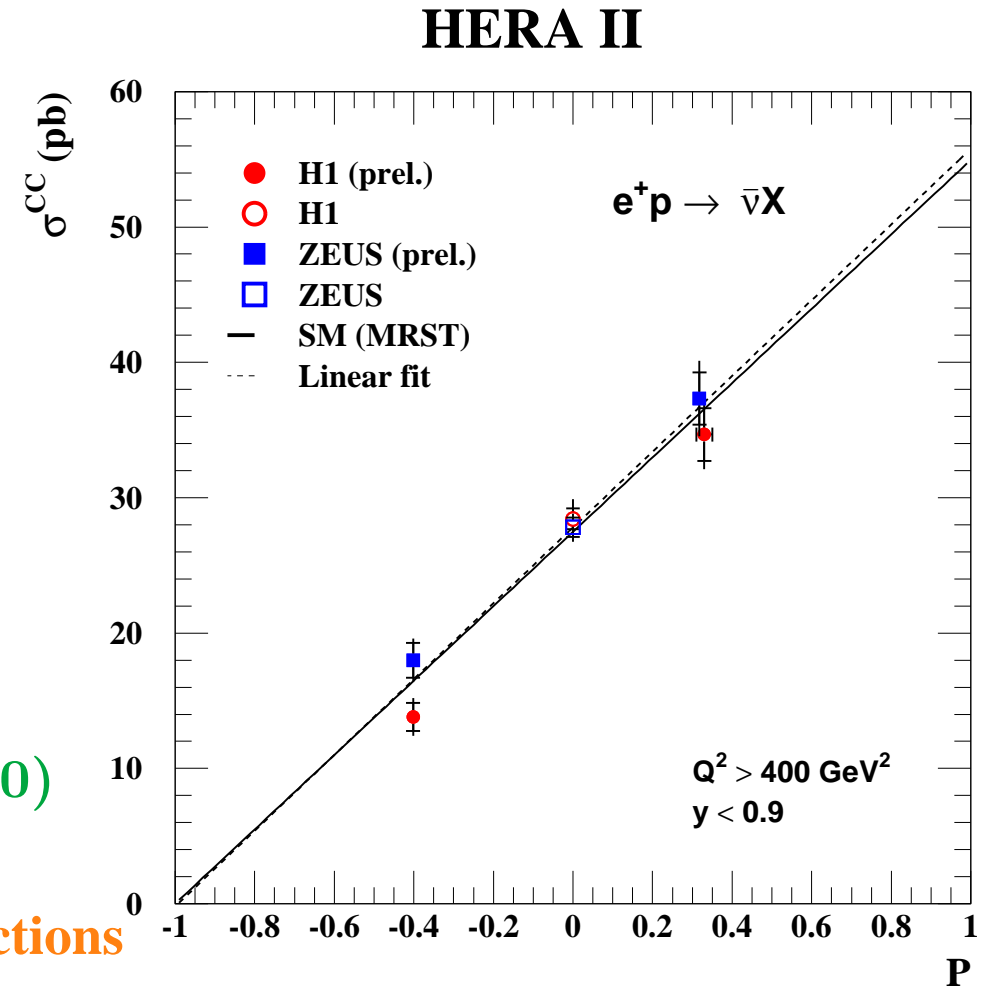
$$\sigma_{CC}(e^+p, P) = (1 + P) \cdot \sigma_{CC}(e^+p, P = 0)$$

→ Prediction $\sigma_{CC}(e^+p, P = -1) = 0$

- Direct sensitivity to right-handed CC interactions

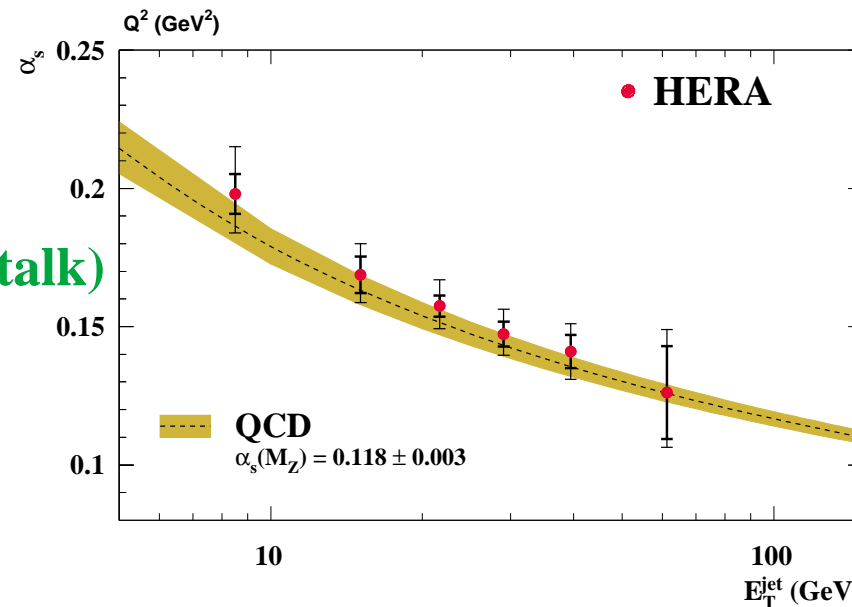
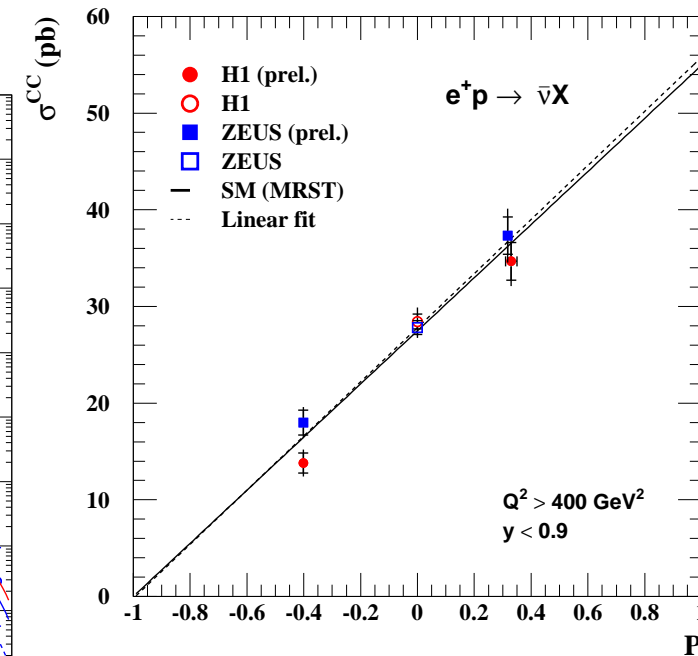
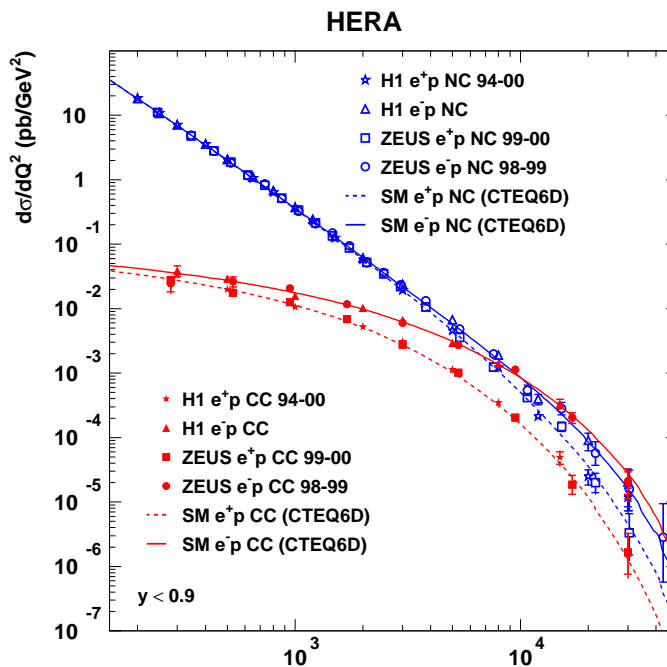
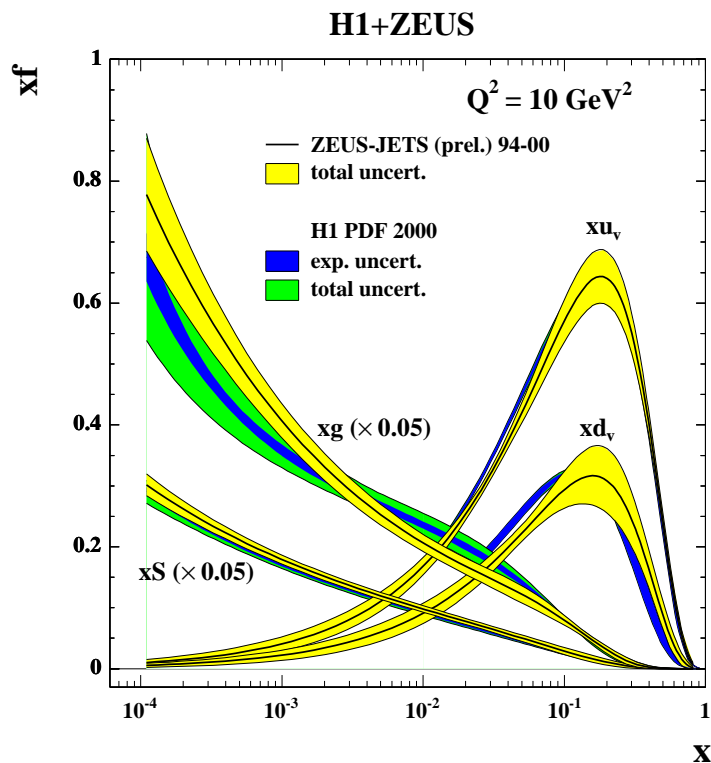
$$\sigma_{CC}(e^+p, P = -1) = 0.2 \pm 1.8(\text{stat}) \pm 1.6(\text{sys}) \text{ pb} \quad (\text{H1+ZEUS combined})$$

⇒ Results in agreement with the prediction of the Standard Model



HERA II

Summary



● Other areas of HERA physics (not covered in this talk)

- Diffraction
- Heavy quarks
- Searches for Physics beyond SM