

# Neutrino Oscillation Physics

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# The neutrino

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The most curious elementary particle  
and the one that gave us more surprises

is still a perfect unknown

...because it only interacts weakly

three active neutrinos only

+ the possibility of sterile neutrinos

Flavour mixing  
(oscillations)



Massive Neutrinos

First evidence of Physics beyond  
the Standard Model



# Flavour Mixing

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$\nu_e$

$\nu_\mu$

$\nu_\tau$

weak  
eigenstates

$$\nu_{\alpha L} = \sum_{k=1}^n U_{\alpha k} \nu_{kL}$$



$m_1$



$m_2$



$m_3$

mass  
eigenstates

$\theta_{23}$

$\theta_{13}, \delta_{\text{CP}}$

$\theta_{12}$

$\alpha_1, \alpha_2$

PMNS mixing matrix

$$U = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix} \begin{pmatrix} c_{13} & 0 & s_{13}e^{-i\delta} \\ 0 & 1 & 0 \\ -s_{13}e^{i\delta} & 0 & c_{13} \end{pmatrix} \begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

atmospheric neutrinos

connection between  
solar and atmospheric

solar neutrinos

$$\begin{pmatrix} e^{i\alpha_1} & 0 & 0 \\ 0 & e^{i\alpha_2} & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

**Majorana**

**Dirac**

Introduction

the  $\theta_{13}$  quest

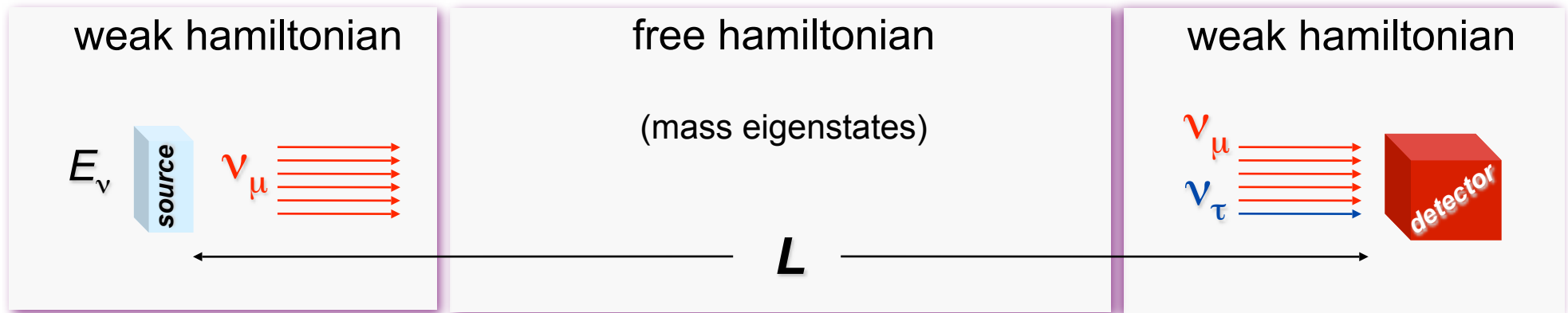
the path to  
CP violation

which way ?

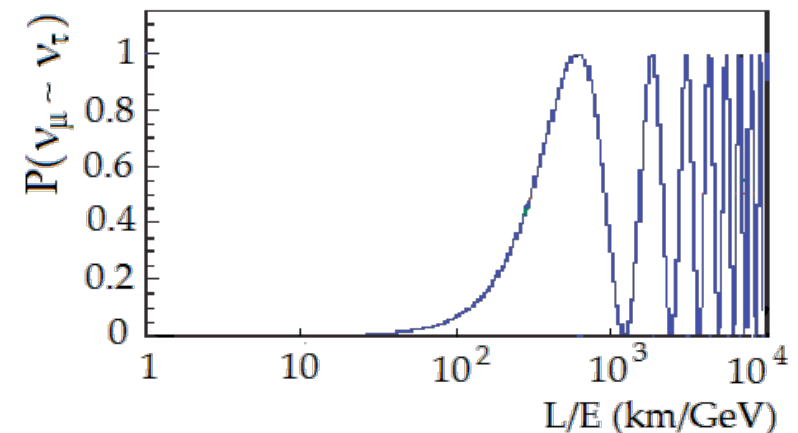
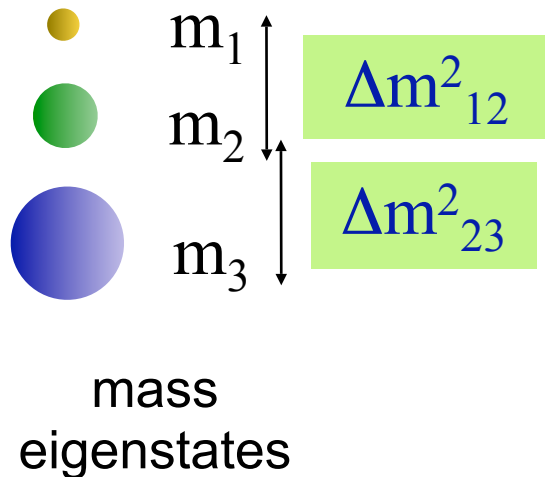
# Neutrino oscillations

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**Requirements:** Massive neutrinos & different masses



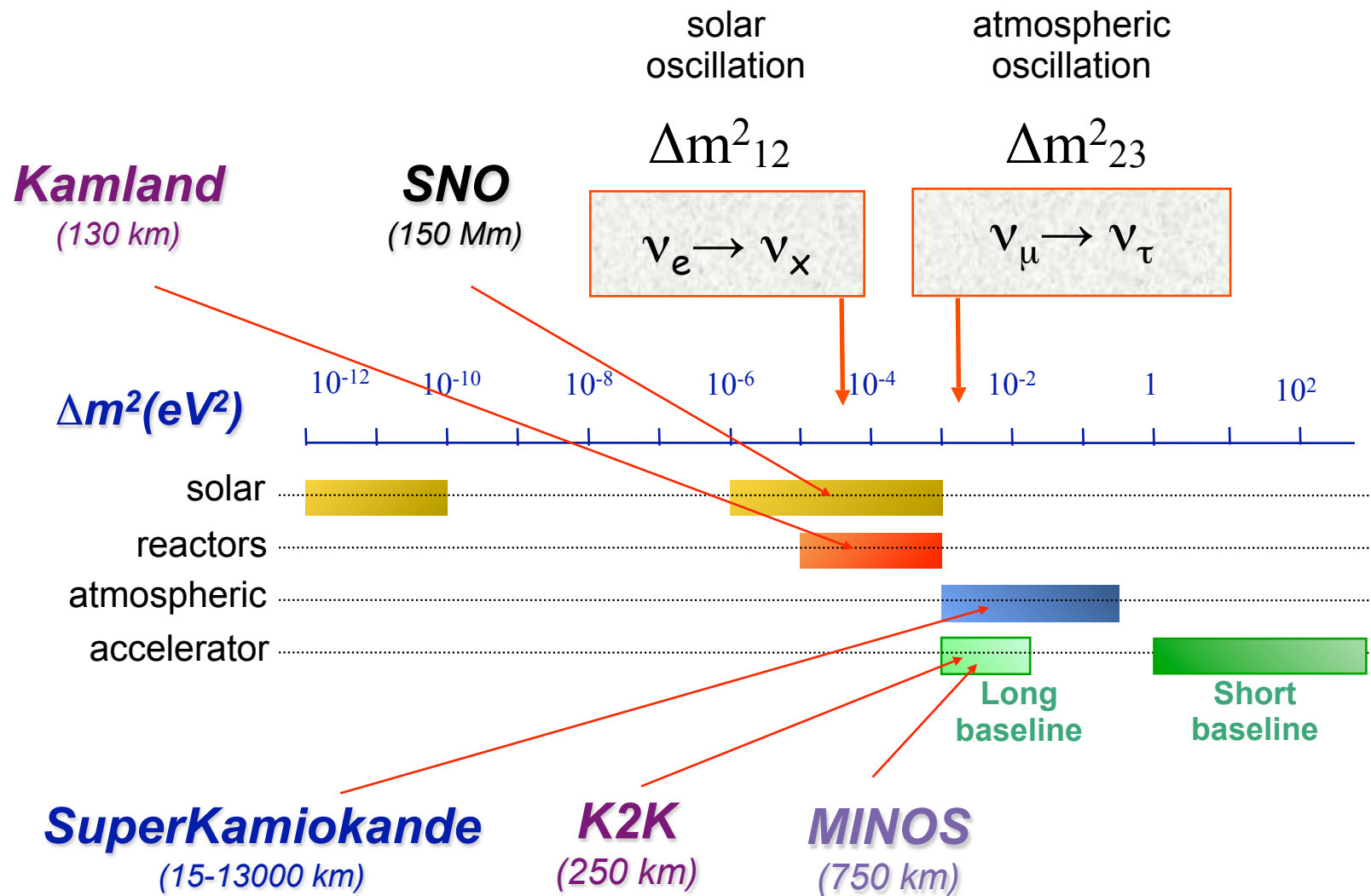
$$P_{\nu_\mu \nu_\tau} = \sin^2 2\theta \cdot \sin^2 \left( \frac{\Delta m^2 \cdot L}{4E_\nu} \right)$$





# Experimental results I

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# Experimental results II

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Errors from 10 to 30%

$$\Delta m_{21}^2 = 7.67^{+0.22}_{-0.21} \left( {}^{+0.67}_{-0.61} \right) \times 10^{-5} \text{ eV}^2,$$

$$\Delta m_{31}^2 = \begin{cases} -2.37 \pm 0.15 \left( {}^{+0.43}_{-0.46} \right) \times 10^{-3} \text{ eV}^2 & \text{(inverted hierarchy),} \\ +2.46 \pm 0.15 \left( {}^{+0.47}_{-0.42} \right) \times 10^{-3} \text{ eV}^2 & \text{(normal hierarchy),} \end{cases}$$

$$\theta_{12} = 34.5 \pm 1.4 \left( {}^{+4.8}_{-4.0} \right),$$

$$\theta_{23} = 42.3^{+5.1}_{-3.3} \left( {}^{+11.3}_{-7.7} \right),$$

$$\theta_{13} = 0.0^{+3.9} \left( {}^{+9.0} \right)$$

Still missing

$\theta_{13}$

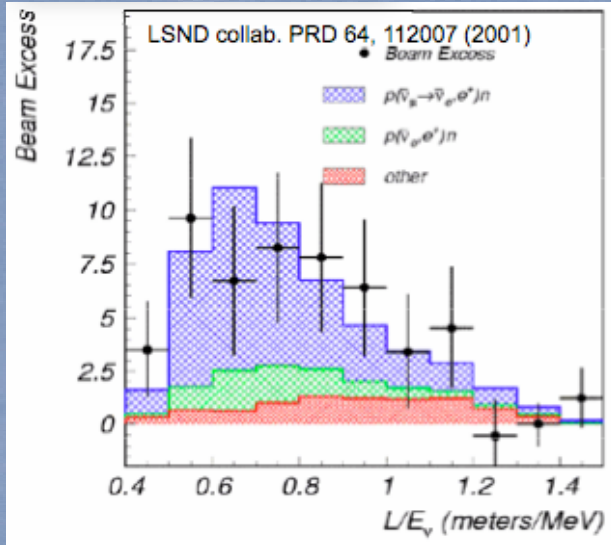
$\text{sign}(\Delta m_{23}^2)$

$\delta_{\text{cp}}$

$\text{is } \theta_{23} = 45^\circ ?$

# Sterile neutrinos

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LSND

$$\bar{\nu}_{\mu} \rightarrow \bar{\nu}_e$$

$$L/E \sim 1$$

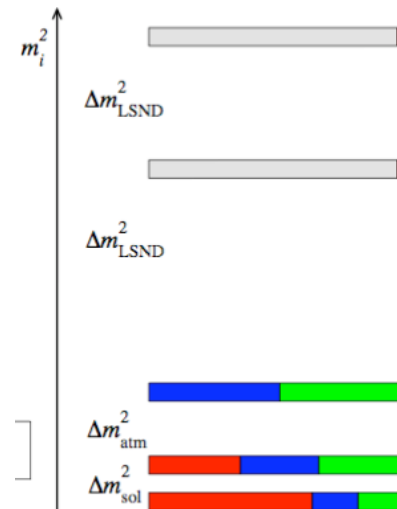
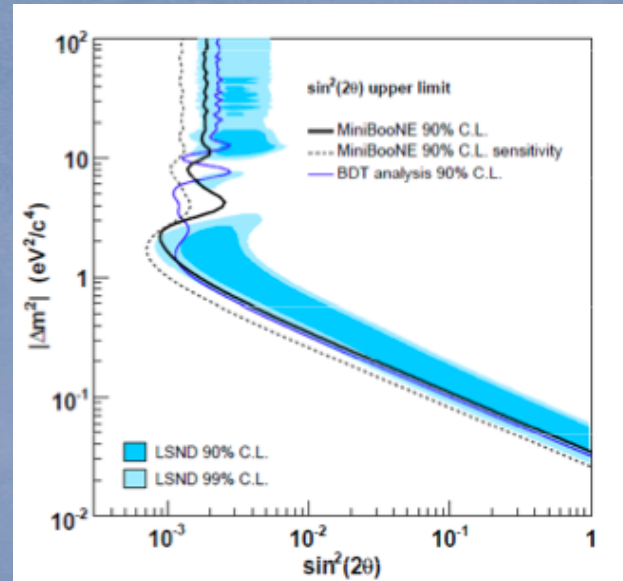


$$\Delta m^2 \sim 1 \text{ eV}$$

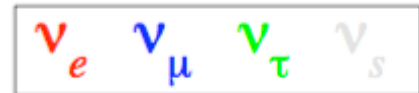
Incompatible  
with all other experiments  
for 3 neutrinos only

## MiniBooNE

Excludes the  
LSND result  
as two family  
oscillations



two sterile  
neutrinos



Three active  
light neutrinos



# The $\theta_{13}$ quest

# Oscillation length

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$$P_{\nu_\mu \nu_\tau} = \sin^2 2\theta \cdot \sin^2 \left( \frac{\Delta m^2 \cdot L}{4E_\nu} \right)$$

$$\frac{\Delta m^2 \cdot L}{4E_\nu} = \frac{\pi}{2} \longrightarrow L_{osc} = \frac{2\pi}{\Delta m^2}$$

$$L_{osc}^{23} = \frac{2\pi}{\Delta m_{23}^2} \simeq 475 \text{ Km}$$

$$L_{osc}^{12} = \frac{2\pi}{\Delta m_{12}^2} \simeq 15500 \text{ Km}$$



# Subdominant oscillation

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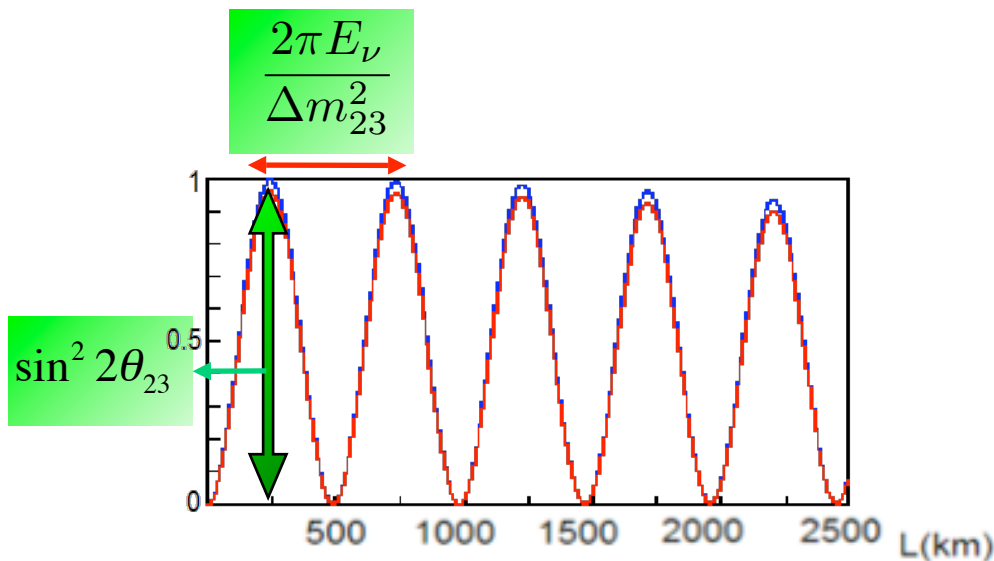
atmospheric

solar

interference

$$\frac{P(\text{no } \nu_e)}{P(\nu_e)} \approx \frac{P_{atm}(\theta_{23}, |\Delta m_{23}^2|)}{\frac{\sin^2 2\theta_{13}}{2} \cdot P_{atm}(\theta_{23}, |\Delta m_{23}^2|) + P_{sol}(\theta_{12}, \Delta m_{12}^2)} \pm \sin 2\theta_{13} \cdot F_{solar} \cdot F_{atm}(\sin 2\theta_{23}, |\Delta m_{23}^2|) \cdot F(\delta_{cp}, \Delta m_{23}^2)$$

Dominant (no  $\nu_e$ )



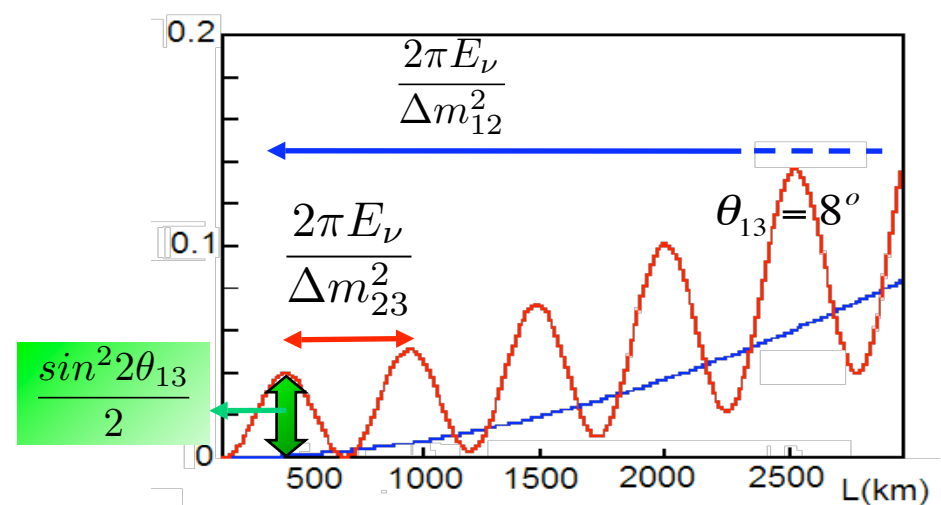
$\nu_\mu \rightarrow \nu_\tau$

OPERA

$\nu_\mu \rightarrow \nu_\mu$

MINOS

Subdominant ( $\nu_e$ )



$\nu_e \rightarrow \nu_\mu$

$\nu_e \rightarrow \nu_\tau$

D-Chooz

$\nu_e \rightarrow \nu_e$

$\nu_\mu \rightarrow \nu_e$

T2K  
NOvA



# The $\theta_{13}$ quest

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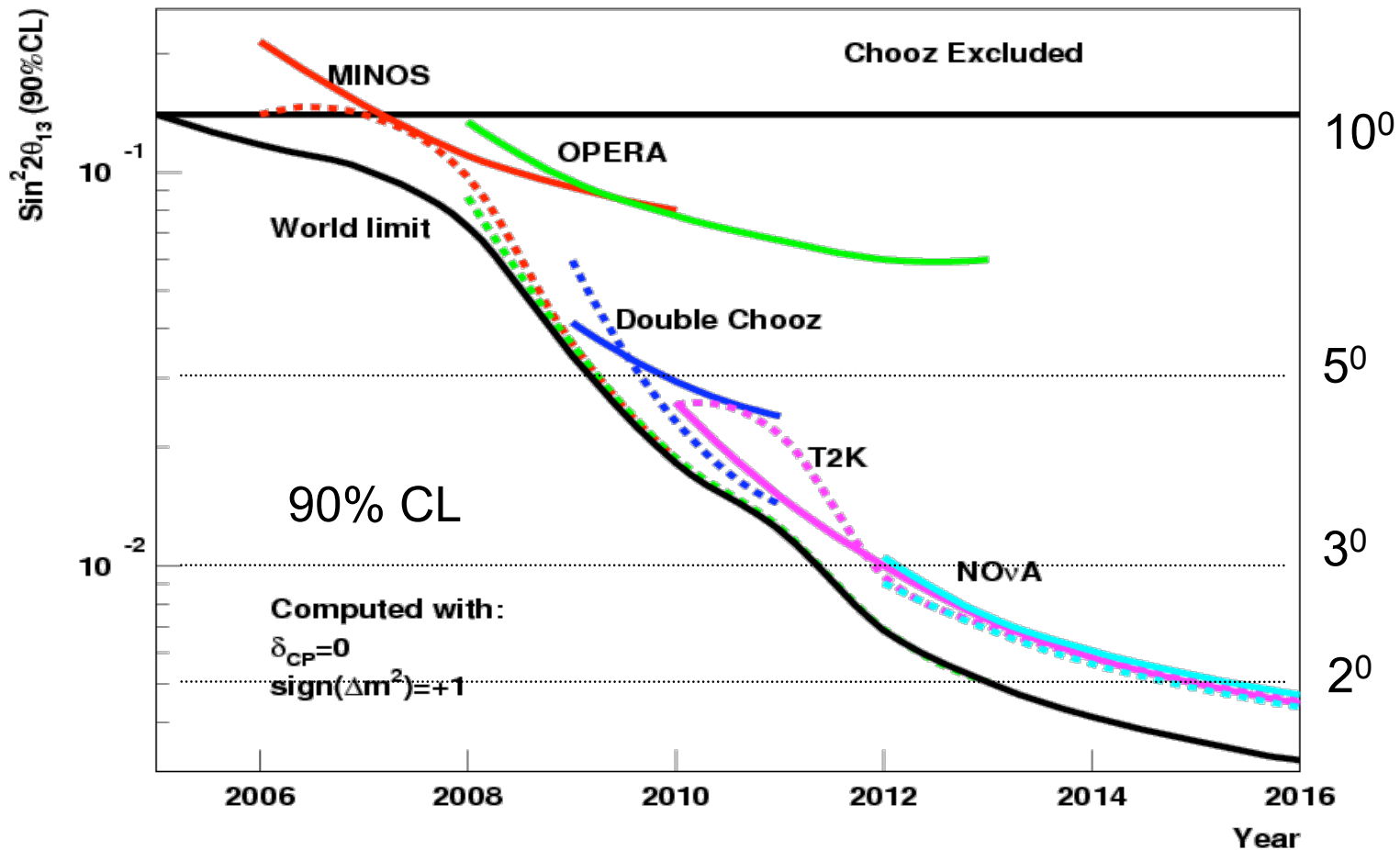
Subdominant oscillation:

Accelerators

$$\nu_{\mu} \rightarrow \nu_e$$

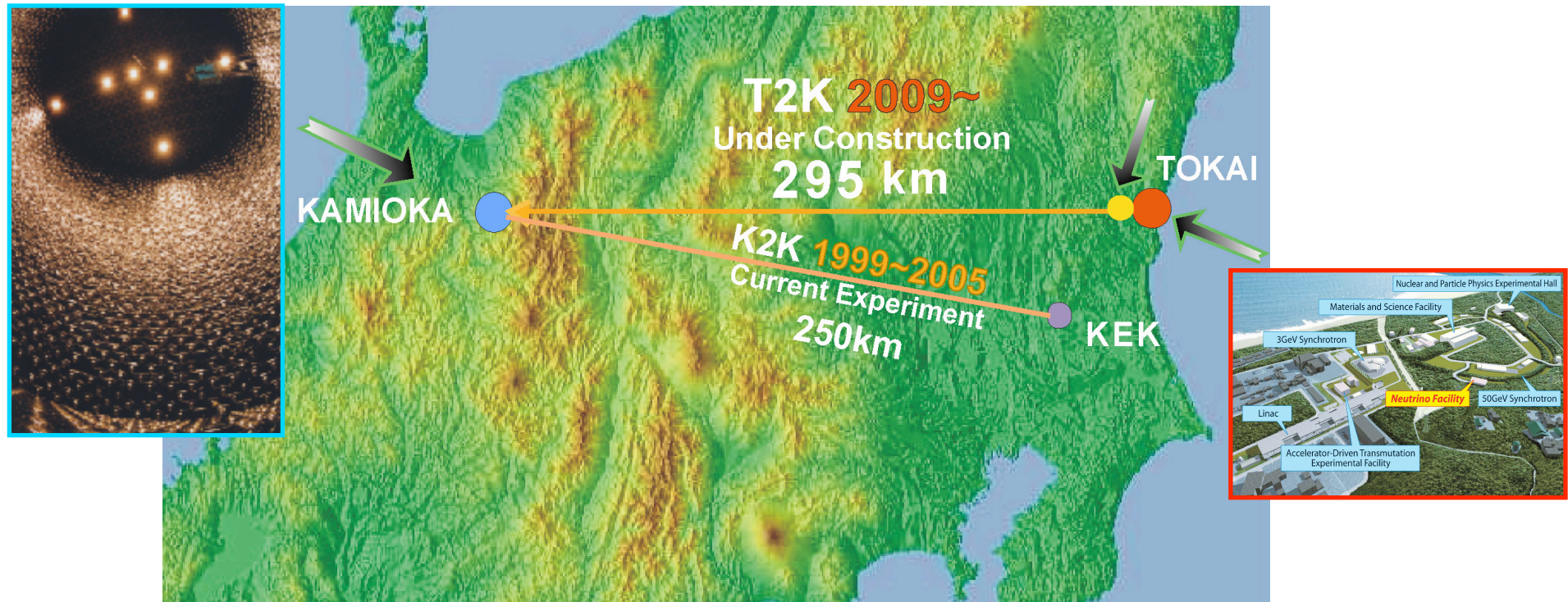
Reactors

$$\bar{\nu}_e \rightarrow \bar{\nu}_e$$



# Super-beams I: T2K

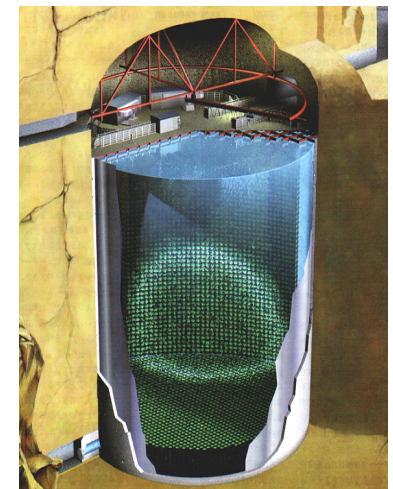
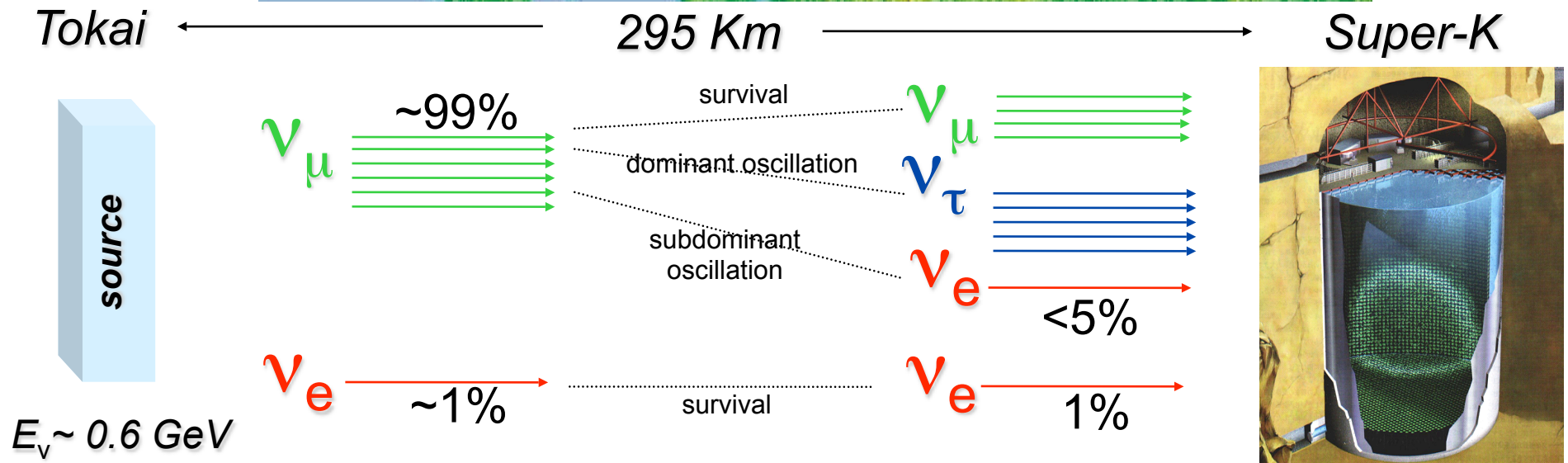
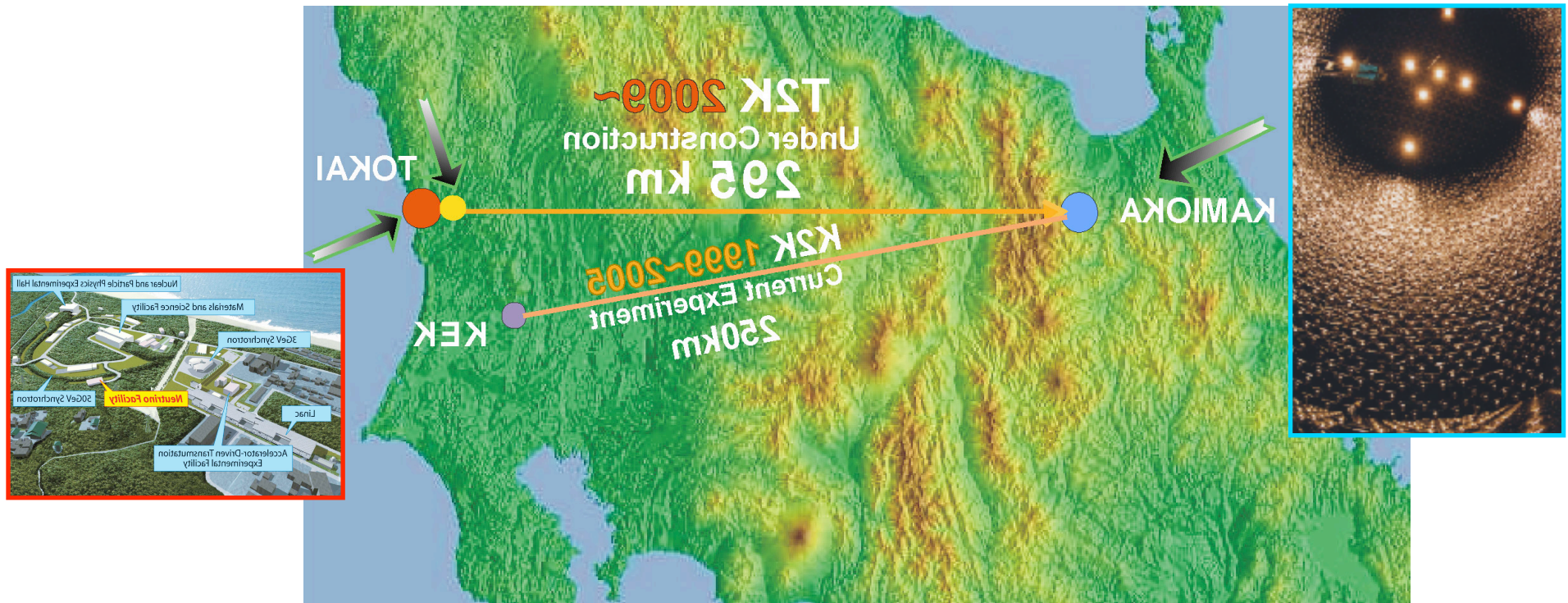
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# T2K: Tokai to Kamioka

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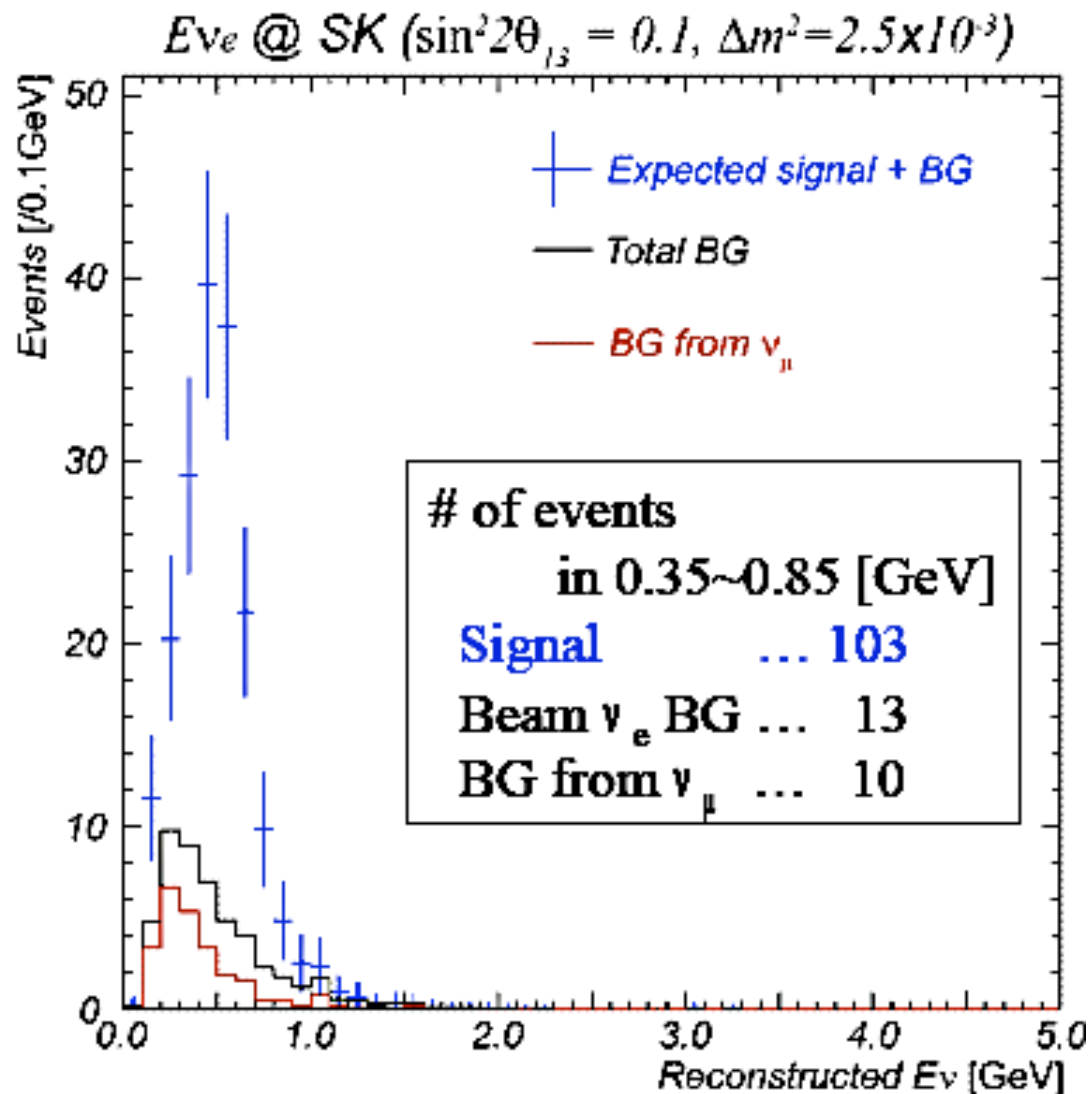




# T2K expected sensitivity

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$$\theta_{13} = 9^\circ$$



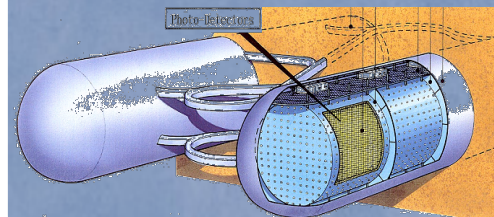
Current status  $\theta_{13} < 10^\circ$   
 $\sin^2 2\theta_{13} < 0.15$

T2K 1<sup>st</sup> phase  $\theta_{13} \sim 2.5^\circ$   
 $\sin^2 2\theta_{13} \sim 10^{-2}$



Super-K  
(50 Kton)

T2K 2<sup>nd</sup> phase  $\theta_{13} \sim 1^\circ$   
 $\sin^2 2\theta_{13} \sim 10^{-3}$



Hyper-K  
(500 Kton)

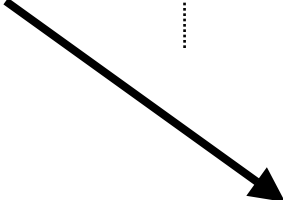
$$n \rightarrow p + e^- + \bar{\nu}_e$$

$$E_\nu \sim \text{MeV}$$

$$L_{\text{osc}} \sim \text{Km}$$

$$P(\nu_e) \simeq \frac{\sin^2 2\theta_{13}}{2} \cdot P_{\text{atm}}(\theta_{23}, |\Delta m_{23}^2|) + P_{\text{sol}}(\theta_{12}, \Delta m_{12}^2) \pm \sin 2\theta_{13} \cdot F_{\text{solar}} \cdot F_{\text{atm}}(\sin 2\theta_{23}, |\Delta m_{23}^2|) \cdot F(\delta_{\text{cp}}, \Delta m_{23}^2)$$

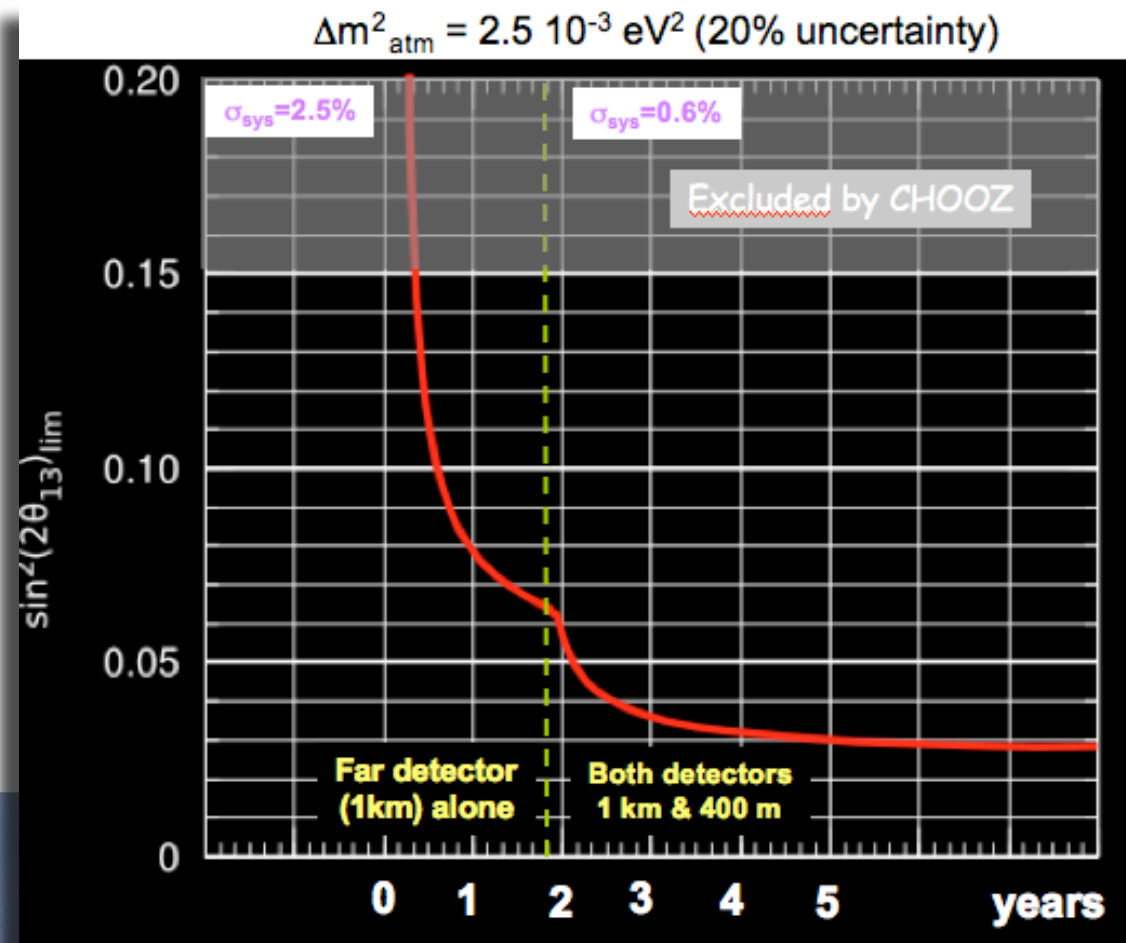
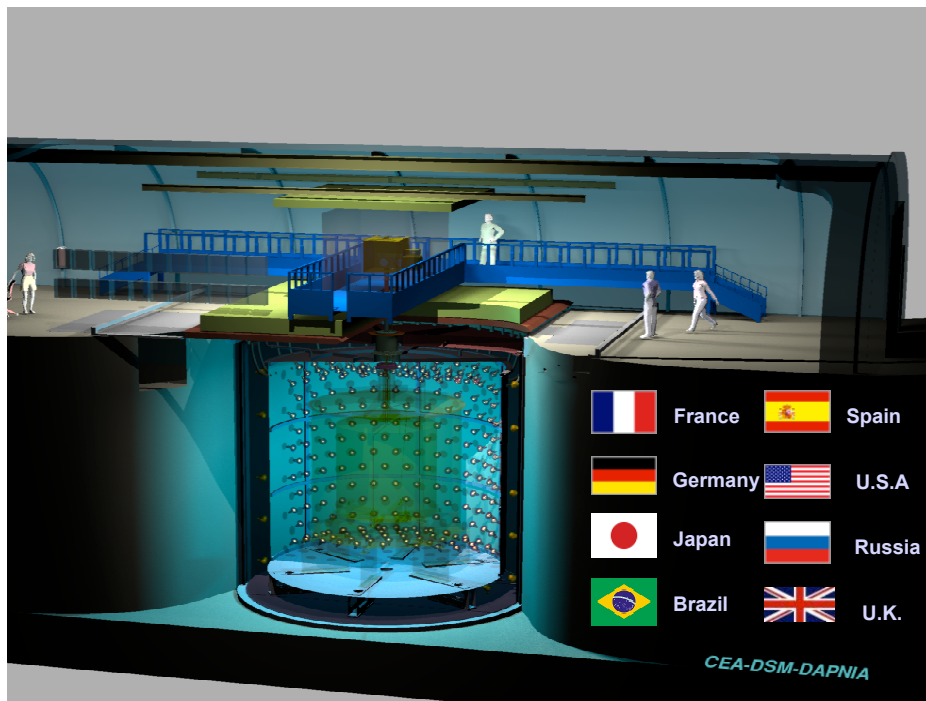
**atmospheric**
**solar**
**interference**



$$P_{\nu_e \nu_e} = 1 - P_{\nu_e \nu_\mu} - P_{\nu_e \nu_\tau} \simeq 1 - \sin^2 2\theta_{13} \cdot \sin^2 \left( \frac{\Delta m_{23}^2 L}{4E} \right)$$

## A clean probe of $\theta_{13}$

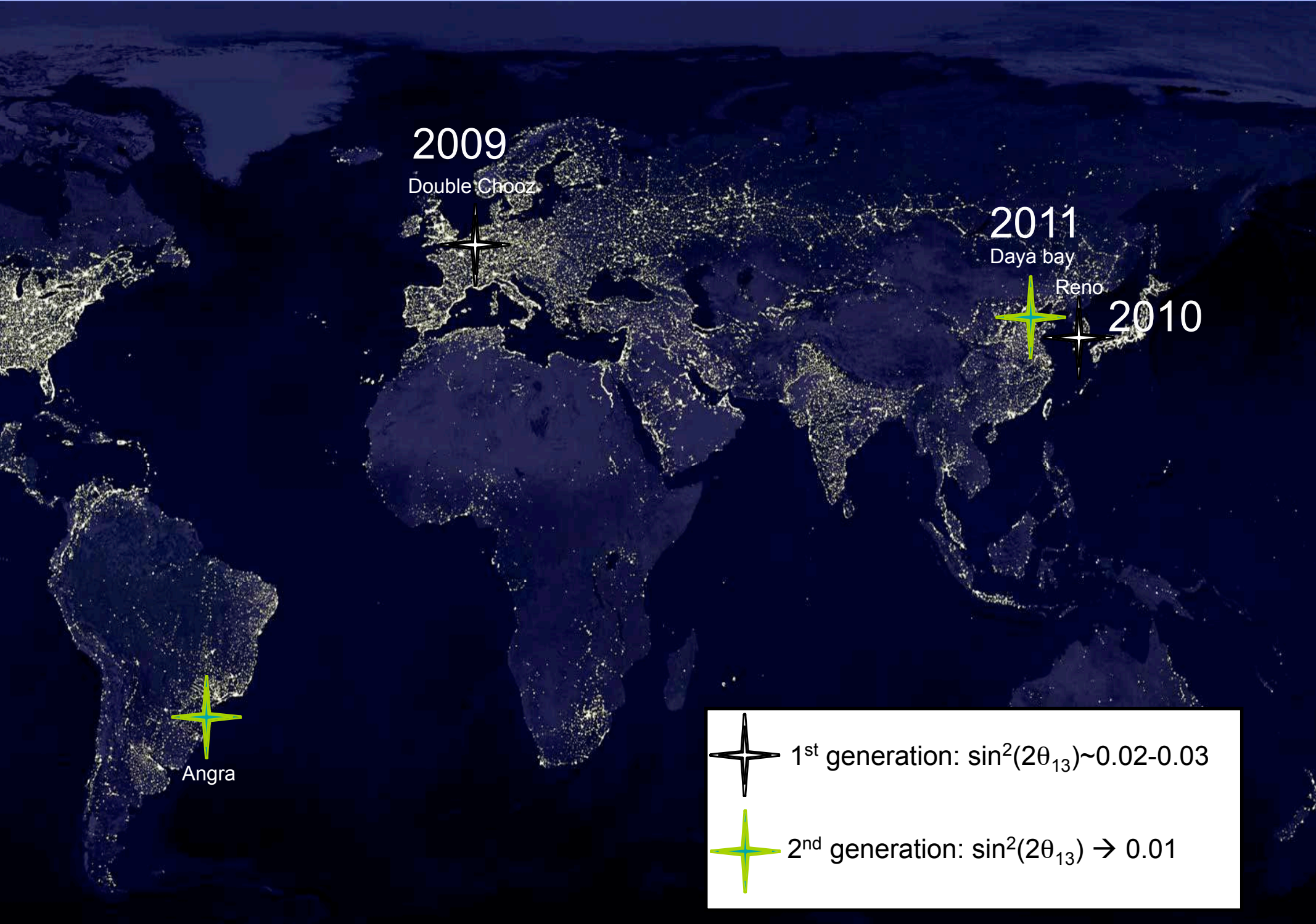
- Below muon and tau production thresholds: **disappearance**
- Interference term cancels out: **no dependency  $\delta_{\text{cp}}$**
- Short baseline: **no dependence on mass hierarchy**



## Timeline

- 2008-09: Far detector construction and integration
- Mid-2009: Phase I data taking
- 2008-10: near site and detector
- 2011: Start of phase II data taking





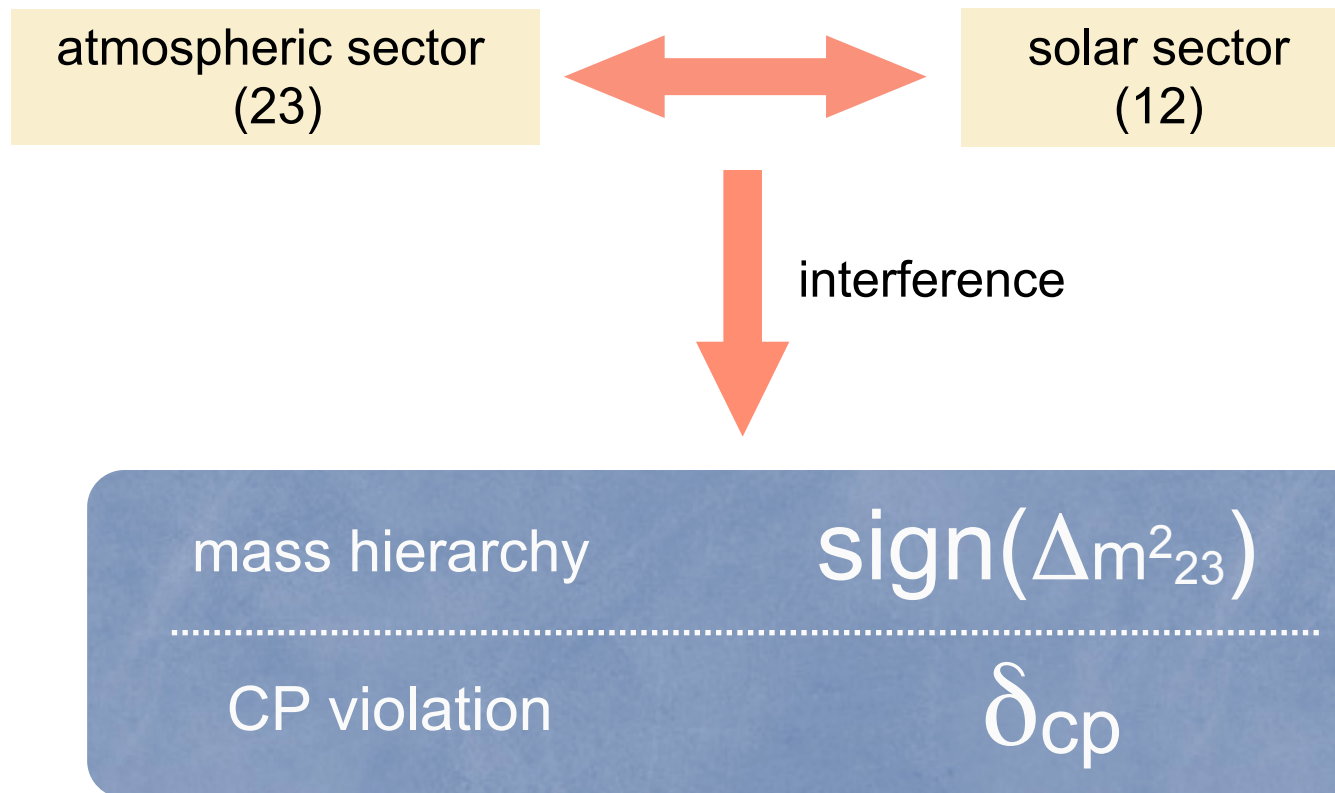


# The path to leptonic CP violation

# Beyond T2K and Double-Chooz

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If Nature is generous T2K, D-Chooz, ... will observe the subdominant oscillation  $\nu_\mu \rightarrow \nu_e$  ( $\nu_e \rightarrow \nu_e$ ) and measure  $\theta_{13}$





# Studying the interference

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However, observing a positive interference ( $\theta_{13} \neq 0$ ) is one thing but studying different interference patterns is much more difficult

**atmospheric**

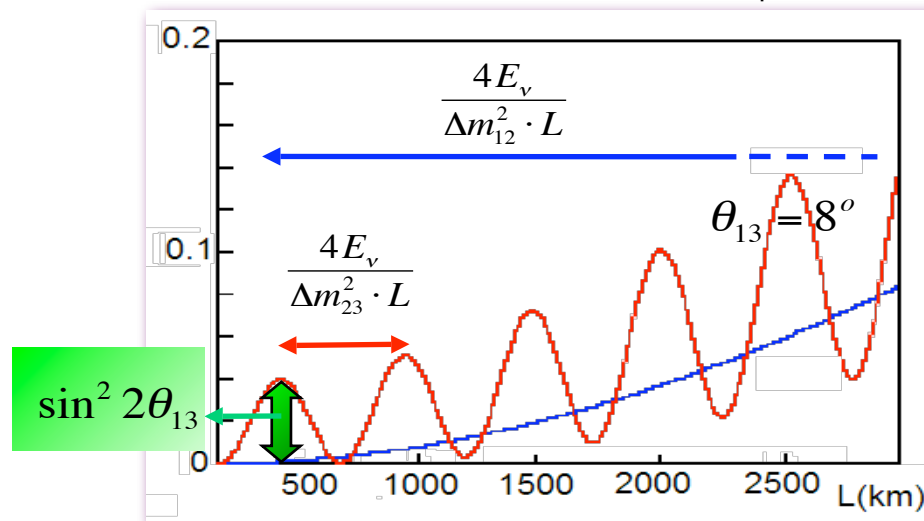
**solar**

**interference**

$$P(\text{no } \nu_e) \simeq \cos^2 2\theta_{13} \cdot P_{atm}(\theta_{23}, |\Delta m_{23}^2|)$$

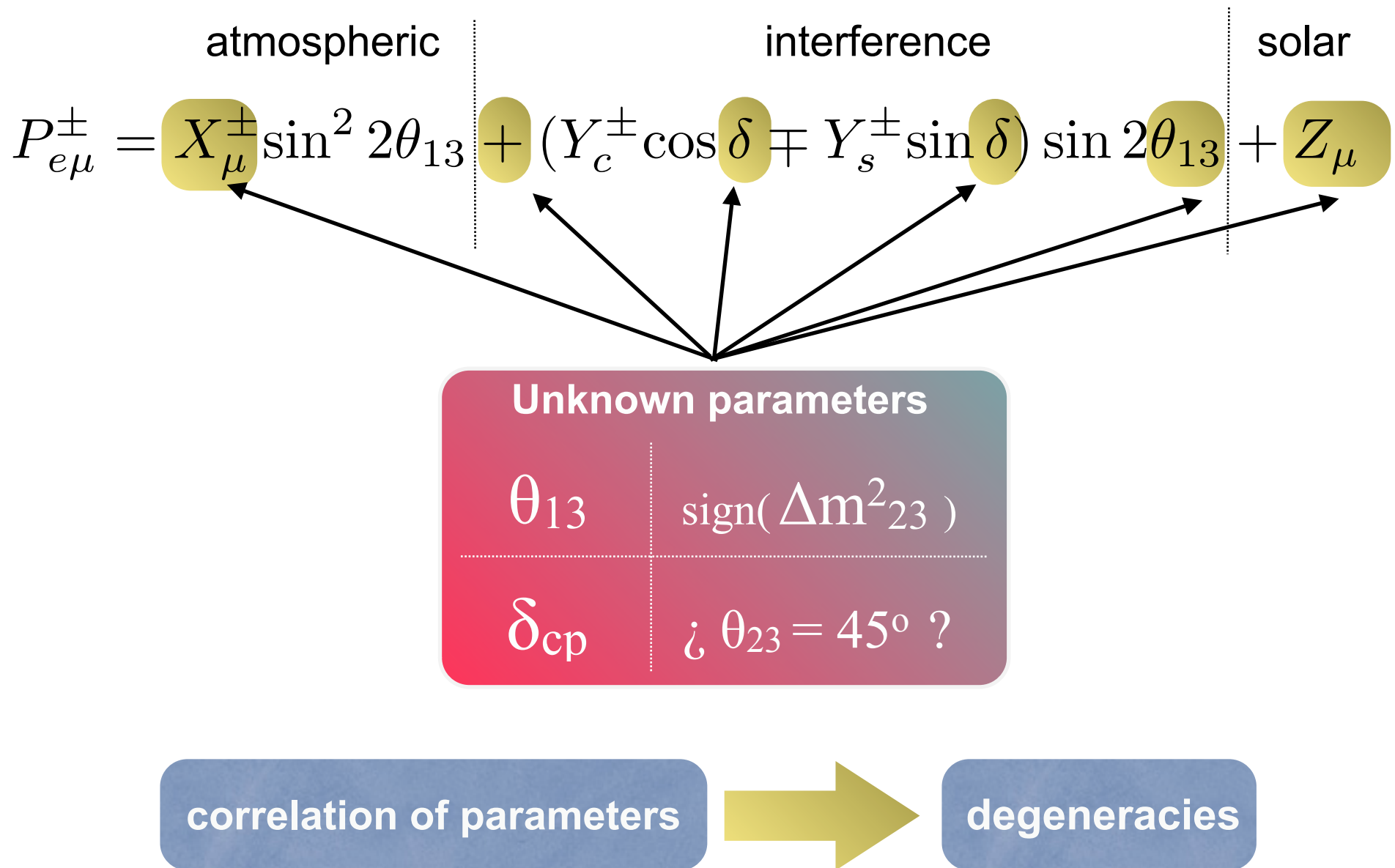
$$P(\nu_e) \simeq \sin^2 2\theta_{13} \cdot P_{atm}(\theta_{23}, |\Delta m_{23}^2|) + P_{sol}(\theta_{12}, \Delta m_{12}^2)$$

$$\pm \sin 2\theta_{13} \cdot F_{solar} \cdot F_{atm}(\sin 2\theta_{23}, |\Delta m_{23}^2|) \cdot F(\delta_{cp}, \Delta m_{23}^2)$$



# Correlations and degeneracies

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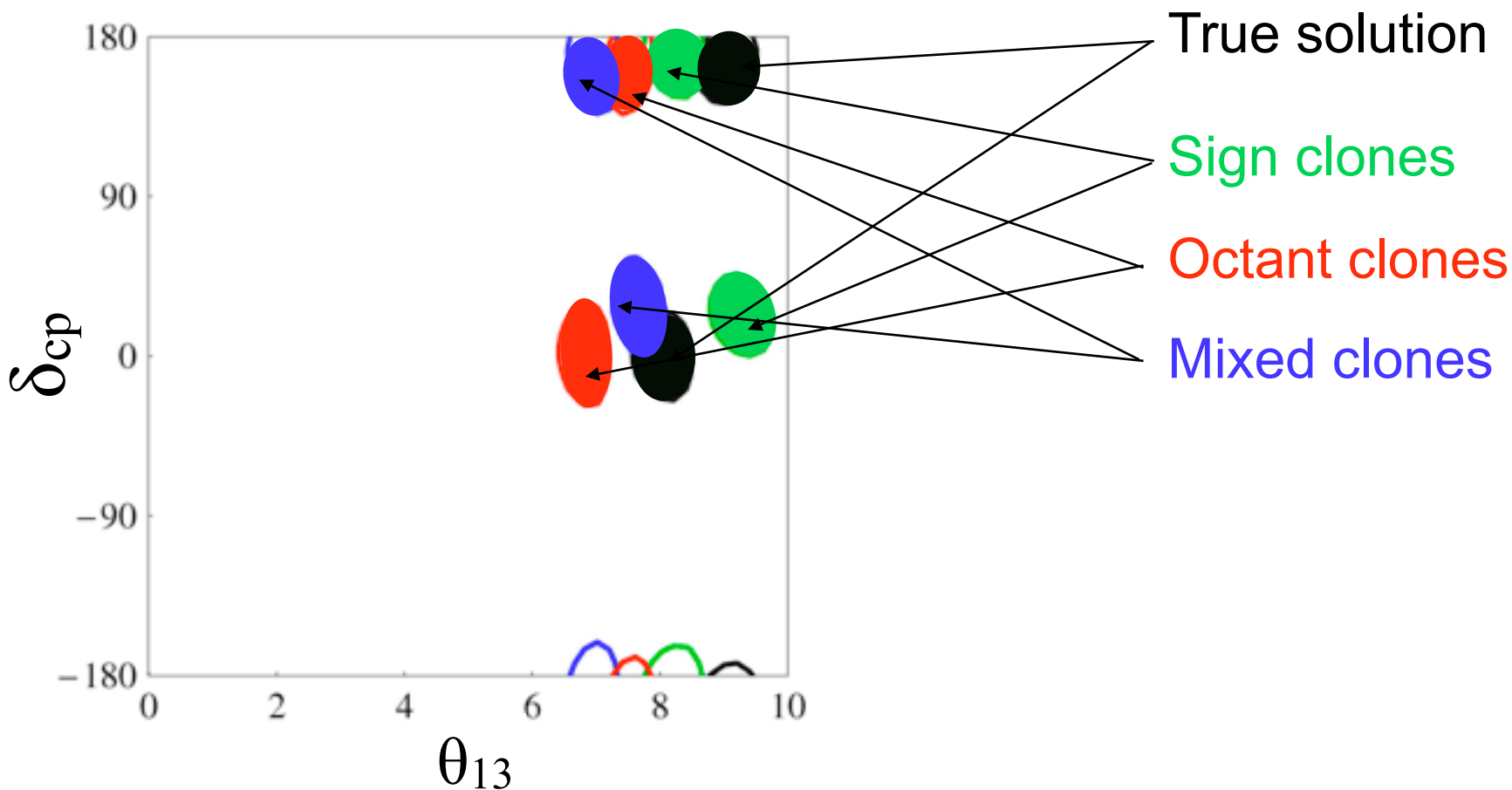


# The attack of the clones

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$$P_{e\mu}^{\pm} = \underbrace{X_{\mu}^{\pm} \sin^2 2\theta_{13}}_{\substack{\theta_{23} > 45^\circ \text{ or } \theta_{23} < 45^\circ \\ \text{octant}}} + \underbrace{(Y_c^{\pm} \cos \delta \mp Y_s^{\pm} \sin \delta)}_{\text{sign } \Delta m_{23}^2} \sin 2\theta_{13} + \underbrace{Z_{\mu}}_{\substack{\theta_{23} > 45^\circ \text{ or } \theta_{23} < 45^\circ \\ \text{octant}}}$$

atmospheric                      interference                      solar





## degeneracy solvers

several channels

several energies

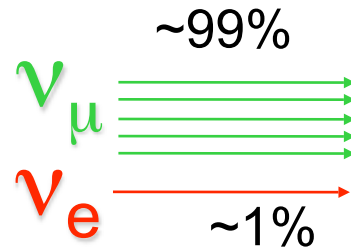
several baselines



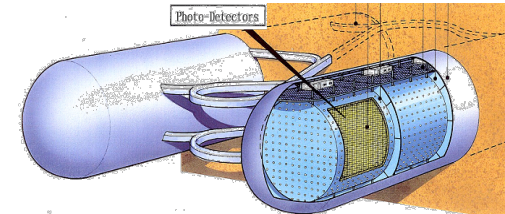
maximises the synergies  
with other Physics

- unitarity
- dark matter
- T violation
- CPT tests
- ...

## Super beams II

 $\pi^+$ 


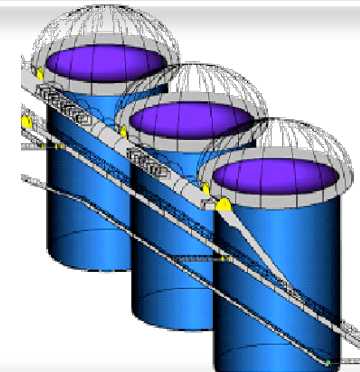
< 5 GeV



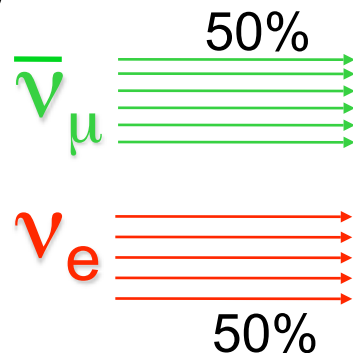
## Beta beam

 $^{18}_{10}Ne$ 

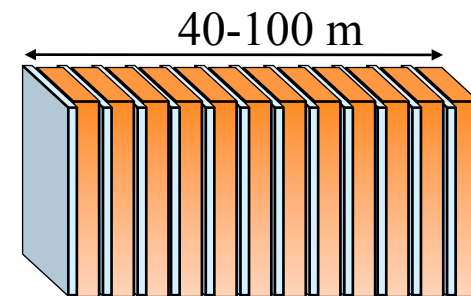

< 5 GeV



## Neutrino factory

 $\mu^+$ 


<20-50 GeV



## strategy

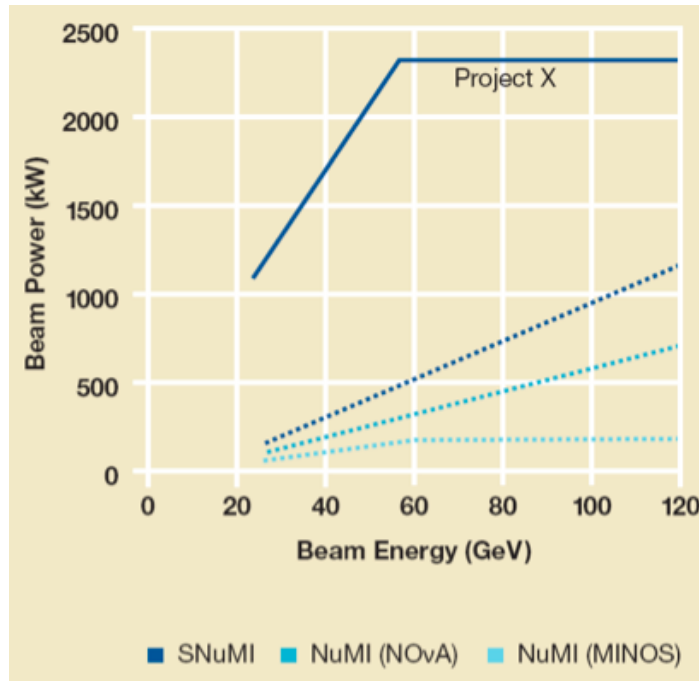
- More powerful beams (x 10)
- Bigger detectors (x 10)
- Longer distances to explore mass hierarchy ( $> 800$  Km)

wide band beams versus off-axis beams

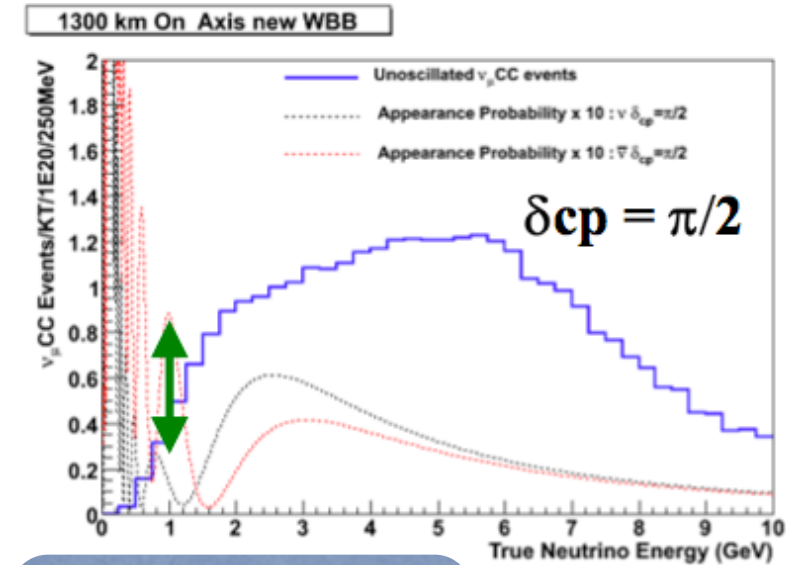


# Fermilab programme

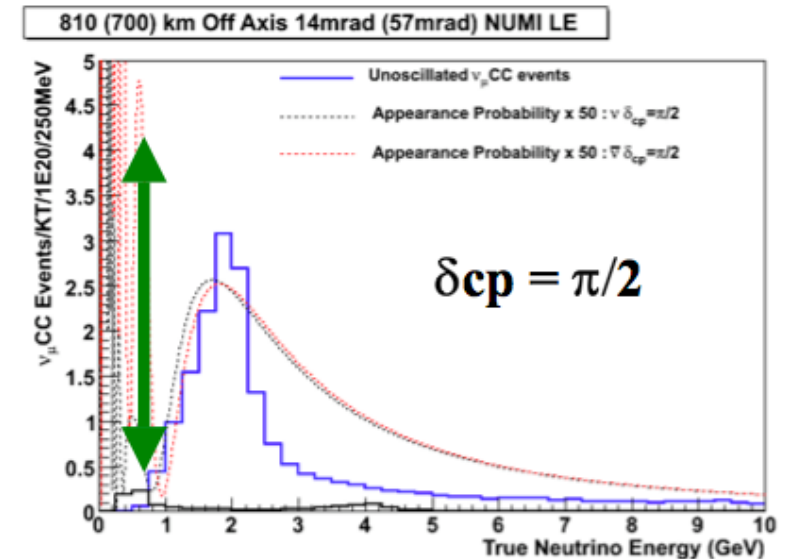
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## on-axis (Wide Band Beam)

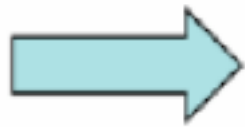


## off-axis beam



## Linac : 181 MeV to 400 MeV

0.60 MW  
0.28 Hz

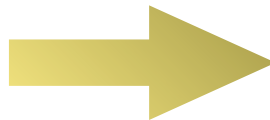
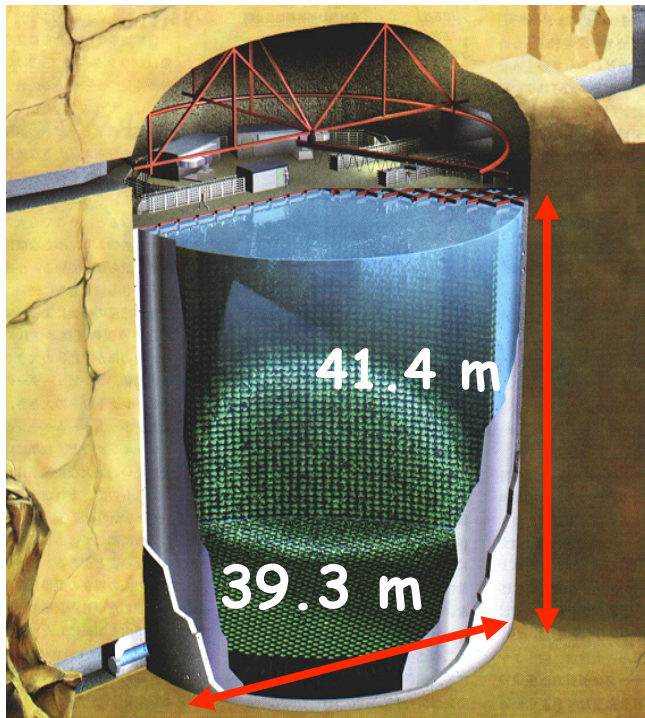


0.91 MW  
0.57 Hz

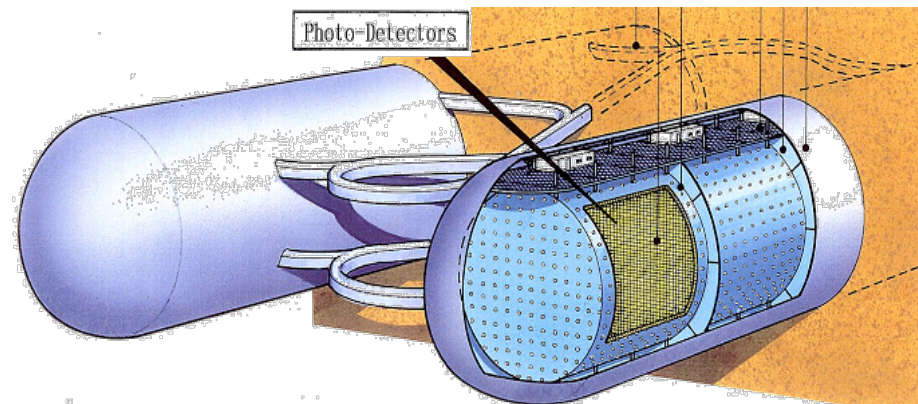


1.66 MW  
0.52 Hz

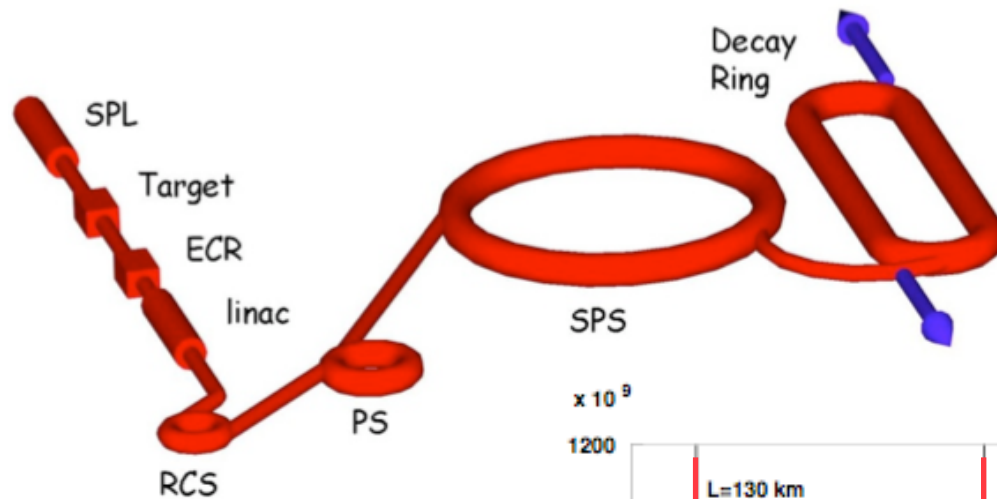
50 Kton



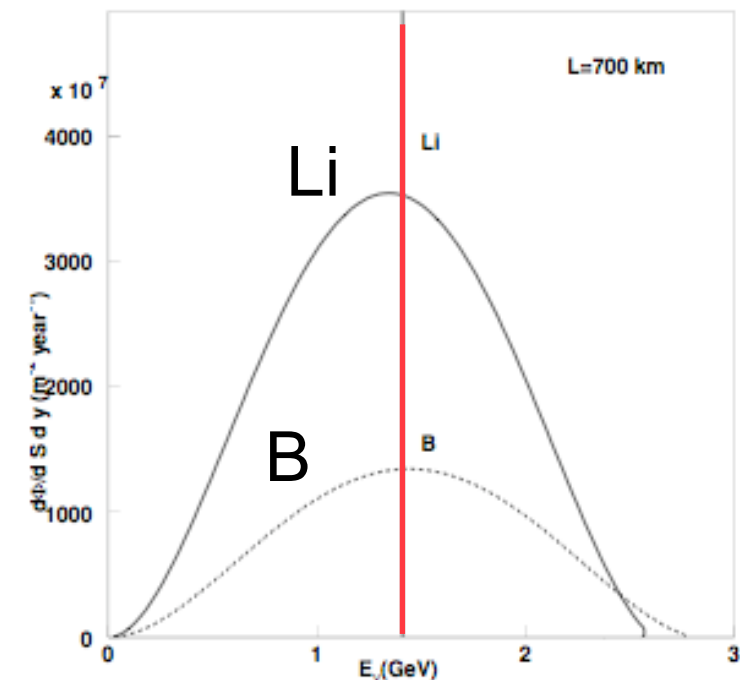
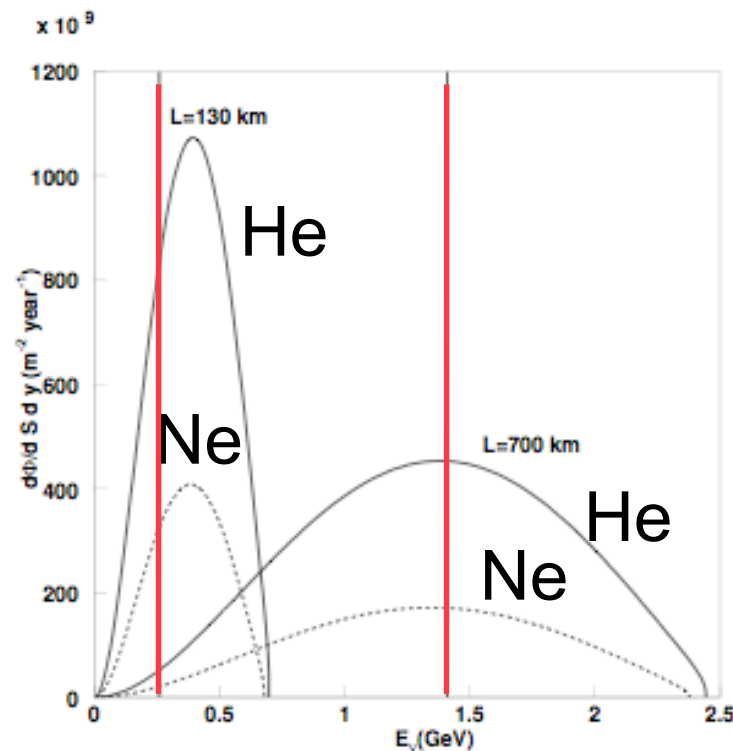
500 Kton



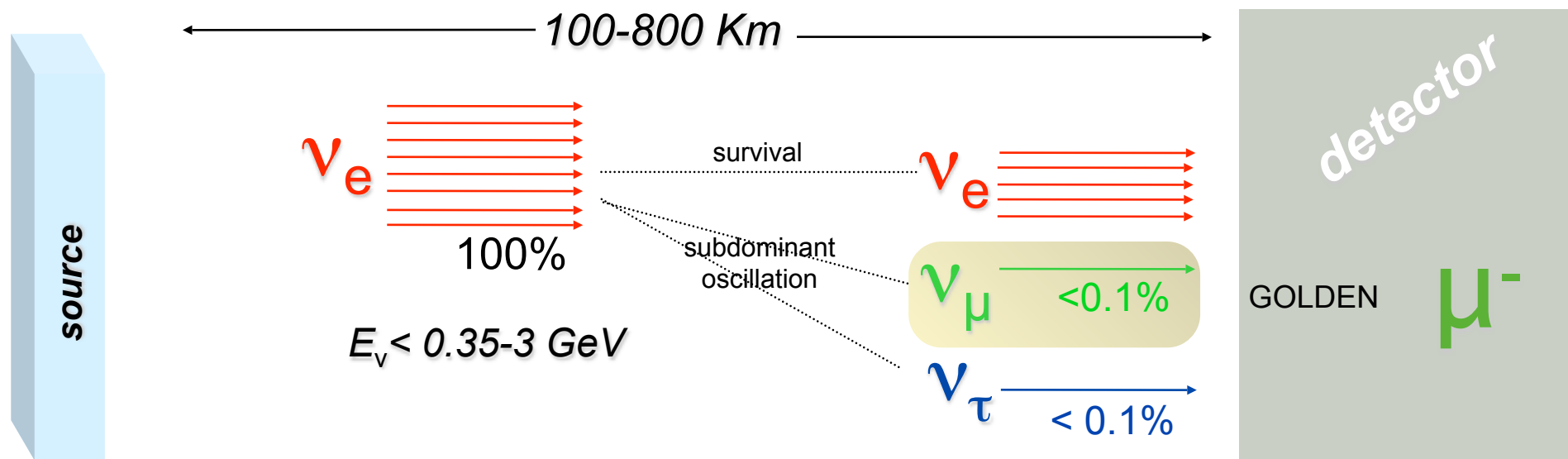
Pure  $\nu_e$  beam  $\rightarrow$  small beam systematics and backgrounds



Ion	$\gamma$	$L(\text{km})$	$\bar{\nu}_e$ CC	$\nu_e$ CC	$\langle E_\nu \rangle (\text{GeV})$
He/Ne	100	130	28.9	32.8	0.39/0.37
He/Ne	350	700	62.0	55.	1.35/1.3
Li/B	100	700	5.0	4.9	1.3/1.4

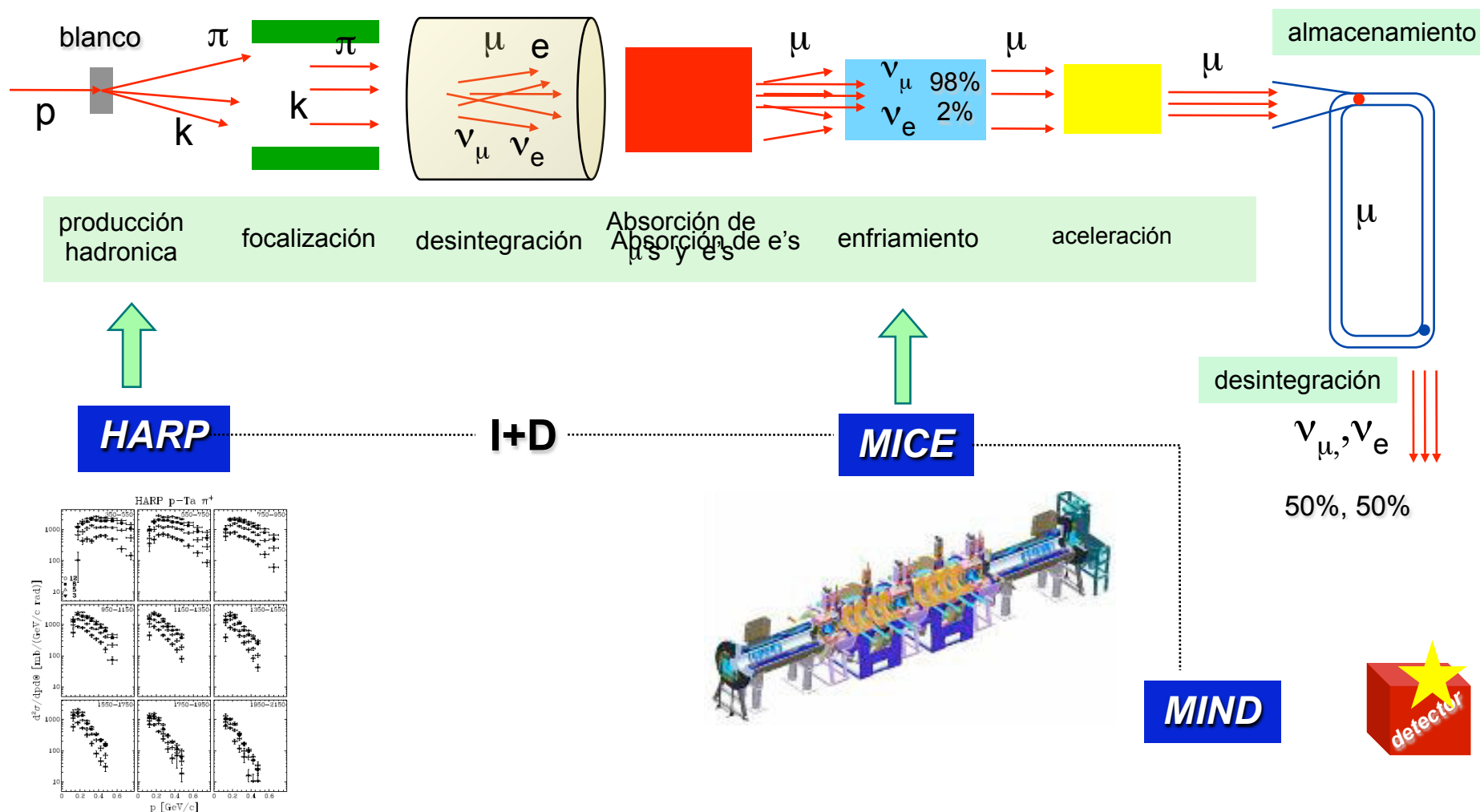






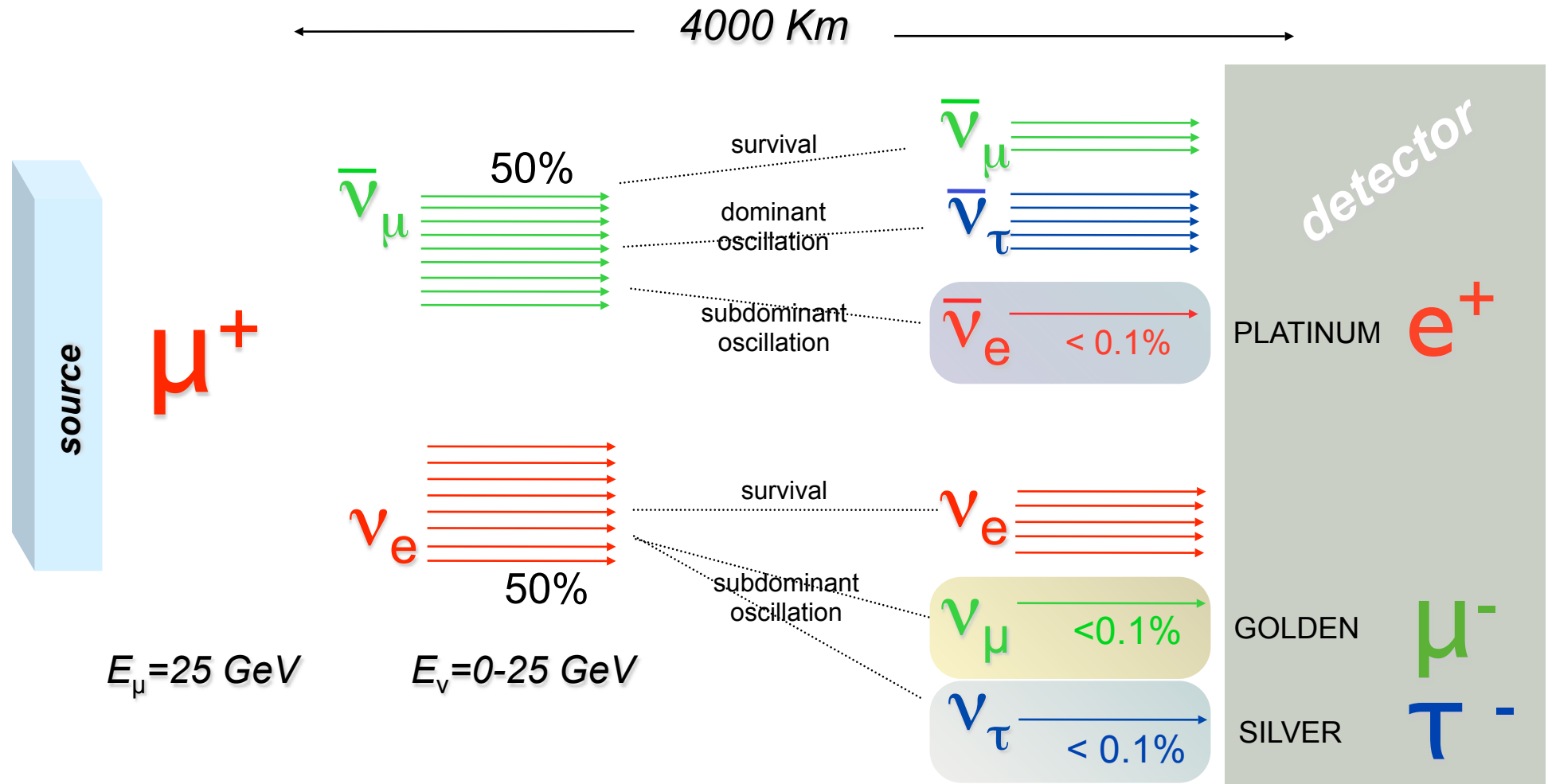
Relatively short baseline ➡ small sensitivity to mass hierarchy

# The neutrino factory



# The neutrino factory

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The ideal detector should be able to detect **e,  $\mu$ ,  $\tau$**  and identify their **charge**



	atmospheric	interference	solar
golden	$P_{e\mu}^{\pm} = X_{\mu}^{\pm} \sin^2 2\theta_{13}$	$+ (Y_c^{\pm} \cos \delta \mp Y_s^{\pm} \sin \delta) \sin 2\theta_{13}$	$+ Z_{\mu}$
platinum	$P_{\mu e}^{\pm} = X_{\mu}^{\pm} \sin^2 2\theta_{13}$	$+ (Y_c^{\pm} \cos \delta \pm Y_s^{\pm} \sin \delta) \sin 2\theta_{13}$	$+ Z_{\mu}$
silver	$P_{e\tau}^{\pm} = X_{\tau}^{\pm} \sin^2 2\theta_{13}$	$- (Y_c^{\pm} \cos \delta \mp Y_s^{\pm} \sin \delta) \sin 2\theta_{13}$	$+ Z_{\tau}$

golden      Easy to detect muons and measure their charge

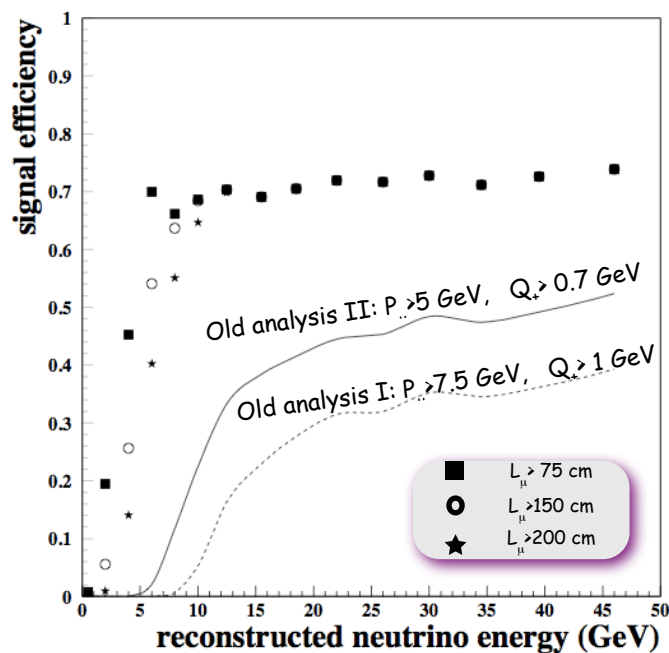
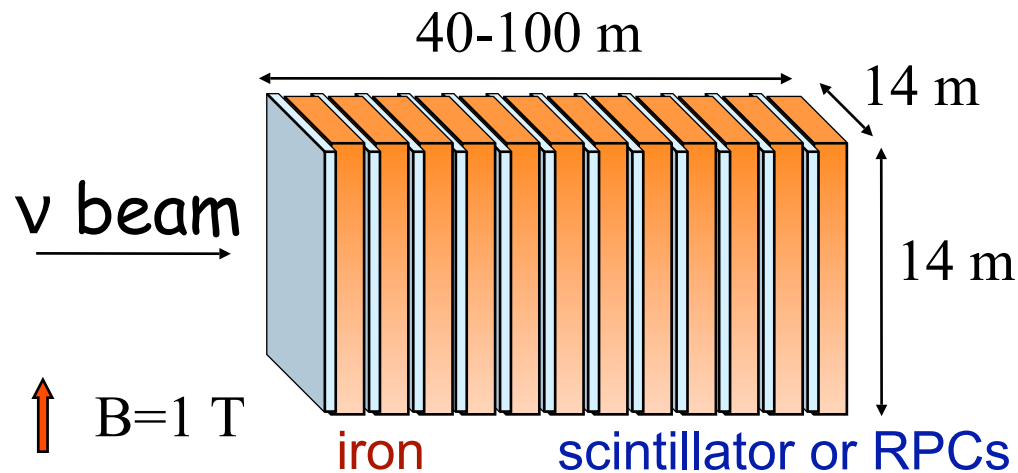
platinum      Electron charge identification is complicated

silver      Tau detection requires emulsions  
Not all tau decay channels are useful

Statistically limited  
Expensive

# The golden detector: MIND

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Energy threshold 3-5 GeV  
Modest energy resolution  
Insensitive to taus and electrons

Maybe not  
sufficient

## degeneracy solvers

several channels

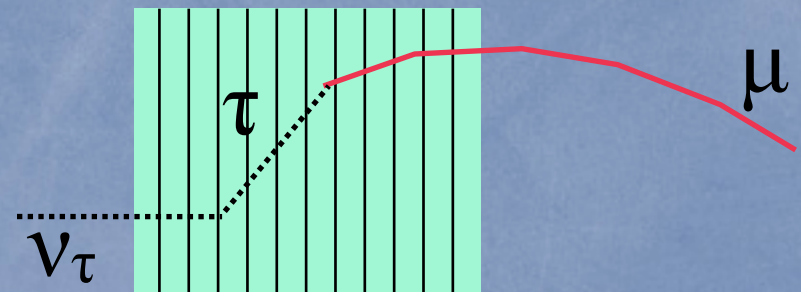
several energies

several baselines

- Expensive option
- It implies new detector technologies

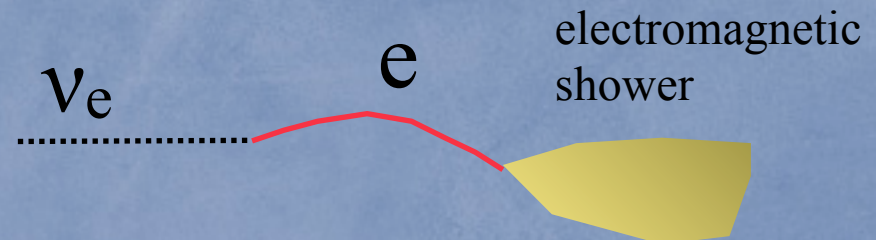
## 1. Detection of taus (silver channel)

- emulsions (OPERA-like)
- Baseline option is 15 Kton



## 2. Detection of electrons (platinum channel)

- emulsions
- liquid argon (in R&D phase)



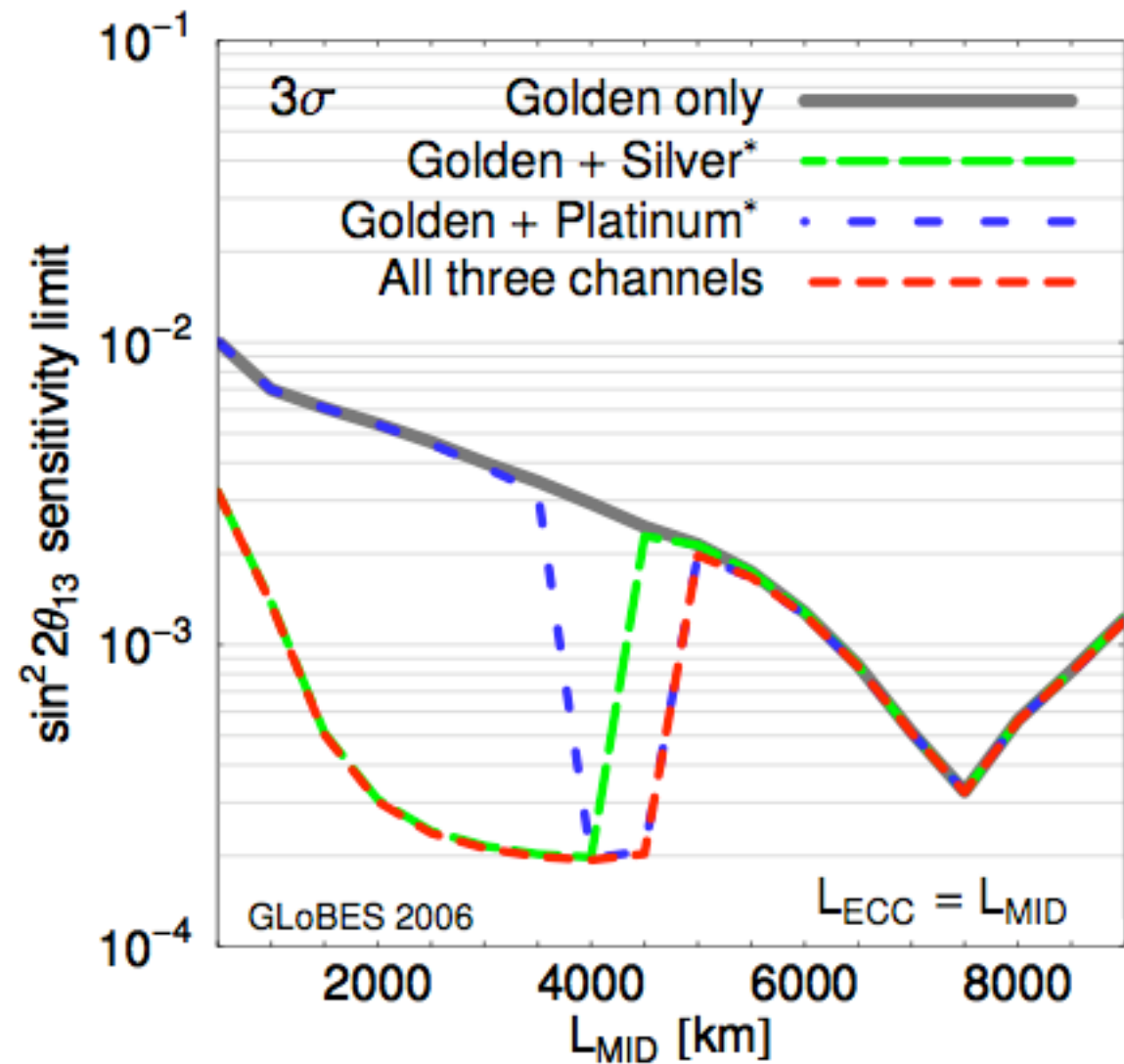


golden 50 Kton MIND

silver 5 Kton emulsions

platinum 15 Kton Liquid Argon

Ideally one would like to build a very massive hybrid detector able to measure all oscillation channels at a reasonable cost



## degeneracy solvers

several channels

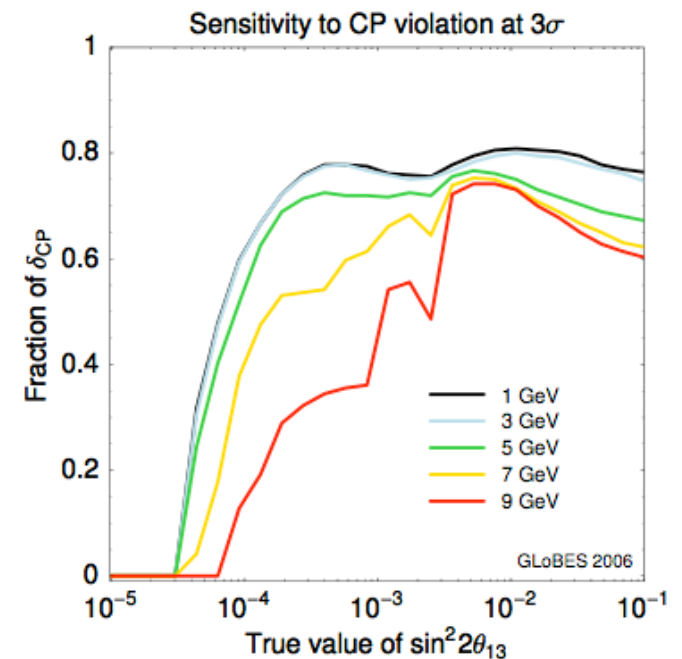
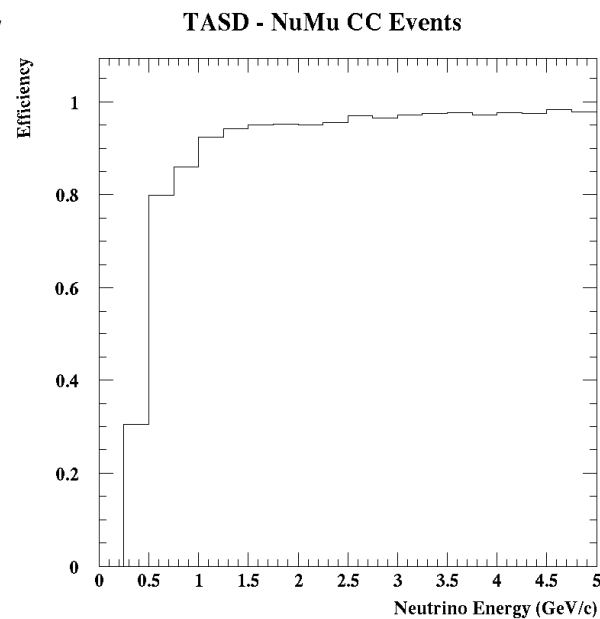
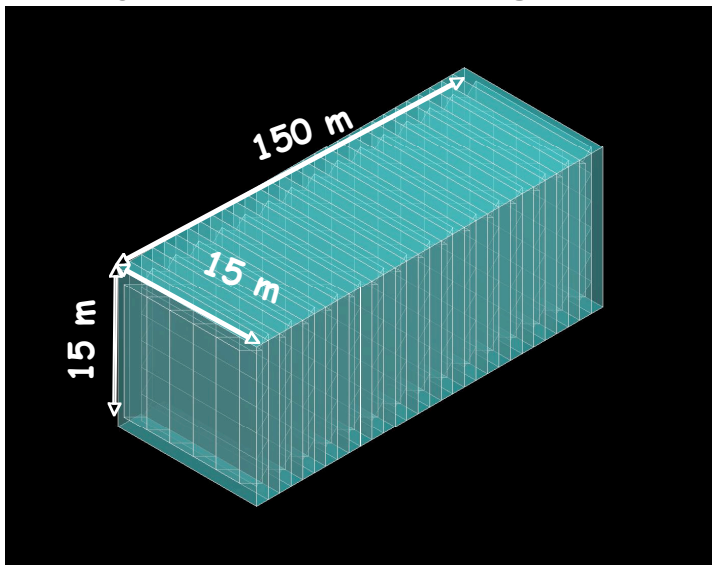
**several energies**

several baselines

## Options

- Improve energy resolution
- Reduce threshold to detect second maximum

## Totally Active Scintillating Detector

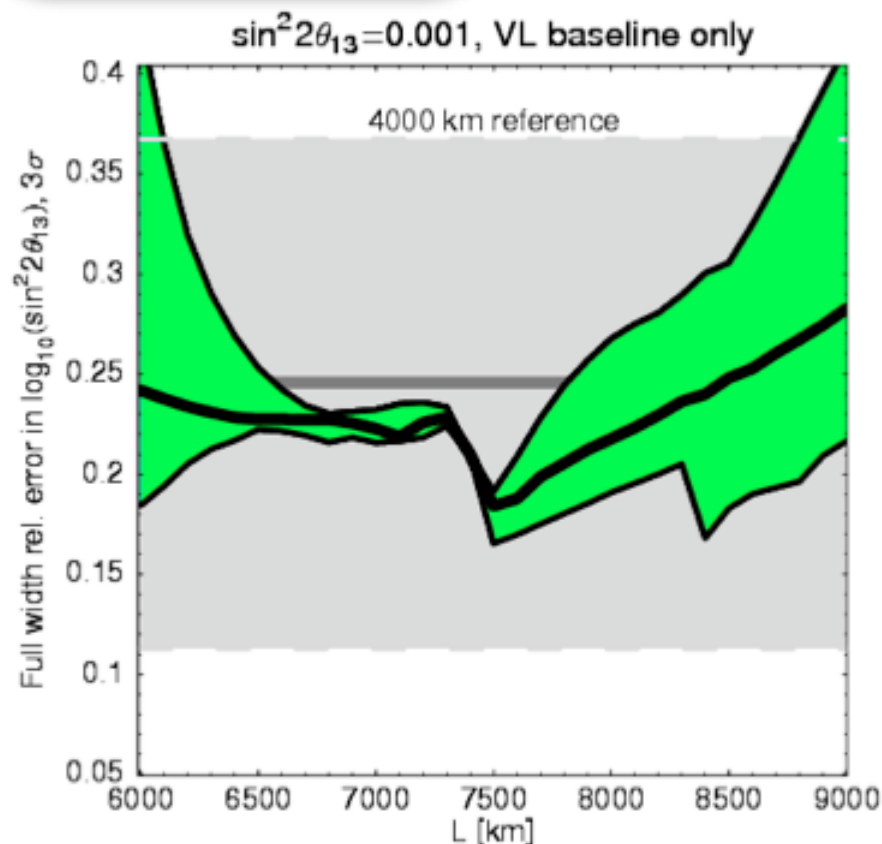


## degeneracy solvers

several channels

several energies

**several baselines**



At  $\sim 7500$  Km the oscillation probability is independent of  $\delta_{CP}$

Good to measure  $\theta_{13}$  and solve the intrinsic degeneracy

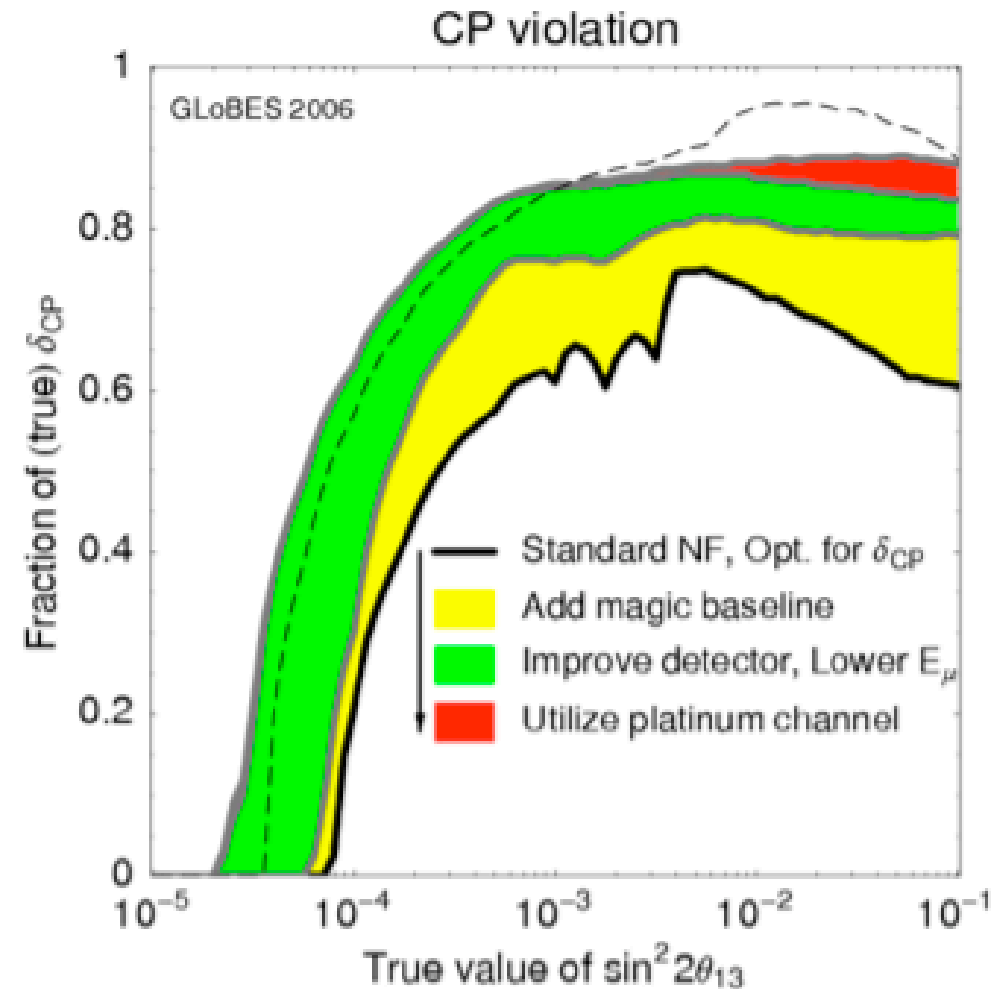
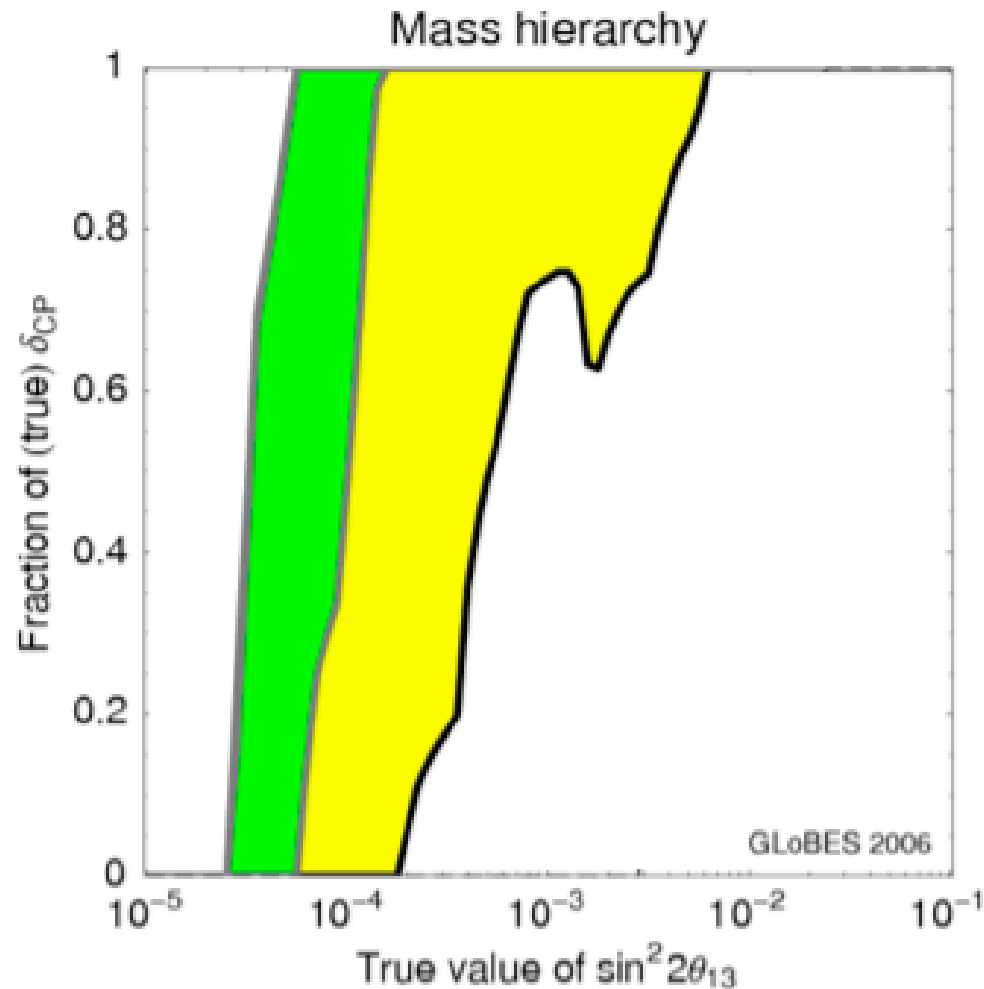
In combination with the intermediate baseline (4000 Km) constitutes a good option

Two MIND-like detectors: feasible and “cheap”



# Which neutrino factory ?

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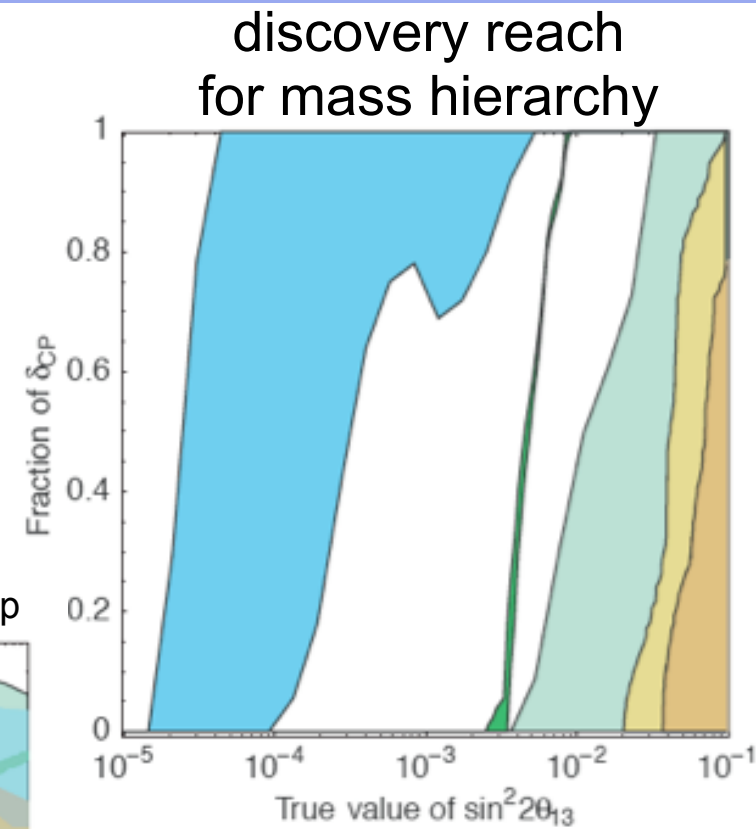
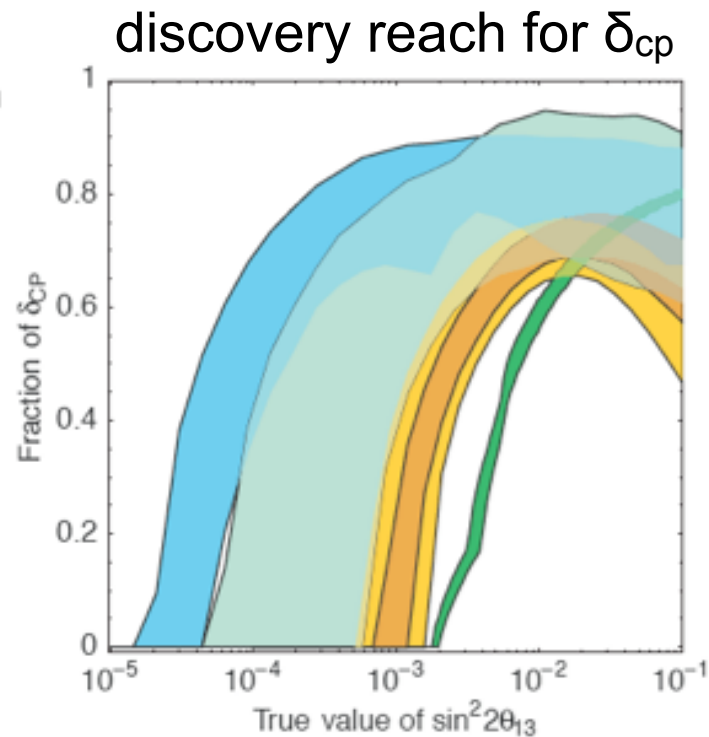
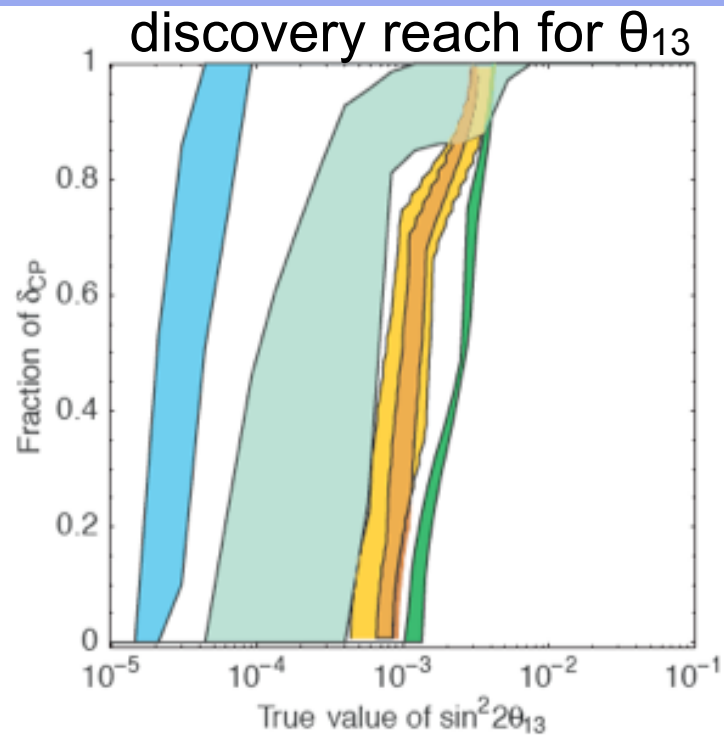
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And  
the winner  
is ...



# Comparison of facilities

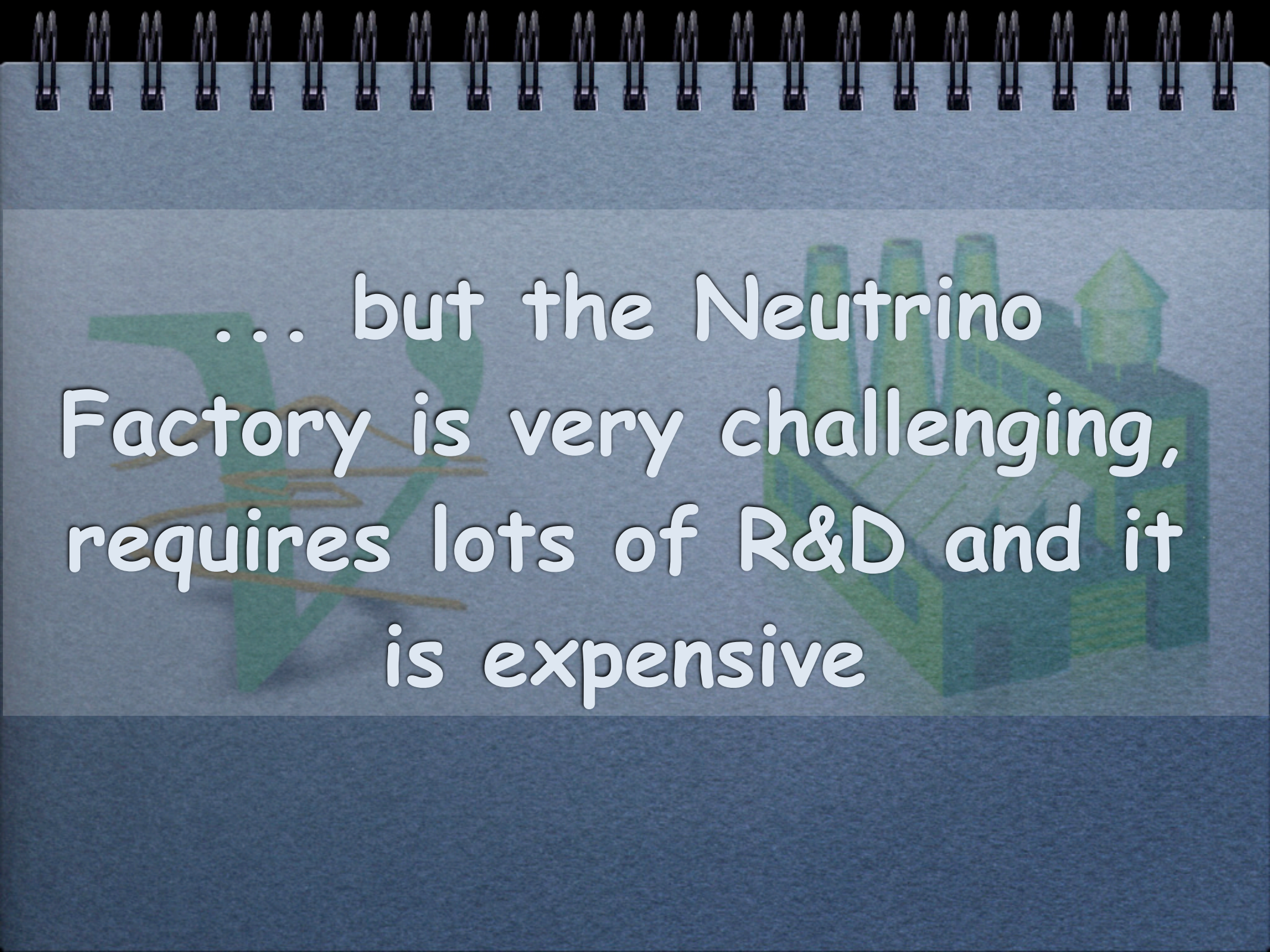
40





Which road  
to take





... but the Neutrino  
Factory is very challenging,  
requires lots of R&D and it  
is expensive





Do we need  
such a powerful facility ?



Beta-Beam is also challenging,  
but probably less.

It is also very expensive,  
but may be less.

However it has much lower  
sensitivity to mass hierarchy.

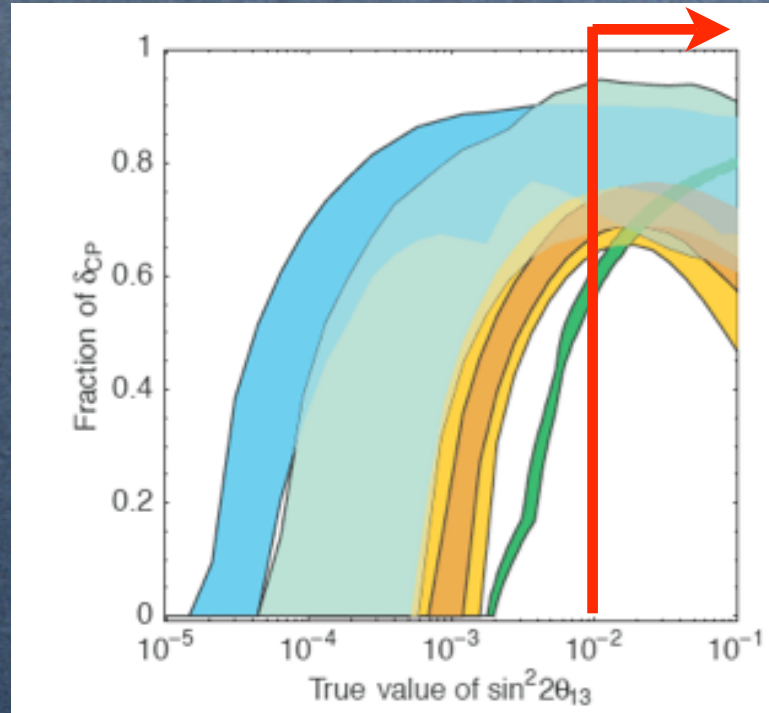


everything depends on the  
value of  $\theta_{13}$



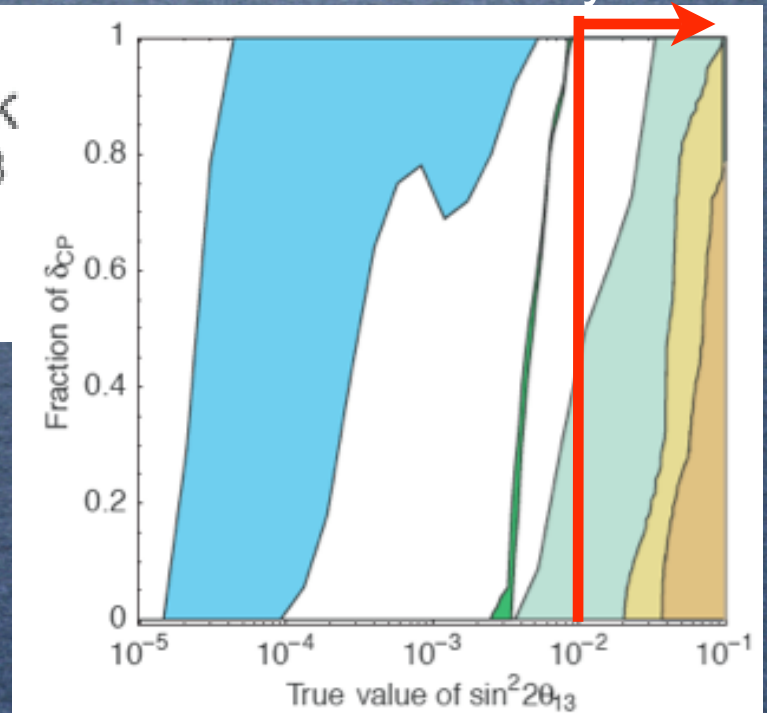
# Hypothesis I: we measure $\theta_{13}$ by 2012

discovery reach for  $\delta_{CP}$



SPL  
T2HK  
WBB  
NF  
BB

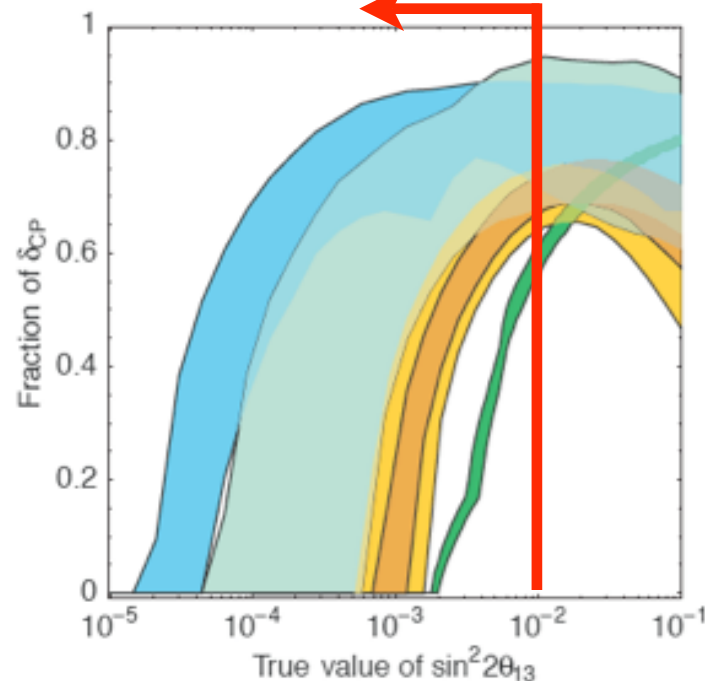
discovery reach  
for mass hierarchy



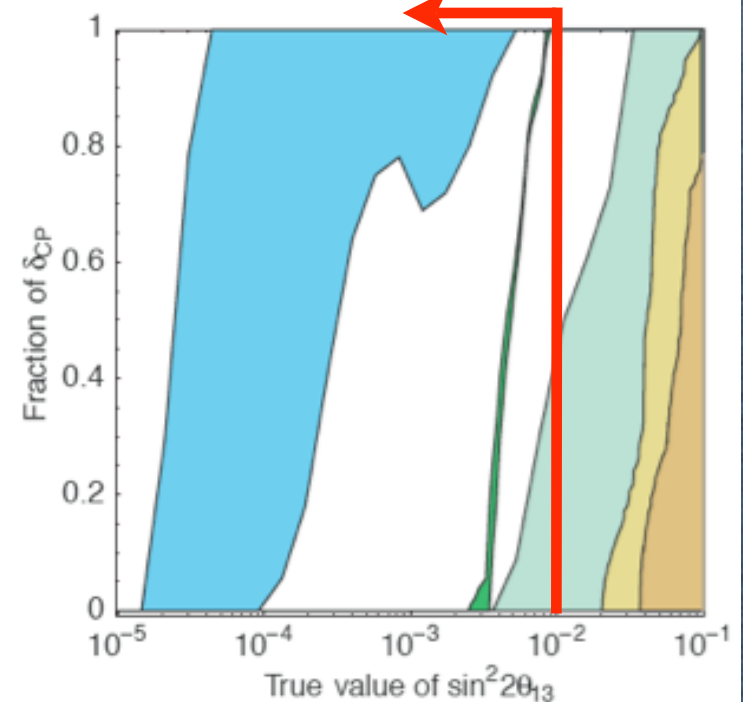


# Hypothesis II: $\theta_{13}$ unknown by 2012

discovery reach for  $\delta_{CP}$

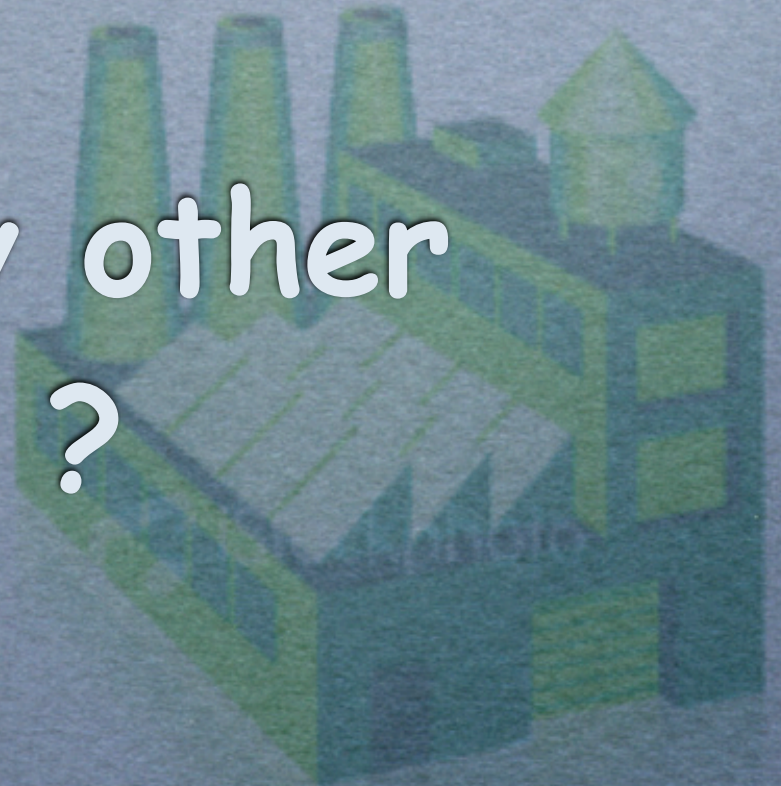
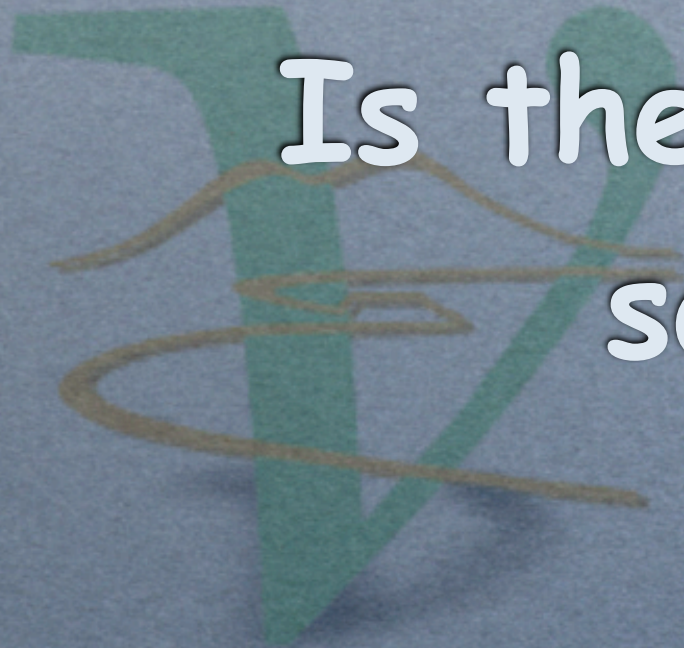


discovery reach  
for mass hierarchy





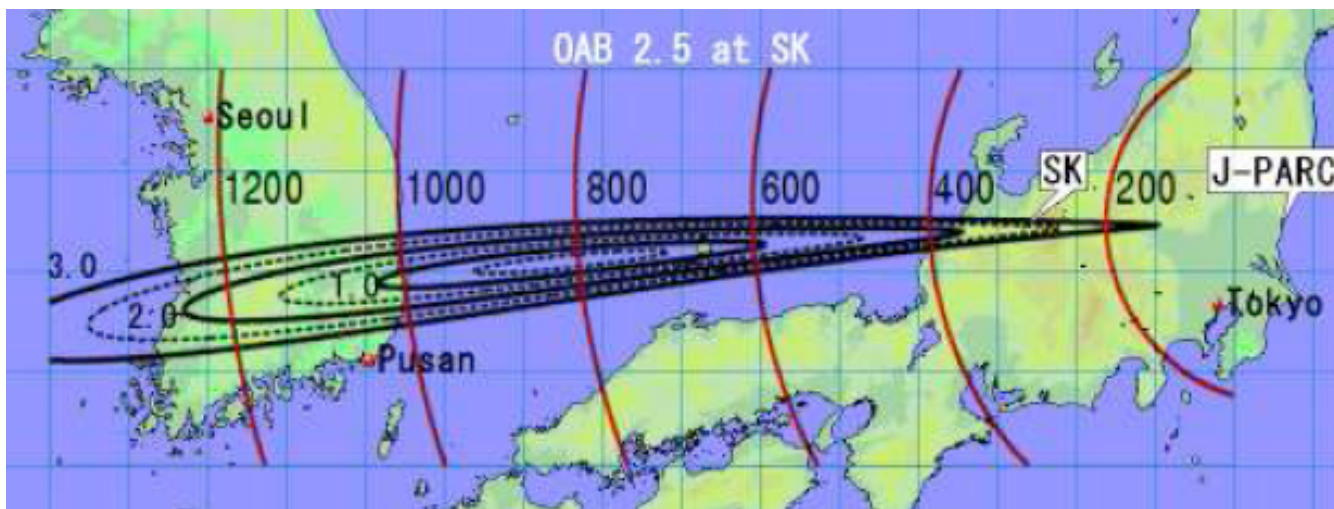
Is there any other  
solution ?





# A variety of ideas

- Electron capture beta beam (monoenergetic)
- Beta-beam with two ions and two baselines
- Beta-beam with two ions at a single baseline
- Beta-beam combined with a super-beam (CPT conjugates)
- Beta-beam or super-beam combined with atmospheric data
- Super-beam with two detectors at different baselines and off-axis angles (T2KK)



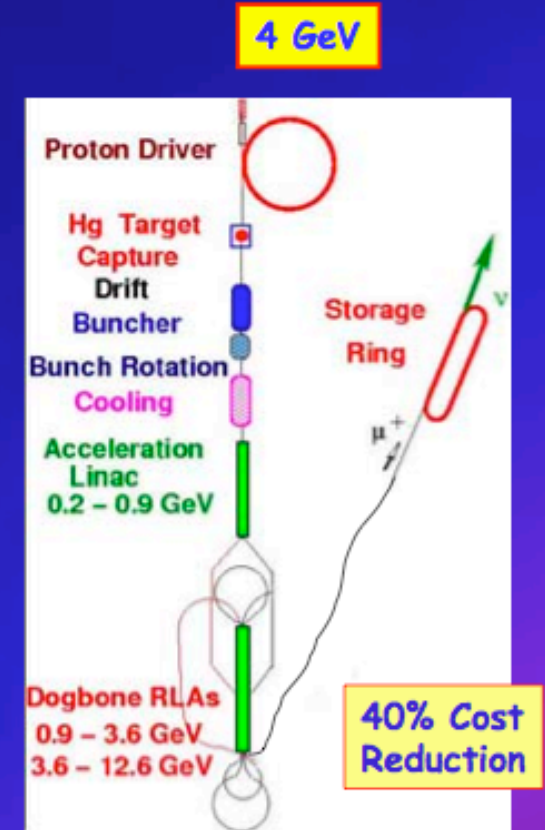
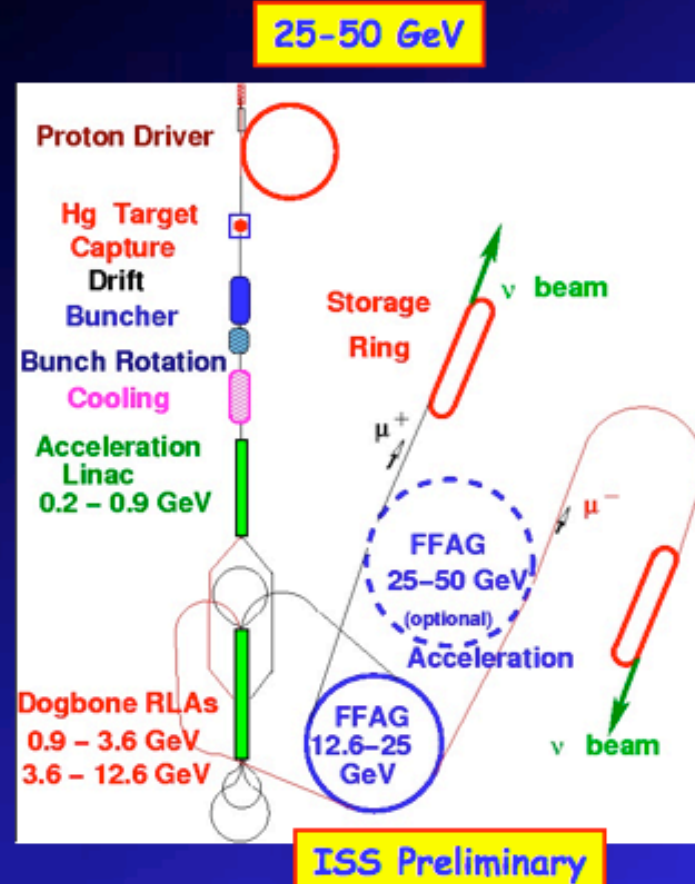


# Low Energy Neutrino Factory

50



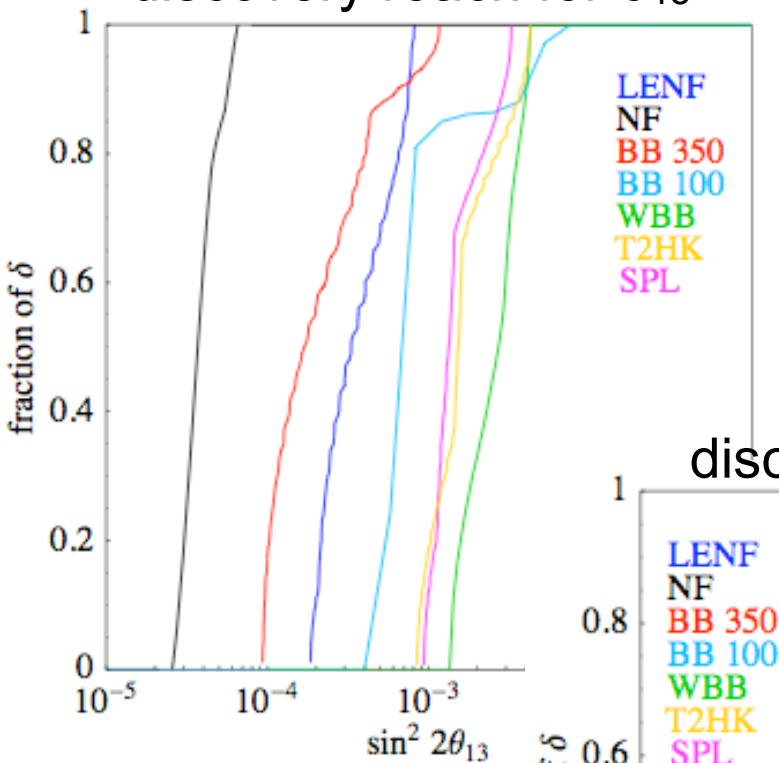
*Well, Cost is Certainly a Motivation*



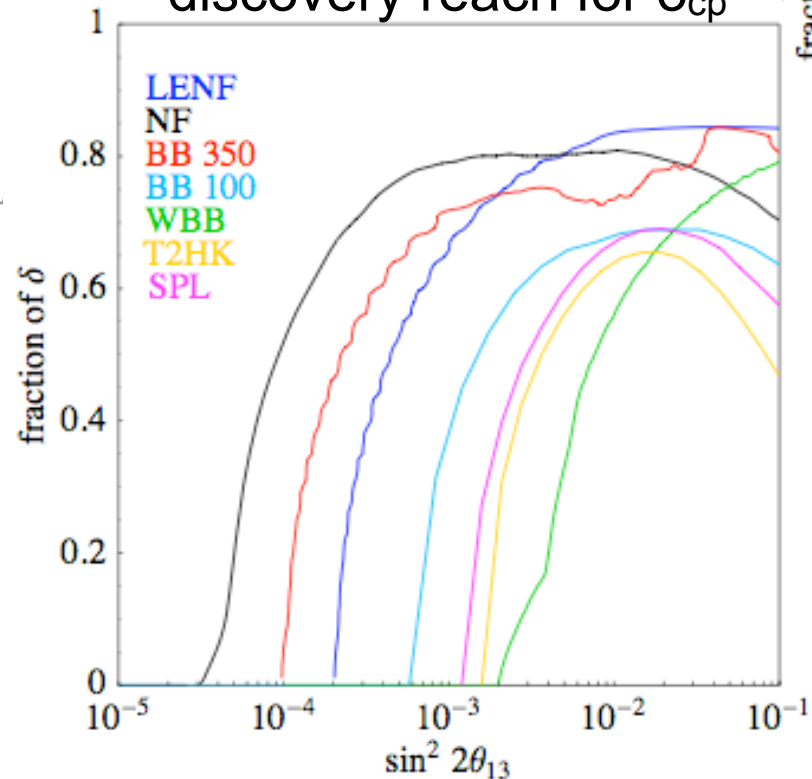
# Expected sensitivity for LENF

51

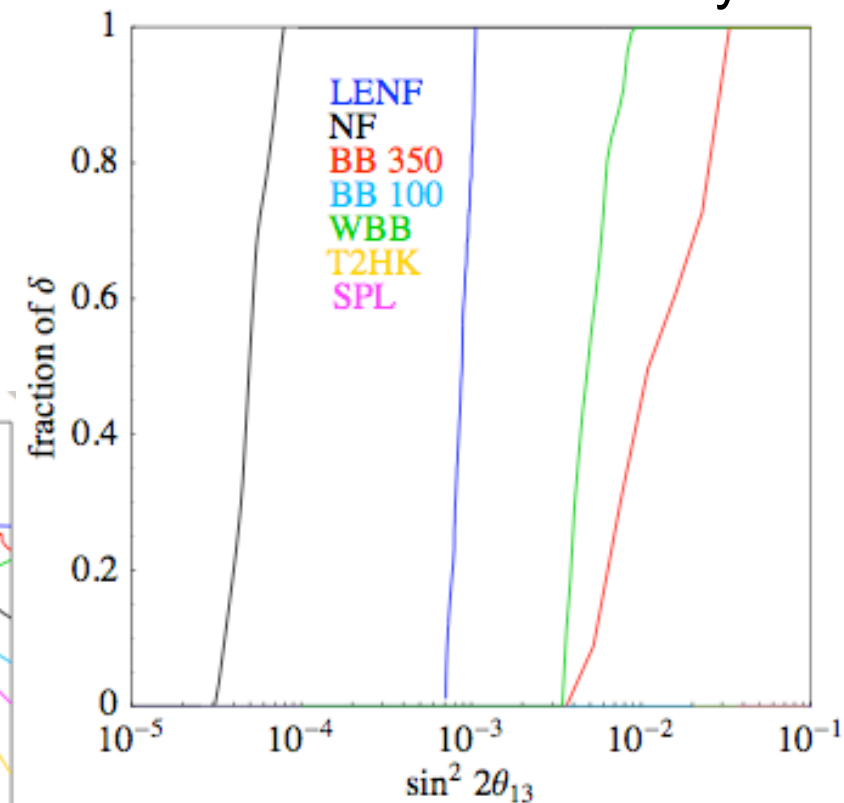
discovery reach for  $\theta_{13}$



discovery reach for  $\delta_{cp}$



discovery reach for mass hierarchy





There is no final strategy  
yet and several options are  
still opened



We should do our home  
work in order to be  
prepared to take a decision  
by 2012



decision =  $f(\theta_{13}, \epsilon, \dots)$

thanks